

## **EARLY ONLINE RELEASE**

This is a PDF of a manuscript that has been peer-reviewed and accepted for publication. As the article has not yet been formatted, copy edited or proofread, the final published version may be different from the early online release.

This pre-publication manuscript may be downloaded, distributed and used under the provisions of the Creative Commons Attribution 4.0 International (CC BY 4.0) license. It may be cited using the DOI below.

The DOI for this manuscript is

DOI:10.2151/jmsj.2020-049

J-STAGE Advance published date: July 14th 2020

The final manuscript after publication will replace the preliminary version at the above DOI once it is available.

1  
2 **Assimilation of Lidar**

3 **Water Vapour Mixing Ratio and Temperature Profiles**  
4 **into a Convection-Permitting Model**

5  
6 **Rohith THUNDATHIL**

7  
8 **and**

9  
10 **Thomas SCHWITALLA, Andreas BEHRENDT, Shravan Kumar**  
11 **MUPPA\*, Stephan ADAM, Volker WULFMEYER**

12 *Institute of Physics and Meteorology*

13 *University of Hohenheim, Stuttgart, Germany*

14 *\*Current affiliation: Micrometeorology Group*

15 *University of Bayreuth, Bayreuth, Germany*

16  
17  
18  
19 Submitted: November 8, 2019

20 Revised: March 6, 2020

21 Revised: April 20, 2020

22 Revised: June 1, 2020

23 Accepted: June 2, 2020

24  
25  
26  
27  
28  
29  
30 -----  
31 1) Corresponding author: Rohith Thundathil, Institute of Physics and Meteorology,  
32 University of Hohenheim, Garbenstrasse 30, Stuttgart 70599, Germany.  
33 Email: rohith.thundathil@uni-hohenheim.de  
34 Tel: +49-711-459-22131  
35

## Abstract

36

37

38 The impact of assimilating thermodynamic profiles measured with lidars into the Weather  
39 Research and Forecasting (WRF)-Noah-Multiparameterization model system on a  
40 2.5-km convection-permitting scale was investigated. We implemented a new forward  
41 operator for direct assimilation of the water vapor mixing ratio (WVMR). Data from two  
42 lidar systems of the University of Hohenheim were used: the water vapor differential  
43 absorption lidar (UHOH WVDIAL) and the temperature rotational Raman lidar (UHOH  
44 TRL). Six experiments were conducted with 1-hour assimilation cycles over a 10-hour  
45 period by applying a 3DVAR rapid update cycle (RUC): 1) no data assimilation 2)  
46 assimilation of conventional observations (control run), 3) lidar-temperature added, 4)  
47 lidar-moisture added with relative humidity (RH) operator, 5) same as 4) but with the  
48 WVMR operator, 6) both lidar-temperature and moisture profiles assimilated (impact  
49 run). The root-mean-square-error (RMSE) of the temperature with respect to the lidar  
50 observations was reduced from 1.1 K in the control run to 0.4 K in the lidar-temperature  
51 assimilation run. The RMSE of the WVMR with respect to the lidar observations was  
52 reduced from 0.87 g kg<sup>-1</sup> in the control run to 0.53 g kg<sup>-1</sup> in the lidar-moisture  
53 assimilation run with the WVMR operator, while no improvement was found with the RH  
54 operator; it was reduced further to 0.51 g kg<sup>-1</sup> in the impact run. However, the RMSE of  
55 the temperature in the impact run did not show further improvement. Compared to

56 independent radiosonde measurements, the temperature assimilation showed a slight  
57 improvement of 0.71 K in the RMSE to 0.63 K, while there was no conclusive  
58 improvement in the moisture impact. The correlation between the temperature and  
59 WVMR variables in the static-background error-covariance matrix affected the  
60 improvement in the analysis of both fields simultaneously. In the future, we expect better  
61 results with a flow-dependent error covariance matrix. In any case, the initial attempt to  
62 develop an exclusive thermodynamic lidar operator gave promising results for  
63 assimilating humidity observations directly into the WRF data assimilation system.

64

65 **Keywords** data assimilation; numerical weather prediction; water vapour; temperature;

66 lidar

67

## 68 **1. Introduction**

69           The vertical and horizontal distribution of water vapor and temperature in the  
70 atmosphere is crucial for the evolution of weather on all spatial and temporal scales.  
71 Detailed observations are important for improving the initial fields for numerical weather  
72 predication (NWP) from nowcasting to the very short-range, the short-range, and the  
73 medium range. However, our present representation of land–atmosphere (L–A) interaction  
74 and convection initiation (CI) suffers in mesoscale models largely from huge observational  
75 gaps, consequently also limiting the predictive skill of NWP. Therefore, it is essential to  
76 enhance these observations and to investigate the impact of new remote sensing systems  
77 which are capable of measuring water vapor and temperature profiles into NWP models by  
78 means of data assimilation (DA).

79           Small-scale variations in moisture due to collision of boundaries (Kingsmill 1995),  
80 horizontal convective rolls and mesocyclones (Weckwerth et al. 1996; Murphey et al. 2006),  
81 and intersections between boundaries and horizontal convective rolls (Dailey and Fovell  
82 1999) influences the location and timing of CI. The amount of moisture and variations in the  
83 vertical gradients of moisture and temperature at lower levels of the atmosphere can  
84 change the strength of CI significantly (Lee et al. 1991; Crook 1996). Several field  
85 campaigns have been conducted to understand the relationship between the  
86 three-dimensional thermodynamic fields and CI as well as the impact of assimilation of

87 thermodynamic profiles. These have included the Mesoscale Alpine Program 1990  
88 (Richard et al. 2007); the International H<sub>2</sub>O Project (IHOP) 2002 (Weckwerth and Parsons  
89 2006); the Convection Storm Initiation Project conducted in the summer period of 2004 and  
90 2005 (Browning et al. 2007) and which provided sufficient data for impact studies using the  
91 Met Office unified model (Dixon et al. 2009); the Lindenberg Campaign for Assessment of  
92 Humidity and Cloud Profiling Systems and its Impact on High-Resolution Modeling  
93 (LAUNCH, Engelbart and Haas (2006) in the late summer of 2005; the Convective and  
94 Orographically-induced Precipitation Study (COPS) 2007 (Wulfmeyer et al. 2011); and the  
95 Plains Elevated Convection At Night (Geerts et al. 2017) campaign in summer 2015.

96         Recently, studies of land–atmosphere (L–A) feedback have also become the focus  
97 of improving the quality of weather forecast models as it was realized that a realistic  
98 representation of L–A interaction in mesoscale models is crucial for an accurate prediction  
99 of the pre-convective, dynamic, and thermodynamic environments. The first extensive  
100 study was the Land Atmosphere Feedback Experiment (Wulfmeyer et al. 2018) conducted  
101 in August 2017, which also provided a large data set for the assimilation of thermodynamic  
102 profiles measured with lidar in mesoscale models. The importance and sensitivity of L–A  
103 feedback for the simulation and prediction of the formation and organization of clouds and  
104 precipitation was exemplified in Santanello et al. (2018).

105         At the major forecast centers, there are mainly three DA approaches which are  
106 currently used: (1) variational techniques like 3DVAR and 4DVAR (Courtier 1998; Barker et

107 al. 2004; Huang et al. 2009); (2) ensemble-based approaches which include flavors of the  
108 ensemble Kalman filter (Evensen 2003), and (3) hybrid combinations of these (Ingleby et al.  
109 2013). In 3DVAR, the data is assimilated at specific analysis time-steps, whereas in 4DVAR  
110 there is an adjoint model so that the cost function is minimized over a time period and not at  
111 a particular time-step. The drawback of the 3DVAR is the static nature of the background  
112 error covariance ( $B$ ) matrix in the cost function. This prevents the model from incorporating  
113 the present dynamics of the atmosphere. Although 4DVAR implicitly incorporates a  
114 time-evolving background error covariance model (Lorenc 2003), the same static matrix,  $B$ ,  
115 is propagated implicitly to a later time-step. However, the 4DVAR is superior to the 3DVAR  
116 scheme due to the evolution of the background error covariance matrix and the reduction of  
117 the model imbalance at the analysis time. Meteo-France uses the incremental 3DVAR in  
118 the Aire Limitée Adaptation dynamique Développement InterNational (ALADIN) model  
119 (Brousseau et al. 2011; Berre 2000); the German Weather Service (DWD) and MeteoSwiss  
120 uses the Local Ensemble Transform Kalman Filter (LETKF) DA in the Consortium for  
121 Small-scale Modelling (COSMO) model (Schraff et al. 2016); the UK Met Office has  
122 implemented incremental 3DVAR and 4DVAR (Ingleby et al. 2013); NOAA's National  
123 Centers for Environmental Prediction uses incremental hybrid 3D $En$ Var and non-variational  
124 cloud analysis (Wu et al. 2017; Hu et al. 2006; Benjamin et al. 2004, 2016; Hu et al. 2017);  
125 and the Japan Meteorological Agency (JMA) applies incremental 4DVAR and 3DVAR  
126 (Honda et al. 2006; Aranami et al. 2015). A recent discussion of the DA methods used in

127 various forecast centers is given by Gustafsson et al. (2018). All of these DA techniques are  
128 capable of assimilating profiles of the thermodynamics and dynamics of the atmosphere.

129         Radiosonde and aircraft measurements are the only conventional data observation  
130 sources currently providing water vapor and temperature data within the planetary  
131 boundary layer (PBL) and lower troposphere. Radiosondes provide a vertical  
132 thermodynamic profile of the atmosphere from the surface layer through the lower  
133 troposphere whereas weather stations provide only surface measurements with limited  
134 impact on the vertical thermodynamic structure. Radiosondes provide instantaneous data  
135 only at the time of ascent, giving more or less a snapshot of the atmosphere along their  
136 vertical track. Therefore, the soundings suffer from significant sampling errors, especially in  
137 the boundary layer with its highly turbulent fluctuations (Weckwerth et al. 1999). The  
138 coverage of the radiosonde network is quite coarse, and the number of radiosonde stations  
139 is decreasing rather than increasing in most countries due to their high cost of operation.

140         Another option is the application of passive and active remote sensing data.  
141 Wulfmeyer et al. (2015) gave a comprehensive overview of the current observational  
142 capabilities of remote sensing techniques with respect to thermodynamic fields in the lower  
143 troposphere. It was demonstrated that using space-borne passive remote sensing systems  
144 for thermodynamic observations does not provide the necessary vertical resolution in the  
145 lower troposphere to recover its vertical structure. Ground-based passive remote sensing  
146 instruments like microwave radiometers produce reliable data but have a coarse resolution



147 of around 300 m to 1000 m in the lower 2000 m above the ground (Blumberg et al. 2015;  
148 Cadeddu et al. 2002; Wulfmeyer et al. 2015). IR spectrometers have higher vertical  
149 resolutions due to having more spectroscopic lines which can be evaluated; however, their  
150 vertical resolution is still limited to 100 m to 800 m up to 2000 m above ground level (Turner  
151 and Löhnert, 2014). Convection-permitting models have vertical resolutions in the range of  
152 100 m or less within the boundary layer, where fine-scale processes are crucial, in order to  
153 recover the thermodynamic structure of the atmosphere. Therefore the observation  
154 systems must fulfill the data requirements of convective-scale DA models to ensure higher  
155 representativeness (Wulfmeyer et al. 2015). Therefore, microwave radiometers and IR  
156 spectrometers are not capable of resolving the vertical structure of the lower troposphere,  
157 including the top of the PBL, the inversion strength at the PBL top, or the elevated inversion  
158 layers and the moisture structure in the free lower troposphere. However, this capability is  
159 expected to be crucial to achieving an improved prediction of L–A feedback and CI. Typical  
160 temporal resolutions of passive remote sensing instruments are 5–10 minutes, but further  
161 processing time is required either for the inversion of the spectra to vertical water vapor and  
162 temperature information or for the assimilation of the spectra through a forward operator in  
163 a DA system.

164 Active remote sensing techniques offer high temporal and spatial resolution data  
165 simultaneously to accurately capture the atmospheric fields without much loss of  
166 temperature and moisture gradient information. Two main techniques for humidity profiling

167 are available: water vapor differential absorption lidar (WVDIAL) and water vapor Raman  
168 lidar (WVRL). Both systems achieve a high vertical and temporal resolution during both  
169 day- and night-time (Lange et al. 2018; Späth et al. 2018). Whereas WVDIAL does not  
170 require calibration (Ismail and Browell 1989; Bösenberg 1998), it has been demonstrated  
171 that, for WVRL, the calibration has long-term stability, and a high accuracy can be  
172 maintained for the measurements. Ground-based WVDIAL has been implemented for  
173 tropospheric measurements at various centers. Depending on the efficiency of the receiver  
174 and the average power of the laser transmitter, the combination of temporal and spatial  
175 resolution ranges from 1 s, 15 m (Metzendorf 2019) to 5 min, 300 m (Spuler et al. 2015).  
176 The NCAR and Montana State University have developed a compact, field-deployable  
177 micro-pulse DIAL (Spuler et al. 2015; Weckwerth et al. 2016) with a range resolution of 300  
178 m and a temporal resolution of 1–5 min. The vertically pointing WVDIAL of the Institute of  
179 Physics and Meteorology (IPM, Wagner et al. 2011, 2013; Metzendorf 2019) has a range  
180 resolution of 15–300 m and temporal resolution of 1–10 s. The first WVDIAL with a 3-D  
181 scanner was also developed at the IPM of the University of Hohenheim (UHOH, Behrendt  
182 et al., 2009; Späth et al., 2014). Typical accuracies of the absolute humidity for the IPM's  
183 WVDIAL are in the range of 5–10% within the PBL during the daytime. WVRLs have been  
184 making continuous measurements at various centers, such as the operational WVRL  
185 (Goldsmith et al. 1998; Turner and Goldsmith 1999) at the Atmospheric Radiation  
186 Measurements Southern Great Plains site in the U.S; the Raman Lidar for Meteorological

187 Observations ( RALMO, Dinoev et al. 2013; Brocard et al. 2013) in Payerne, Switzerland  
188 used by MeteoSwiss; the Raman Lidar for Atmospheric Moisture Sensing (RAMSES,  
189 Reichardt et al. 2012) in Lindenberg, Germany, used by the German Meteorological Service  
190 (DWD); and the WVRL at the Cabauw Experimental Site for Atmospheric Research  
191 ( CESAR, Apituley et al. 2009) in the Netherlands. Typical resolutions of WVDIALs are  
192 around 150 m for the spatial resolution and 10 s for the temporal resolution, with an  
193 accuracy of < 5%.

194 For temperature profiling in the lower troposphere, the temperature rotational  
195 Raman lidar (TRL) technique demonstrated the best performance (Behrendt et al. 2004; Di  
196 Girolamo et al. 2004; Arshinov et al. 2005; Radlach et al. 2008). It is now possible to  
197 measure temperature profiles from close to the surface to the lower troposphere with a  
198 temporal resolution of a few minutes and a vertical resolution of approximately 100 m. This  
199 performance permits the detection of inversion layers and the characterization of the  
200 temperature gradient with a high degree of accuracy (Hammann et al. 2015). Continuous  
201 time–height cross-sections of the atmospheric thermodynamic profile are a unique feature  
202 of these lidar systems which enables promising research and applications in the direction of  
203 mesoscale DA. Therefore, WVDIAL, WVRL, and TRL are suitable and ready for application  
204 in DA impact studies.

205 The subject of this work is the analysis of the impact of two relatively new lidar  
206 systems used for water vapor and temperature profiling in mesoscale DA. The two active

207 remote sensing system are the high-power, high-efficiency, 3D scanning WVDIAL which  
208 has an extraordinary resolution, accuracy, and range (Wagner et al. 2013; Späth et al. 2016,  
209 2014) and the TRL for daytime and night-time temperature profiling (Radlach et al. 2008;  
210 Hammann et al. 2015; Behrendt et al. 2015; Lange et al. 2018), both developed and  
211 operated at the IPM in Stuttgart, Germany.

212 The experimental setup was based on the Weather Research  
213 Forecasting-Noah-Multiparameterization (WRF-Noah-MP) model system and the WRF DA  
214 (WRFDA) system using a 3DVAR rapid update cycle (RUC). This RUC was developed and  
215 optimized for Europe (Schwitalla and Wulfmeyer 2014) and is operated on the  
216 convective-permitting scale. Previously, the water vapor mixing ratio (WVMR) or other  
217 water vapor variables were assimilated by applying the radiosonde relative humidity (RH)  
218 operator. It is obvious that this is not the optimal approach because the RH is strongly  
219 sensitive to temperature. Therefore, we developed a new forward operator for the  
220 assimilation of absolute humidity, mixing ratio or specific humidity independent of any  
221 cross-sensitivity to temperature. This forward operator was based on an already-existing  
222 atmospheric infrared sounding retrieval (AIRSRET) observation operator in the WRFDA  
223 system. We expected that this new operator would provide a strong and direct impact. The  
224 first key objective of this work was to quantify this impact.

225 So far, there have been only a few impact studies using thermodynamic lidar data.  
226 During IHOP 2002, Wulfmeyer et al. (2006) assimilated airborne water vapor DIAL data

227 from the NASA LASE system into the 5<sup>th</sup> generation Pennsylvania State University-NCAR  
228 Mesoscale Model (MM5), which was based on a 4DVAR DA system. The results from the  
229 assimilation resulted in a considerably improved prediction of CI due to strong and positive  
230 analysis increments, not only with respect to water vapor but also to dynamics. During  
231 LAUNCH, Grzeschik et al. (2008) assimilated water vapor data from a triangle of three  
232 WVRLs, again into the MM5. The initial water vapor field was corrected by about 1 g kg<sup>-1</sup>  
233 and the WVRL impact on the water vapor field continued for up to 12 h in the forecast  
234 model. Airborne water vapor data from the Water Vapour Lidar Experiment in Space  
235 demonstrator was assimilated into the ECMWF 4DVAR global model by Harnisch et al.  
236 (2011). The analysis error was reduced after the assimilation of WVDIAL observations.  
237 COPS (Wulfmeyer et al. 2011) had two airborne lidars which measured lower tropospheric  
238 water vapor fields: these were assimilated into the 3DVAR assimilation system of the  
239 Application of Research to Operations at Mesoscale (AROME) numerical weather  
240 prediction model (Bielli et al. 2012). Temperature data from TRL were assimilated into the  
241 WRF model by Adam et al. (2016), which produced positive results. Also recently, as  
242 described in Yoshida et al. (2020), water vapor profiles from Raman lidar were assimilated  
243 using the LETKF system to investigate the effects on precipitation forecasts. All of these  
244 results confirm the positive impact of thermodynamic lidar DA on NWP models. The first  
245 study where WV and T profiles from active remote sensing measurements were assimilated  
246 simultaneously into a forecast system will be presented here.

247 For this purpose, we investigated the impact of assimilating high-resolution  
248 temperature profiles from the UHOH TRL and water vapor profiles from the UHOH WVDIAL  
249 into our version of the WRFDA model using a 3DVAR RUC.

250 This work describes how well the new forward operator can assimilate WVMR and  
251 temperature data from the lidar instruments and focuses on the following questions:

- 252 - Does the new operator work and have a reasonable impact on the analysis of the  
253 WV field?
- 254 - What is the impact of WV DA alone, the impact of T DA alone, and the combined  
255 impact?
- 256 - How large is the inter-dependency of the WVMR and temperature variables in the  
257 DA system?

258 The manuscript is arranged as follows. Section 2 gives a brief overview about the HOPE  
259 campaign. Section 3 describes the WRFDA system, the configuration of the RUC applied in  
260 our study, as well as the new water vapor operator. The lidar observations are shown at the  
261 end of section 3 together with a brief description of their principles. Section 4 describes the  
262 results of the impact study with respect to temperature and moisture. The manuscript  
263 finishes with a summary of our results and an outlook.

264

## 265 **2 Observations**

### 266 **2.1 The HOPE measurement campaign**

267           The High Definition Clouds and Precipitation for advancing Climate Prediction  
268 HD(CP)<sup>2</sup> project aimed at improving the representation of clouds and precipitation in  
269 atmospheric models. By resolving clouds and precipitation processes, the uncertainty in  
270 climate change predictions can be significantly reduced (Stevens and Bony (2013); see  
271 <http://www.hdcp2.eu> for more information). The project was initiated by the German Federal  
272 Ministry of Education and Research in coordination with the German Meteorological  
273 Service (DWD) in October 2012. In order to evaluate the performance of models, the  
274 HD(CP)<sup>2</sup> Observation Prototype Experiment (HOPE) campaign (Macke et al. 2017) was  
275 conducted to provide high-resolution observations. The HOPE campaign focused on  
276 multi-sensor synergy within a micro- to mesoscale domain. The campaign took place in  
277 north-western Germany around the Jülich Research Centre during April and May 2013. The  
278 HOPE field campaign was conducted mainly at three supersites, which covered an  
279 approximately 10-km radius around the Jülich Research Centre. The supersites were  
280 designed in such a way to derive data concerning moisture, temperature, and wind at a  
281 resolution of 100 m for a volume of around 10 km ×10 km × 10 km. The three supersites  
282 used, where the main remote sensing facilities were deployed, were Jülich (JUE),  
283 Krauthausen (KRA), and Hambach (HAM). The IPM lidar systems were deployed at the  
284 Hambach site, where radiosondes were also launched during intensive observation periods  
285 (IOPs). The radiosonde type used during the IOPs was the DFM-09 model from GRAW  
286 (<https://www.graw.de/products/radiosondes/dfm-09/>). The WVDIAL (Späth et al. 2016) and

287 the TRL (Hammann et al. 2015) from UHOH were positioned at 50°53'50.55" N,  
 288 6°27'50.27" E and 110 m above sea level (Fig. 1). The IPM lidar systems were designed to  
 289 observe the three-dimensional thermodynamic temperature and moisture fields along with  
 290 their turbulent fluctuations (Muppa et al. 2016; Behrendt et al. 2015; Wulfmeyer et al. 2016).

## 291 **2.2 UHOH WVDIAL**

292 In the DIAL technique, two laser signals are used, namely  $P_{on}$  and  $P_{off}$ , the online  
 293 and offline signals, respectively. The wavelength of the  $P_{on}$  signal is tuned in such a way  
 294 that there is a strong absorption of water vapor in the atmospheric signal resulting in a  
 295 reduction in the backscatter, whereas the  $P_{off}$  signal wavelength is tuned for weak  
 296 absorption. The number density of the water vapor molecules is derived from the differential  
 297 absorption of the online and offline signals (Schotland, 1966):

$$N_{WV}(r) = \frac{1}{2(\sigma_{on}(r) - \sigma_{off}(r))} \frac{d}{dr} \ln \left( \frac{P_{off}(r) - P_{B,off}}{P_{on}(r) - P_{B,on}} \right) \quad (1)$$

298 where  $N_{WV}$  is the water vapor number density,  $\sigma$  denotes the absorption cross section,  
 299  $P_B$  is the background signal, and the argument  $r$  is the distance measured from the lidar  
 300 system to the scattering volume along the line of sight of the laser beam. Further details of  
 301 the UHOH WVDIAL can be found in Wagner et al. (2013) and Späth et al. (2016).

302 The data acquisition system had a sampling rate of 10 MHz, which allowed the  
 303 atmospheric backscatter signals to be recorded with a fine vertical resolution of 15 m. The  
 304 data were recorded for each laser shot and averaged over a period of 1 s to 10 s. The raw



305 data used for the present study had a temporal resolution of 10 s. In Eq. (1), the derivative  
306 with respect to the range is derived by the Savitsky–Golay (SaGo) algorithm (Savitzky and  
307 Golay 1964). The window length in the SaGo algorithm was set to 135 m up to a height of  
308 1500 m above ground level based on a consideration of the average height of the PBL.  
309 Between 1500 m and 3000 m, a window length of 285 m was applied since the  
310 signal-to-noise-ratio (SNR) of the signals decreased due to a reduction in the signal  
311 strength and differential optical thickness.

312 Time windows of  $\pm 10$  minutes around the assimilation time step were chosen. A  
313 total of 120 lidar profiles from the high-resolution absolute humidity data (Fig. 2) which fall  
314 into these 20-minute windows were averaged for input at each assimilation time-step. The  
315 absolute humidity data and the corresponding error derived from the number density were  
316 then converted to WVMR data with associated errors. We ensured that the input data for  
317 the assimilation had a resolution roughly similar to that of the model. Hence the WVMR  
318 data, which was in 15-m steps, was fed into the assimilation data in 30-m steps. The  
319 WVDIAL error for the resolutions that were used ranged from  $0.01 \text{ g kg}^{-1}$  at a height of 400  
320 m to a maximum of  $1 \text{ g kg}^{-1}$  at heights above 2 km (Späth et al. 2014).

### 321 **2.3 UHOH TRL**

322 The UHOH TRL measures atmospheric temperature profiles through the rotational  
323 Raman technique (Cooney 1972; Behrendt and Reichardt 2000; Behrendt et al. 2004). This  
324 method relies on the temperature-dependent inelastic scattering of UV laser pulses when

325 collided with, Nitrogen and Oxygen molecules, the major gaseous constituents of the  
326 atmosphere.

327 The rotational Raman spectrum of air consists of two parts, the Stokes and the  
328 anti-Stokes branches. The Stokes branch is found at wavelengths greater than that of the  
329 incident radiation while the anti-Stokes branch is found at shorter wavelengths. The UHOH  
330 TRL extracts only signals of the latter. The temperature is determined using the ratio  $Q$  of  
331 the two background-corrected Raman signals  $RR2$  and  $RR1$ .  $P_{RR2}$  and  $P_{RR1}$  are the  
332 signals for low and high quantum-number transition settings of the filter, respectively, so  
333 that

$$Q(r) = \frac{P_{RR2}(r)}{P_{RR1}(r)} \quad (2)$$

334 The temperature profile of the atmosphere  $T(r)$  is obtained from

$$T(r) = \frac{b}{a - \ln(Q(r))} \quad (3)$$

335 where  $a$  and  $b$  are calibration constants. The statistical error in the temperature  
336 measurements are derived from Poisson statistics applied to the signal intensities of the  
337 photon-counting data. For a signal count number  $s$ ,  $\sigma$  denoting the standard deviation,  $1\sigma$   
338 statistical error is given by the square root of  $s$ . The error characteristics are detailed in  
339 Behrendt et al. (2015), Behrendt and Reichardt, (2000), and Wulfmeyer et al. (2015, 2016).  
340 The temperature profiles are also averaged over a time window of 20 minutes at each  
341 assimilation time-step before assimilation into the model. The vertical profile from the TRL  
342 was smoothed with a running-average window of 108.75 m and then thinned to one value

343 of 3.75 m. The error range of the profiles was from 0.1 K at 500 m to 1.1 K at 3000 m  
344 (Hammann et al. 2015). Figure 3 shows the time series data prior to further temporal  
345 averaging over 20 minutes. The averaged data were then used for assimilation.

## 346 **2.4 Conventional Observations**

347 The DA system was augmented by a dense network of surface reports, SYNOP  
348 and METAR, over Europe. A set of radiosonde (RS) measurements, TEMP, provided a  
349 snapshot of the thermodynamic structure of the atmosphere from the point of launch. A set  
350 of wind profilers (PROFL) provided wind measurements along with the wind data provided  
351 along with the radiosonde products. Aircraft measurements (AMDAR) were also  
352 assimilated as part of the conventional observations. All of these observations were  
353 obtained from the Global Telecommunication System data archive of the WMO, which are  
354 stored at the ECMWF. Satellite Atmospheric Motion Vectors (AMVs) above 700 hPa from  
355 the Meteosat Second Generation satellite were also included in the assimilation dataset.  
356 The AMVs data below 700 hPa were discarded since the data retrieval algorithm is not  
357 reliable (Horváth et al. 2017). Apart from these observations, global navigation satellite  
358 systems-zenith total delay (GNSS-ZTD) data were used in the DA system for improving the  
359 accuracy for humidity distributions over the domain. These data were obtained from the  
360 E-GVAP network (<http://egvap.dmi.dk/>). Table 1 shows a summary of the already large  
361 number of observations assimilated into the DA system within the conventional DA run,  
362 which meant that it was quite a challenge for the lidar data to achieve any additional impact.

363 Figure 4 depicts the conventional observations assimilated into the model for 09 UTC: this  
364 was roughly the same for all the subsequent assimilation cycles.

365

### 366 **3. Model setup**

#### 367 **3.1 WRF model and configuration**

368 The WRF model (Skamarock et al. 2008), version 3.8.1, was used for the impact  
369 study presented here. The WRF model has been applied for research at various  
370 characteristic spatial scales like the synoptic-scale, mesoscale, and large eddy simulation  
371 (LES) scale (Talbot et al. 2012; Wei et al. 2017; Muppa et al. 2018; Schwitalla et al. 2017).  
372 Furthermore, the WRF model is extensively used for operational forecasting in various  
373 weather forecasting centers across the world (Powers et al. 2017). The WRF has two  
374 dynamical solvers – the Advanced Research WRF (ARW) core (Skamarock et al. 2008)  
375 and the Nonhydrostatic Mesoscale Model core (Janjic 2003). The former was applied in our  
376 study.

377 Compressible and nonhydrostatic Euler equations are integrated in the ARW  
378 dynamic solver. The prognostic variables in the model are the velocity components  $\mathbf{u}$  and  
379  $\mathbf{v}$  in Cartesian coordinates and  $\mathbf{w}$  in the vertical coordinate, the perturbation potential  
380 temperature  $\theta$ , the perturbation geopotential  $\varphi$ , and the perturbation surface pressure  $p_s$ .  
381 The WVMR  $q_v$  is also a prognostic variable in the ARW solver.

382 The model was configured with a spatial resolution of 2.5 km and 856 × 832 grid cells (Fig.  
383 1). The vertical resolution of the model was set to 100 levels up to 50 hPa with 27 levels  
384 within the PBL. Compared to the study of Adam et al., (2016), the number of vertical levels  
385 in the model was increased from 57 to 100 in order to even better resolve gradients. The  
386 model time step for the simulation was set to 15 s. All simulations were initialized using  
387 European Centre for Medium Range Weather Forecasts (ECMWF) analysis with a spatial  
388 resolution of 0.125° (approximately 13.5 km). Also the Operational Sea Surface  
389 Temperature and Sea Ice Analysis (OSTIA; Donlon et al., 2012) data provided by the Met  
390 Office were applied to accurately initialize the sea surface temperatures.

391 The WRF model physics configuration used for the simulations is summarized in  
392 Table 2. The physics configuration used for the study was based on previous research and  
393 DA efforts (Adam et al. 2016; Schwitalla and Wulfmeyer 2014; Bauer et al. 2015; Schwitalla  
394 et al. 2011). The WRF was coupled with the Noah–MP Land Surface Model (Niu et al. 2011;  
395 Yang et al. 2011) which includes a canopy layer, three layers of snow, and four layers of soil.  
396 The skin temperature of the canopy and snow or soil surface are predicted by an interactive  
397 energy balance method. Shortwave and longwave radiation are parameterized with the  
398 RRTMG scheme (Iacono et al. 2008). Microphysical properties are represented by the  
399 Thompson double-moment scheme (Thompson et al. 2008), which explicitly predicts mixing  
400 ratios of cloud water, rain, cloud ice, snow, and graupel. The Mellor–Yamada Nakanishi  
401 Niino (MYNN; Nakanishi and Niino (2006) Level-2.5 scheme (Nakanishi and Niino 2009)

402 was used as the PBL scheme. A new formulation of the turbulent length scales and  
403 parameterization of the pressure covariance as well as parameterization of the stability  
404 functions of third-order turbulent fluxes were incorporated in this MYNN scheme.

405 Deep-convection parameterization was not used in the study since we were  
406 running the model at the convection-permitting scale (Weisman et al. 2008). For shallow  
407 cumulus parameterization, the Global/Regional Integrated Model System Scheme (Hong et  
408 al. 2013) was used.

### 409 **3.2 Data assimilation system**

410 The WRFDA system incorporates a number of DA techniques which can be broadly  
411 classified as being based on the deterministic approach or the probabilistic approach.  
412 Deterministic approaches include the variational DA systems like the 3DVAR and 4DVAR.  
413 In this study, we applied the 3DVAR DA system in a RUC mode with an hourly update cycle.  
414 The code of the RUC is completely automated from the pre-processing stage to  
415 post-processing of the analysis and is designed for variable assimilation time windows. The  
416 WRFDA 3DVAR system is based upon the principle of iteratively minimizing the cost  
417 function  $J(\mathbf{x})$ , whose independent variable or the control variable is the analysis state  
418 vector  $\mathbf{x}$ . The equation of the cost function for 3DVAR reads

$$J(\mathbf{x}) = \frac{1}{2}(\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1}(\mathbf{x} - \mathbf{x}_b) + \frac{1}{2}(\mathbf{y} - \mathbf{H}(\mathbf{x}))^T \mathbf{R}^{-1}(\mathbf{y} - \mathbf{H}(\mathbf{x})) \quad (4)$$

419 The cost function  $J(\mathbf{x})$  consists of two terms, a background and an observation  
420 term. The vector fields  $\mathbf{x}$ ,  $\mathbf{x}_b$  and  $\mathbf{y}$  are the analysis state, the background or the first

421 guess, and the observation state vectors, respectively.  $\mathbf{H}$  is the forward operator, which  
422 maps the analysis state vector space to the observation vector space. For instance, a  
423 corresponding operator is required for the DA of WVMR profiles, but this did not exist at the  
424 time this project started.

425         Apart from the general column vectors, there are two square matrices which play a  
426 major role in the cost function minimization: the background error covariance matrix  $\mathbf{B}$  and  
427 the observation error covariance matrix  $\mathbf{R}$ . In the DA system,  $\mathbf{R}$  is a diagonal matrix since  
428 we assume that there is no correlation among the observation errors between different  
429 instruments or height levels.  $\mathbf{B}$  is a square, positive, semi-definite and symmetric matrix  
430 whose eigenvalues are positive.  $\mathbf{B}$  consists of the variances of the background forecast  
431 errors as the diagonal elements, and the covariance between them as the symmetric upper  
432 and lower triangular elements. The variances and covariances of  $\mathbf{B}$  strongly contribute to  
433 the response of an analysis after an observation has been assimilated. The ratio of these  
434 values to the RMS errors of  $\mathbf{R}$  determine the impact on the analysis. Hence an appropriate  
435 determination of  $\mathbf{B}$  is crucial in a variational DA system.

436          $\mathbf{B}$  can be calculated mainly by three methods, namely, the NMC method (Parrish  
437 and Derber, 1992), the analysis ensemble method (Fisher, 2003), and by using innovation  
438 statistics (Hollingsworth and Lönnberg, 1986). All these methods have their own merits  
439 (and drawbacks). The NMC method, in which climatological background error covariances  
440 are estimated, is the most widely used method for the generation of  $\mathbf{B}$ . We used the NMC

441 method in our study since it provides physically reasonable results in regional model  
442 domains and is computationally less expensive than the ensemble method. In the NMC  
443 method, forecast difference statistics are computed, from which the forecast error  
444 covariance is then derived. The forecast error covariance is specifically derived for the  
445 domain in order to incorporate the errors applicable to that domain. However, the NMC  
446 method has certain drawbacks: it overestimates the covariances in large-scale simulations  
447 and poorly observed regions (Berre 2000; Fischer 2013; Berre et al. 2006). The statistics  
448 were derived for a period of a month from forecast differences of 24 hours and 12 hours  
449 since we were performing a regional simulation. The month of April 2013 was selected to  
450 derive the statistics. We used the CV6 option for implementing multivariate background  
451 error statistics in the  $B$  matrix. In the CV6 option, the moisture analysis is multivariate,  
452 which means that moisture increments are derived from temperature and wind increments  
453 and vice-versa.

### 454 **3.3 WVMR forward operator**

455 To assimilate the WVMR directly, a new forward operator had to be developed and  
456 incorporated in the WRFDA. This new forward operator allowed WVMR data to be used  
457 directly without converting it to RH, for which temperature data is also needed. Until now,  
458 the WRFDA system has ingested humidity data in the form of RH through the conventional  
459 radiosonde operator. Previously, all the vertical profile data products from radiosondes,



460 ground-based microwave radiometers, and other humidity profiling instruments have used  
 461 the radiosonde operator for the assimilation of humidity in the form of RH (Bielli et al. 2012).

462 The advantage of expressing moisture in the form of the WVMR is that the variable  
 463 is a tracer and remains insensitive if there are changes in the atmospheric temperature or  
 464 pressure fields. Consequently, the maximum information content of the observation is used  
 465 with respect to the WV budget in the area of interest and unnecessary cross-sensitivities  
 466 are avoided.

467 When the RH operator in the WRFDA is used for assimilating mixing ratio  
 468 measurements  $m$ , the following relationship is used:

$$\begin{aligned}
 RH &= \frac{m R_w}{1 + m R_L} \frac{p}{E(T) \left[ 1 + \frac{m R_w - R_L}{1 + m R_L} \right]} \\
 &\cong m \frac{R_w}{R_L} \frac{p}{E(T) \left[ 1 + m \frac{R_w - R_L}{R_L} \right]} = 1.607 m \frac{p}{E(T) [1 + 0.607 m]} \\
 &\cong 1.607 m \frac{p}{E(T)} \tag{5}
 \end{aligned}$$

469 Here,  $T$  is the ambient temperature in units of  $K$  and  $p$  is the total atmospheric pressure  
 470 exerted by moist and dry air in units of  $Pa$ .  $R_w$  and  $R_L$  are the specific gas constants of  
 471 water vapor and dry air, respectively, in units of  $Jkg^{-1}K^{-1}$ . This relationship confirms that it  
 472 is not the best idea to assimilate the WVMR using an RH operator because the sensitivity to  
 473 temperature in the equation for the water vapor saturation pressure  $E(T)$  (Bolton 1980),

$$E(T) = 611.2 \exp \left[ 17.67 \left( \frac{T - 273.15}{T - 273.15 + 243.5} \right) \right], \tag{6}$$

474 is comparable with the sensitivity to  $m$  and thus not negligible. This can be proved by  
 475 deriving the total derivative of  $RH$  with respect to the variables  $m$ ,  $p$ , and  $T$ . Starting from  
 476 the total derivative of Eq. 5 with reference to Eq. 6, we finally get the expression for  $\delta RH$   
 477 as

$$\delta RH = RH \left[ \frac{\delta m}{m} + \frac{\delta p}{p} - \left( \frac{(17.67) \cdot (243.5)}{(T - 29.65)^2} \right) \delta T \right] \quad (7)$$

478 Considering the absolute values of the terms within the square brackets in Eq. 7, the third  
 479 term  $\left( \frac{(17.67) \cdot (243.5)}{(T - 29.65)^2} \right) \delta T$  is comparable with the first term  $\frac{\delta m}{m}$ . The second term  $\frac{\delta p}{p}$  is very  
 480 small compared to the other two terms. Please refer to the appendix section for a quantified  
 481 analysis. From Eq. 7, we infer that the value of  $RH$  is dependent on  $T$  and  $m$ .

482 Therefore, a new operator that focuses on increased analysis of the WVMR field  
 483 was implemented in the WRFDA in this study. In the case of the measurement of WVMR,  
 484 the conversion is trivial because this is the prognostic variable used in the WRFDA. It  
 485 should be noted that, in contrast to the WVRL, the WVDIAL measures absolute humidity  
 486 and not the WVMR as the primary product. However, the conversion of absolute humidity to  
 487 WVMR is not as critically sensitive to temperature as the conversion to RH is.

488 When the absolute humidity  $\rho_{wv}$  is measured, the conversion is very simple and  
 489 reads

$$m = \frac{\rho_{wv}}{\rho - \rho_{wv}} \cong \frac{\rho_{wv}}{\frac{p}{R_L T} [1 + 0.607m] - \rho_{wv}} \cong \frac{\rho_{wv}}{\frac{p}{R_L T} - \rho_{wv}} \cong \frac{\rho_{wv} R_L T}{p} \quad (8)$$

490 For the conversion, simply the model temperature and pressure variables are used. The  
 491 WVMR error becomes mainly dependent on the error in the absolute humidity and reads

$$\delta m \cong \frac{R_L T}{p} \delta \rho_w + \frac{\partial m}{\partial T} \delta T + \frac{\partial m}{\partial p} \delta p = \frac{R_L T}{p} \delta \rho_{wv} + \frac{\rho_{wv} R_L}{p} \delta T + \frac{-\rho_{wv} R_L T}{p^2} \delta p$$

$$\cong \frac{R_L T}{p} \delta \rho_{wv}$$
(9)

492 since  $\frac{\rho_{wv} R_L}{p} \delta T \ll \frac{R_L T}{p} \delta \rho_{wv}$  and since  $\frac{\rho_{wv} R_L T}{p^2} \delta p$  is less than the other two terms. Please  
 493 find a numerical example in the appendix.

494 The error in  $m$  was determined with the total error in the absolute humidity data, which is  
 495 the sum of a time-independent systematic error, the noise error, and the representativeness  
 496 error. The systematic error was obtained from previous comparisons with other sensors  
 497 (Bhawar et al. 2011) and the WVDIAL equation error propagation (Wulfmeyer and  
 498 Bösenberg 1998). Due to the self-calibration property of the WVDIAL, the results revealed a  
 499 very low systematic error of approximately 3 %, and so this error could be neglected in the  
 500 DA process. It is one of the big advantages of the WVDIAL methodology that the  
 501 corresponding measurements can be considered as bias-free or very small and unknown,  
 502 and thus used as a reference. Hence we can only consider the statistical uncertainty for DA  
 503 studies. Regarding the bias of the model, we constrained ourselves to the quality control of  
 504 the data input to the model at the time of assimilation by introducing a new variable  
 505 *max\_error\_q\_DIAL*, into the WRF model registry that is described later in this section. The  
 506 model bias greatly depends upon the model physics, which was not modified in this  
 507 research.

508 The noise error can be determined in near-real-time by the determination of the  
509 autocovariance function of the high-resolution absolute humidity time series at each height.  
510 This method is explained in detail in Lenschow et al. (2000) and Wulfmeyer et al. (2016)  
511 and is routinely implemented in the IPM data-processing algorithms. Another advantage of  
512 the temporal resolution of time series data is that it allows an estimate of the  
513 representativeness error to be obtained. If we apply the Taylor hypothesis to the water  
514 vapor time–height cross section measured in a grid box of the model system, the water  
515 vapor variability will be representative for this box for a time period  $\Delta T \approx \frac{\Delta x}{V}$ , where  $\Delta x$  is  
516 the horizontal grid increment of the model and  $V$  is the horizontal wind speed. Using  
517 autocovariance function analysis, it is possible to separate atmospheric variance and noise  
518 variance to produce information about the accuracy of the measurement and the  
519 atmospheric variability. If the autocovariance is taken at lag 0, which is equivalent to  
520 calculating the total variance of the time series, we can take this as an estimate of the total  
521 error consisting of the noise error variance and the variance of the representativeness error  
522 so that we can write

$$\delta\rho_{\text{wv}}(z) \cong \sqrt{\text{var}(\rho_{\text{wv}}(t, z))} \cong \sqrt{(\delta\rho_{\text{wv},\text{noise}}(z))^2 + (\delta\rho_{\text{wv},\text{represent}}(z))^2} \quad (10)$$

523 These error profiles were calculated by averaging temporally over a 20-minute window of  
524  $\pm 10$  minutes around the time-step of the assimilation.

525 The new operator contains a couple of further essential data-processing steps. The  
526 WRFDA system assimilates observations obtained from various instruments. The initial

527 step is the conversion of raw observations from these instruments to the LITTLE R format.  
 528 LITTLE R is an ASCII-based file format and is an intermediate format used by the WRFDA  
 529 to assimilate any number of observation types in a universal manner. The observation  
 530 preprocessor (OBSPROC) of the WRFDA package reads only observations in the LITTLE  
 531 R format. The OBSPROC removes the observations which do not fit in the specified  
 532 temporal and spatial domain. Also it applies a number of other tasks like reordering and  
 533 merging or deleting duplicate data.

534 As a starting point in our efforts toward developing an exclusive forward operator  
 535 for the atmospheric products derived by lidar, an already-existing atmospheric infrared  
 536 sounding retrieval (AIRSRET) or the FM-133 observation operator was used. We tested the  
 537 AIRSRET operator because this operator has temperature and WVMR fields, which are  
 538 basically the lidar end-products, in the model. The AIRSRET operator takes RH and  
 539 temperature data and then converts them to WVMR:

$$m = \frac{RH \cdot E(T)}{1.607 p} \quad \left[ \frac{kg}{kg} \right] \quad (11)$$

540 which is basically Eq. (5). In the new operator, the WRFDA code was modified in such a  
 541 way that the RH field was replaced by the WVMR data field by using Eq. (8). We call this  
 542 new operator the thermodynamic lidar (TDLIDAR) operator.

543 The vertical profiles of the WVMR and temperature fields are linearly interpolated  
 544 from the model levels to the observation data levels according to

$$\rho_{w'} T(l_{in}) = (\rho_{w'} T(l+1) - \rho_{w'} T(l)) \delta z + \rho_{w'} T(l) \quad \left[ \frac{kg}{m^3}, K \right] \quad (12)$$

545 Here  $l$  is the model vertical level and  $l_{in}$  is the observation point within the model  
546 levels  $l + 1$  and  $l$ .  $z$  is the height difference between two model levels.

547 As the total observation error for moisture measurements obtained from lidar is  
548 much lower than that for conventional datasets, a new error factor *max\_error\_q\_DIAL*  
549 was incorporated in the WRFDA registry. This new error factor enables the user to adjust  
550 the size of the error window through which the observations are ingested by the model. The  
551 observations are ingested only if the innovation or the difference between the observation  
552 and the first guess fall within  $m_{err}$  (Eq. 13). The model filters out low-quality WVDIAL  
553 observations that have a significant difference with the first guess of the model. The filtering  
554 is done with the help of this variable. The error factor is a scalar quantity which is multiplied  
555 by  $\delta m$ , the observation error, to get

$$m_{err} = \delta m \times \text{max\_error\_q\_DIAL} \quad (13)$$

556 The error factor can be included in the WRFDA name list under section wrfvar 5  
557 as *max\_error\_q\_DIAL*. We did not yet introduce a separate registry variable for the  
558 temperature. However, we will incorporate the error factor for temperature in the next  
559 version of the operator.

### 560 **3.4 Experimental setup**

561 The assimilation was designed with 10 assimilation time-steps with hourly intervals  
562 between them. As shown in Fig. 5, the RUC was started after a spin-up period of 18 hours  
563 from 12 UTC 23<sup>rd</sup> April to 06 UTC 24<sup>th</sup> April, 2013. This spin-up was necessary for the

564 model to stabilize itself with the initial and boundary conditions so that the model could then  
565 be forced in any desired manner. Only after a minimum spin-up time period are the model  
566 forecasts reliable for further analysis through DA.

567 We conducted 6 experiments: 1) a run (NO\_DA) with no assimilation, 2) a  
568 conventional run (CONV\_DA) with all the conventional data assimilated—the control run, 3)  
569 a TRL DA (T\_DA) with TRL data assimilated along with conventional data using the  
570 standard TEMP forward operator, 4) a WVDIAL DA (Q\_DA) with WVMR data assimilated  
571 along with conventional data using the TDLIDAR operator, 5) a WVDIAL DA (RH\_DA) with  
572 RH data assimilated along with conventional data using the RH operator, and 6) finally the  
573 combined WVDIAL and TRL DA run (QT\_DA) with WVMR and temperature lidar data along  
574 with conventional data assimilated using the TDLIDAR operator. In the Q\_DA run, since the  
575 new operator also required the input of a temperature profile, we used for this the  
576 background temperature. After the initial spin-up of 18 hours, the CONV\_DA run was  
577 initiated for three cycles starting from 0600 UTC each hour. At 0900 UTC, the other DA runs  
578 commenced with the forecast based on the 0800 UTC analysis that was valid for 0900 UTC  
579 as the background for that assimilation time-step. From 0900 UTC, all DA runs including the  
580 CONV\_DA initiated from 0600 UTC were cycled till 1800 UTC (Fig. 5). In addition, a  
581 preconditioning DA run that included only hourly conventional data between 0600 and 0800  
582 UTC was carried out to prepare the lidar DA and then to analyze the exclusive impact of the  
583 lidar data.

584

585 **4. Results**

586           We analyzed the impact of assimilating the temperature and WVMR by applying  
587 TDLIDAR and also the RH forward operator for comparison. This section is divided into 4  
588 subsections: first, the single observation tests for WVMR and temperature are described  
589 followed by an analysis of the sensitivity to the WVMR error factor, the impact of the  
590 temperature, and finally the impact of WVMR. The results of the assimilations are  
591 compared with available, independent radiosondes, which were launched every two hours  
592 during the IOP. It is important to note that the radiosonde measurements performed during  
593 the IOP were not assimilated in any of the experiments conducted.



594

#### 595 **4.1 Single observation tests**

596 The spatial impact of assimilating an observation into the 3DVAR DA system is  
597 dependent on the structure of  $\mathbf{B}$ . In order to understand the behavior of  $\mathbf{B}$ , single  
598 observation tests (SOTs) were conducted. As we assimilated the WVMR and temperature  
599 profiles that also included experiments with background temperature profiles into the  
600 WRFDA system, the correlation of WVMR and temperature needs to be understood to  
601 interpret the combined impact with  $\mathbf{B}$ . Since we were interested in the impact of WVMR  
602 data in the WRFDA system, an increment of  $1 \text{ g kg}^{-1}$  with a unit error of  $1 \text{ g kg}^{-1}$  was  
603 assigned at model level 10, which was approximately 255 m above ground level. This  
604 height was chosen to investigate the impact of assimilating near-surface observations. The  
605 impact on the vertical profile of the SOT is shown in Fig. 6a. The assimilation of a  
606 pseudo-WVMR observation of  $1 \text{ g kg}^{-1}$  results in an analysis increment of  $0.3 \text{ g kg}^{-1}$  at  
607 model level 10. As there is an increment in the WVMR analysis, there is a corresponding  
608 decrement in the temperature analysis at the same sigma level describing the correlation of  
609 temperature and WVMR in the DA system. The temperature at sigma level 10 has  
610 undergone an analysis decrement of 0.15 K. The impact of the assimilated WVMR  
611 pseudo-variable has a Gaussian-like distribution response across the vertical levels. While  
612 the WVMR assimilation created an increment in the WVMR variable, not only in the model  
613 level where assimilation was done but also in the model levels above, the temperature  
614 showed an opposite response. Figure 6b and 6c show the spatial impact of the SOT

615 conducted at model level 10 for an assimilation carried out over the whole model domain.  
616 The impact of the assimilation has the highest WVMR increment at the point of assimilation  
617 and decreases radially with a Gaussian-like shape. The results for the temperature are  
618 similar but with the opposite sign. The WVMR increment was  $0.1 \text{ g kg}^{-1}$  to  $0.3 \text{ g kg}^{-1}$  over a  
619 region 250 km in diameter (Fig. 6b), while the temperature decrement was 0.1 K to 0.15 K  
620 over a region with a 300-km diameter (Fig. 6c). A similar SOT with a 1-K temperature  
621 increment and error of 1 K was also carried out at model level 10. Figure 6d shows the  
622 vertical profile of the SOT used for the temperature increment. An analysis increment of  
623 0.28 K resulted from the SOT with a corresponding decremented response of  $0.17 \text{ g kg}^{-1}$   
624 for the WVMR. The temperature increment was 0.1 K to 0.28 K over a region 300 km in  
625 diameter (Fig. 6e), while the WVMR decrement was  $0.1 \text{ g kg}^{-1}$  to  $0.17 \text{ g kg}^{-1}$  over a region  
626 150 km in diameter (Fig. 6f).

#### 627 **4.2 Sensitivity to WVMR error factor**

628 In order to test the sensitivity to the error factor, the QT\_DA experiment was  
629 conducted in two modes: one with the factor *max\_error\_q\_DIAL* = 1 (QE1) and the other  
630 with *max\_error\_q\_DIAL* = 4 (QE4). There were considerable differences in the model  
631 outputs of the two experiments since the number of observations assimilated was different  
632 in QE1 and QE4. Although the number of observations assimilated in QE1 and QE4 at 09  
633 UTC were similar at 46 and 51, respectively, the later time-steps differed in terms of the

634 number of observations assimilated, which was greater for QE4 than for QE1. The total  
635 number of observations during each assimilation cycle was 70.

636         The model rejected most of the observations in the interfacial layer, where the  
637 gradient of WVMR was high, since the observations were too far away from the first guess.  
638 The difference between the observation and the first guess value of any variable  
639 (innovation) decides whether the observation should be assimilated or not. The vertical  
640 profile of the analysis, profile of the background, and the WVDIAL WVMR observation  
641 profile along with its error bars are depicted in Fig. 7. From Fig. 7 we can see that at 09  
642 UTC, QE4, which used 51 observations, shows a clearer impact on the vertical profile at 09  
643 UTC than QE1, which used 46 observations. The QE1 profile has a higher deviation from  
644 the WVDIAL observations in the PBL than QE4. The WVMR profile from the WVDIAL has a  
645 low observation error until a height of 1300 m but grows significantly above this height.  
646 Hence the error window in the PBL is too small for the observations to be ingested into the  
647 DA.

648         The choice of the error factor is crucial for the quality of the model output. If it is too  
649 low, the model rejects most of the observations, not letting the model adapt toward the  
650 observations, which in turn does not improve the analysis. Otherwise, the model ingests all  
651 the observations including observations with considerable errors compared to the real-time  
652 observations, and this can cause the quality of the analysis to decrease. In this study, the

653 error factor was fixed as four times the DIAL WVMR observation error, which was  
654 considered enough for the experiments to pass the quality check.

### 655 **4.3 Temperature**

656 Figure 8 depicts the temperature profiles at the assimilation time steps 09, 11, 13,  
657 and 15 UTC of all five experiments together with TRL and radiosonde observations. The  
658 radiosonde observations provided by the KIT cube (Kalthoff et al. 2013) were quality  
659 controlled before validation of the temperature profiles since GRAW DFM-09 radiosondes  
660 have a significant bias (Ingleby 2017). At these time-steps in the PBL, the NO\_DA  
661 experiment showed a maximum deviation of around 2 K, which was less than the difference  
662 between the other DA experiments and the radiosonde observations. In the other five  
663 profiles where DA was performed, the temperature profiles significantly improved in the  
664 PBL. The CONV\_DA and T\_DA runs show a significant improvement in the temperature  
665 profile in the PBL compared to the NO\_DA run for all four time-steps. Q\_DA, RH\_DA, and  
666 QT\_DA agree well with the radiosonde at 09 UTC in the PBL but start to deviate slowly to a  
667 higher temperature value after the first time-step. The Q\_DA and RH\_DA deviate by more  
668 in the PBL compared to the other three DA runs since no external temperature profile was  
669 assimilated. As the height increases, the CONV\_DA profile becomes similar to the NO\_DA  
670 profile. This is due to a lack of data points above the PBL in the conventional observations.  
671 However, after assimilating the TRL data along with the conventional data into the model,  
672 the deviation is reduced. In the interfacial layer and the lower free troposphere above this,

673 the T\_DA temperature profile, now having assimilated ample data points, is in good  
674 agreement with the TRL profile at all four assimilation time-steps. The radiosonde profile is  
675 almost the same as the TRL profile for 09, 11, and 13 UTC but deviates above the PBL at  
676 15 UTC. There is a difference of almost 1 K above the PBL; this gradually decreases with  
677 increasing height. This difference occurs due to the decrease of the SNR in the TRL profiles  
678 with height and the increase in distance between the sensors. The Q\_DA, RH\_DA, and  
679 QT\_DA profiles in the lower free troposphere, deviate by less than 1 K and 2 K in the  
680 morning and afternoon, respectively, compared to the radiosonde observations. However,  
681 in the interfacial layer, the QT\_DA is able to capture the inversion at all four time-steps,  
682 which Q\_DA and RH\_DA cannot. Figure 8 shows that Q\_DA, RH\_DA, and QT\_DA deviate  
683 by more at higher ambient temperatures. In short, Q\_DA, RH\_DA, and QT\_DA do not  
684 further improve the temperature profiles of the model compared to the improvement made  
685 by T\_DA.

686 Figure 9a and 9b shows the RMSE with respect to the radiosonde data for all four  
687 assimilation times shown in Fig. 8 and the RMSE with respect to lidar data for all ten  
688 assimilation times, respectively. The overall average RMSE for each experiment (Fig. 9c  
689 and 9d), and the relative change in the RMSE for other DA experiments with respect to  
690 CONV\_DA (Fig. 9e and 9f). At 09 UTC, in Fig. 9c, CONV\_DA and T\_DA have almost the  
691 same RMSE, though the radiosonde temperature profile deviates from the TRL  
692 observations slightly in the upper part of the PBL region. At 11 and 13 UTC, the RMSE of

693 T\_DA has the lowest value. At 15 UTC, the RMSE is higher due to the difference between  
694 the TRL and radiosonde profiles above the PBL which has been discussed earlier. Q\_DA,  
695 RH\_DA, and QT\_DA have a slightly higher RMSE than the other two DA runs but show an  
696 improvement compared to the NO\_DA experiment. Compared to CONV\_DA, the relative  
697 change in the RMSE ( $\Delta$  RMSE) in Fig. 9e for T\_DA shows a decrease of 0.1 K, but Q\_DA,  
698 RH\_DA, and QT\_DA show an increase of 0.5 K, 0.5K, and 0.45 K, respectively.

699 The RMSE of the analysis compared to the lidar observations is shown in Fig. 9b  
700 for all 10 assimilation time-steps. Q\_DA, RH\_DA, and QT\_DA overestimated the  
701 temperature during daytime and, hence, the temperature RMSE with respect to the TRL  
702 observations increases from the first assimilation to the later cycles and decreases again  
703 for the final cycle. Q\_DA and RH\_DA have a higher RMSE than NO\_DA for later cycles.  
704 The interesting feature to note here is that when the amount of moisture in the boundary  
705 layer is higher—that is, from 0900 UTC to 1100 UTC and from 1400 UTC to 1800  
706 UTC—than between 1200 and 1300 UTC, the assimilation has a higher impact. The RMSE  
707 for QT\_DA is less than for CONV\_DA during this time period. Between 1200 UTC and 1300  
708 UTC, when the moisture in this region is lower, the temperature is overestimated, leading to  
709 a higher RMSE during this time. This is again a clear impact of the static nature of the  
710 background error covariance. Due to these counteracting impacts of the assimilation at  
711 different time-periods, the RMSEs for CONV\_DA and QT\_DA are similar in magnitude. The  
712 T\_DA temperature RMSE is mostly constant over the assimilation cycles although there is a

713 decrease of 0.2 K at around 1300 UTC from 0.4 K at 0900 UTC. From Fig. 9f, QT\_DA has  
714 an increase of less than 0.05 K in  $\Delta$  RMSE, which means that QT\_DA did not worsen  
715 CONV\_DA much, whereas Q\_DA and RH\_DA showed an increase of 0.5 K in  $\Delta$  RMSE.  
716 T\_DA shows a decrease of 0.7 K in  $\Delta$  RMSE. In summary, T\_DA outperformed all the other  
717 experiments in terms of the temperature impact.

#### 718 **4.4 Water vapor mixing ratio**

719 Figure 10 depicts the profiles of the analyzed WVMR at the assimilation time steps  
720 09, 11, 13, and 15 UTC for all the different DA experiments including the observations. The  
721 DIAL WVMR observations were limited to a height of 2.5 km since the observation error  
722 was higher than the observed value.

723 All the assimilation runs do not show much difference from NO\_DA in the PBL at 09  
724 UTC. The surface observations were well captured by all the experiments at 11 UTC except  
725 for Q\_DA which shows insignificant values of WVMR. But in the PBL above the surface  
726 layer, Q\_DA and QT\_DA are in good agreement with the radiosonde and DIAL observations  
727 at later time-steps. The Q\_DA and QT\_DA profiles agree with the radiosonde and DIAL  
728 observations at 13 and 15 UTC, whereas NO\_DA, CONV\_DA, and T\_DA have higher  
729 values of WVMR in the PBL. The Q\_DA and QT\_DA profiles are similar to those of the other  
730 two assimilation experiments in the surface layer since there were no lidar observations  
731 available at those levels. NO\_DA shows an overestimation in the WVMR of around  $1 \text{ g kg}^{-1}$

732 in the PBL. RH\_DA did not outperform Q\_DA and QT\_DA as expected although it was close  
733 to QT\_DA at 09 UTC.

734 The interfacial layer was best captured by Q\_DA and QT\_DA at all time-steps apart  
735 from the first assimilation time-step at 09 UTC. NO\_DA and CONV\_DA underestimated the  
736 WVMR at all time-steps, whereas T\_DA shows a positive deviation at 13 and 15 UTC in the  
737 interfacial layer. RH\_DA shows a negative deviation at 11 UTC and a positive deviation at  
738 15 UTC. The lower free troposphere impact for Q\_DA, RH\_DA, and QT\_DA is in better  
739 agreement with the observations than compared to the other runs, which have mixed  
740 results. NO\_DA and CONV\_DA always have a positive deviation. T\_DA has positive and  
741 negative deviations at 09 and 15 UTC, respectively, but matches with Q\_DA, RH\_DA, and  
742 QT\_DA at 11 and 13 UTC. In short, Q\_DA and QT\_DA had a more major impact on the  
743 WVMR than the other experiments.

744 Figures 11a and 11b depict the WVMR RMSE compared to the radiosonde  
745 observations at 09, 11, 13, and 15 UTC, and the WVMR RMSE compared to the lidar  
746 observations at all ten assimilation time steps from 09 UTC to 18 UTC, respectively. The  
747 overall average of RMSE for each experiment are shown in Figs. 11c and 11d. The relative  
748 change in RMSE for the other DA experiments compared to CONV\_DA are shown in Figs.  
749 11e and 11f. Keeping in mind the radiosonde error due to drifting, Q\_DA and QT\_DA  
750 performed better than the other experiments although the difference with T\_DA was less.  
751 The RMSE for RH\_DA is the same as for CONV\_DA although slightly better than T\_DA and



752 QT\_DA. From Fig. 11a, the decline in WVMR RMSE as the assimilation cycle progresses is  
753 visible. Although the QT\_DA RMSE decline rate is small, the decrease is consistent.  
754 Although the overall RMSE for Q\_DA and QT\_DA is closer to that for T\_DA and CONV\_DA,  
755 it is lower (Fig. 11c). The RMSE differences compared to CONV\_DA are considerably less  
756 with magnitudes of +0.01 g kg<sup>-1</sup> for RH\_DA, +0.03 g kg<sup>-1</sup> for QT\_DA, and +0.05 g kg<sup>-1</sup> for  
757 T\_DA. Q\_DA has a difference of -0.05 g kg<sup>-1</sup> compared to CONV\_DA.

758           Compared to the WVDIAL observations, the RMSEs in the WVMR (Figs. 11b, d)  
759 also have a similar declining trend to those seen in the radiosonde comparisons in  
760 consecutive assimilation cycles, but the decline is higher. An important difference between  
761 the WVDIAL and radiosonde observations which needs to be considered is the error due to  
762 the temporal coverage of the two datasets. The WVDIAL dataset gives a complete profile of  
763 the atmosphere every 10 s, while the radiosonde provides data only from the point of  
764 ascent. The mean rate of ascent of the radiosondes launched during IOP 6 of the HOPE  
765 campaign was around 5 m s<sup>-1</sup>. This means that the time taken for a radiosonde to cross the  
766 PBL (taking its height to be 1500 m) would be 5 minutes, which is still 30 times higher than  
767 the time required for obtaining a single lidar profile. This temporal resolution is not optimal if  
768 the atmosphere is rapidly changing. Hence, the DIAL dataset is a continuous measurement  
769 whereas the radiosonde data are instantaneous ones. This also explains the reason why  
770 the DIAL dataset does not have such a smooth profile as the radiosonde data because the  
771 DIAL data capture all the fluctuations in the atmosphere. Q\_DA and QT\_DA (Fig. 11b) have

772 the lowest RMSE in all the assimilation cycles; also, the declining trend for the RMSE in the  
773 successive assimilations proves that the model successfully corrects the WVMR. T\_DA  
774 does not show a visible impact for successive assimilations. Hence, the WVMR RMSE for  
775 T\_DA in Fig. 11b is always higher than for Q\_DA and QT\_DA. However, the WVMR RMSE  
776 for T\_DA has a value similar to the CONV\_DA. Although RH\_DA has lower RMSE values  
777 than CONV\_DA at 09 and 10 UTC, later cycles have a higher RMSE. In Fig. 11d, the overall  
778 RMSE for QT\_DA is the lowest for all the experiments. The  $\Delta$  RMSE in Fig. 11f indicates  
779 that there is a decrease of  $0.36 \text{ g kg}^{-1}$  for QT\_DA and  $0.3 \text{ g kg}^{-1}$  for Q\_DA but only  $0.03 \text{ g}$   
780  $\text{kg}^{-1}$  for T\_DA when compared to CONV\_DA. RH\_DA shows an increase of  $0.02 \text{ g kg}^{-1}$   
781 compared to CONV\_DA. Figure 12 shows an analysis of the difference between QT\_DA  
782 and CONV\_DA. The spatial analysis difference at 09 UTC and 18 UTC on 24 April 2013 are  
783 shown in Fig. 12a and 12b, respectively. A vertical cross-section of the analysis difference  
784 at 09 UTC is shown in Fig. 12c. In order to analyze the impact of the assimilated lidar data,  
785 a 6-hr forecast difference between QT\_DA and CONV\_DA initiated from 18 UTC is shown  
786 in Fig. 12d. However the assimilation impact cannot be due completely to the lidar  
787 observations and, presumably, the number of observations in the conventional data should  
788 be considered. The spatial analyses shown in Figs. 12a, b, and d are for a height of 2000 m,  
789 which is assumed to be the PBL top, where the impact is significant. The impact of a single  
790 lidar profile spreading over an area with a diameter of 300 km shows the potential of a  
791 network of lidars. The forecast difference after six hours initiated from 18 UTC (Fig. 12d)

792 clearly shows that the impact of the assimilation is both enduring and stable since the  
793 impact of the assimilated lidar data lasts for short-range forecasts and does not lead to  
794 significant errors during this forecast range. The six-hour forecast difference does not  
795 exceed an absolute value of  $1.2 \text{ g kg}^{-1}$  in the areas near the lidar instrument location, which  
796 accounts for the stability of the atmosphere after assimilating the thermodynamic lidar data.

797

## 798 **5. Summary and outlook**

799 In this study, we investigated the impact of assimilating WVMR and temperature  
800 data from lidar systems on the vertical structure of temperature and moisture inside the  
801 PBL. For this purpose, we applied WRF version 3.8.1 together with its 3DVAR DA system at  
802 a convection-permitting horizontal resolution of 2.5 km over central Europe. The DA system  
803 was operated in the RUC mode, meaning that the assimilations were hourly. For the  
804 present study, lidar data from the HOPE campaign were used for the assimilation. The IOP  
805 took place from 0900 UTC to 1800 UTC on the 24 April 2013 in western Germany on a  
806 clear-sky day with hardly any optically thick clouds. Temperature data from heights of 500 m  
807 to 3000 m above the ground were taken for the experiment. WVMR data were taken from  
808 400 m to 2500 m above the ground level. Data from lower levels had to be discarded due to  
809 the overlap error. Apart from the lidar measurements, there were four radiosonde launches  
810 at 09, 11, 13 and 15 UTC. The mean of these radiosonde measurements was used for  
811 calibrating the TRL and as an independent measurement for comparison with the model  
812 output since these radiosonde measurements were not assimilated in the DA system.

813           Six model runs were conducted for the whole impact study. A run (NO\_DA) with no  
814 data assimilated, conventional data assimilation (CONV\_DA) or the control run with only  
815 conventional observations from the ECMWF, TRL data assimilation (T\_DA) along with the  
816 conventional dataset, WVMR data assimilation (Q\_DA) along with the conventional dataset,  
817 RH data assimilation (RH\_DA) along with the conventional dataset, and finally the WVMR  
818 and TRL data assimilation (QT\_DA) along with the conventional data.

819           In this study, we introduced a new forward operator called TDLIDAR for direct  
820 WVMR DA, which was developed through the modification of an already-existing operator  
821 in the WRFDA system, the AIRSRET operator. Also, separate sensitivity tests were  
822 conducted with the QT\_DA to study the sensitivity of the newly introduced error factor  
823 ( *max\_error\_q\_DIAL*) in the WRFDA registry. SOTs were conducted to analyze the  
824 response of the input WVMR and temperature data separately in the DA system. An  
825 increase in the WVMR resulted in a subsequent cooling at the point of assimilation in the  
826 model. On the other hand, an increase in the temperature resulted in a subsequent drying.

827           The impact of the assimilation of WVMR and temperature lidar data through the  
828 new forward operator was, overall, positive. The input observations were assimilated with a  
829 very low number of rejected observations: the model only rejected a few observations  
830 during the first assimilation cycle. The WVMR and temperature profiles of the model output  
831 indicated that the input lidar observations could correct the first guess during the  
832 assimilation process to a reasonable extent. From the results of the five DA runs, we

833 conclude that, the assimilation of both temperature and WVMR lidar observations improved  
834 the thermodynamic profiles in the analyses. T\_DA and Q\_DA improved the temperature  
835 and moisture profiles, respectively, whereas QT\_DA improved both compared to  
836 CONV\_DA. RH\_DA did not outperform either Q\_DA or QT\_DA in the study, showing that  
837 the TDLIDAR operator leads to a better impact than the RH operator. We quantified the  
838 analyses by their RMSE with respect to the assimilated lidar observations as well as  
839 independent radiosonde observations. However, the lidar observations were more suitable  
840 for model verification than radiosonde data because they point exactly to the zenith rather  
841 than along an irregular vertical track. The WVMR RMSE computed with respect to the  
842 WVDIAL observations for QT\_DA reduced by 40% compared to those computed for  
843 CONV\_DA run whereas RH\_DA did not show an overall improvement. This highlights that  
844 using the forward operator for the data input had a positive impact on the modeled WVMR  
845 variable. However, at the same time, the impact on the temperature was reduced due to the  
846 significant dependency between the WVMR and temperature variables in the analysis.

847 In real-time operational forecasting with data assimilated from in-situ instruments  
848 like lidars, which provide data with a very low observational bias, a deterministic DA system  
849 whose correlation statistics are derived from a set of forecast error differences might not  
850 provide the best analysis. With the introduction of a flow-dependent background  
851 error-covariance matrix with the help of ensemble-based DA systems, the cross-correlation  
852 between the temperature and humidity variables is expected to be a better representative

853 of the real-time scenario. The matrix  $\mathbf{B}$  in ensemble-based DA systems reflects the dynamic  
854 nature of the atmosphere. Thus, we plan to assimilate thermodynamic lidar data with  
855 ensemble DA techniques in the future. Furthermore, modules for the conversion of absolute  
856 humidity and specific humidity to the WVMR will be incorporated. Currently, with a limited  
857 number of lidars, we limited our studies to convective-scale DA. However, in the future, with  
858 a larger number of lidars which operate as a network, we can enhance our studies to  
859 synoptic-scale DA. We foresee synoptic-scale DA of lidar networks as very beneficial for  
860 operational numerical weather forecasting centers.

861

862

### Acknowledgments

863 We express our sincere gratitude to the High Performance Computing Centre Stuttgart  
864 (HLRS) for providing the necessary computational resources for the completion of the  
865 simulations. We are also grateful to the ECMWF for providing the operational analysis data.  
866 We also express our sincere gratitude to colleagues from KIT Cube for providing  
867 radiosoundings during the IOPs.

868

869

### Appendix

870 The total derivative of RH expands as per the equation

$$\begin{aligned} \delta RH &= 1.607 \frac{p}{E(T)} \delta m + 1.607 \frac{m}{E(T)} \delta p - 1.607 \frac{mp}{(E(T))^2} \delta(E(T)) & (A1) \\ &= \frac{1.607}{E(T)} \left[ p \delta m + m \delta p - mp \left( \frac{(17.67) \cdot (243.5)}{(T - 29.65)^2} \right) \delta T \right] & ) \end{aligned}$$

871 After dividing Eq. A1 by  $RH$  we get the relative error equation

$$\frac{\delta RH}{RH} = \frac{\delta m}{m} + \frac{\delta p}{p} - \left( \frac{(17.67) \cdot (243.5)}{(T - 29.65)^2} \right) \delta T \quad (A2)$$

872 For normal atmospheric conditions

$$873 \quad T = 300K, p = 100,000 Pa, m = 0.01 kgkg^{-1},$$

$$874 \quad \delta m = 0.001 kgkg^{-1}, \delta T = 1.1 K, \delta p = 50 Pa.$$

875 We took a normal value of 10 g kg<sup>-1</sup> and an error of 1 g kg<sup>-1</sup> for the mixing ratio in the

876 numerical example, which are similar to the values for the absolute humidity measurements

877 from the WVDIAL. Similarly, a temperature error of 1.1 K was taken for the TRL

878 measurements. Substituting the above values in Eq. A2, we get these values for the

879 individual terms:

$$880 \quad \frac{\delta m}{m} = 10\%,$$

$$881 \quad \frac{\delta p}{p} = 0.05\%,$$

$$882 \quad \left( \frac{(17.67) \cdot (243.5)}{(T - 29.65)^2} \right) \delta T = 6.5\%.$$

883

884

885 The WVMR error  $\delta m$  expands to

$$\delta m = \frac{R_L T}{p} \delta \rho_{WV} + \frac{\rho_{WV} R_L}{p} \delta T + \frac{-\rho_{WV} R_L T}{p^2} \delta p \quad (A3)$$

886 For normal atmospheric conditions

$$887 \quad T = 300K, p = 100,000 Pa, R_L = 287 JK^{-1}kg^{-1}, \rho_{WV} = 0.01 kgkg^{-1},$$

$$888 \quad \delta \rho_{WV} = 0.001 kgkg^{-1}, \delta T = 1.1 K, \delta p = 50 Pa.$$

889 Substituting the above values we get

$$890 \quad \frac{R_L T}{p} \delta \rho_{WV} = \underline{861} \times 10^{-6} \text{ kg/kg},$$

$$891 \quad \frac{\rho_{WV} R_L}{p} \delta T = \underline{31.57} \times 10^{-6} \text{ kg/kg},$$

$$892 \quad \frac{\rho_{WV} R_L T}{p^2} \delta p = \underline{4.305} \times 10^{-6} \text{ kg/kg}.$$



893

894

## References

895 Adam, S., A. Behrendt, T. Schwitalla, E. Hammann, and V. Wulfmeyer, 2016: First  
896 assimilation of temperature lidar data into an NWP model: Impact on the simulation of  
897 the temperature field, inversion strength and PBL depth. *Quart. J. Roy. Meteor. Soc.*,  
898 **142**, 2882–2896.

899 Apituley, A., K. M. Wilson, C. Potma, H. Volten, and M. de Graaf, 2009: Performance  
900 Assessment and Application of Caeli — A high-performance Raman lidar for diurnal  
901 profiling of Water Vapour, Aerosols and Clouds. *Proceedings of the 8th International  
902 Symposium on Tropospheric Profiling 2009 Oct.* Delft, Netherlands, S06-O10, 4 pp.  
903 [Available at <http://projects.knmi.nl/cesar/istp8/data/1753005.pdf>.]

904 Aranami, K., T. A. Hara, Y. A. Ikuta, K. O. Kawano, K. E. Matsubayashi, H. I. Kusabiraki, T.  
905 A. Ito, T. A. Egawa, K. O. Yamashita, Y. U. Ota, and Y. O. Ishikawa, 2015: A new  
906 operational regional model for convection-permitting numerical weather prediction at  
907 JMA. *Research activities in atmospheric and oceanic modelling*. CAS/JSC Working  
908 Group on Numerical Experimentation. [available at  
909 [https://www.wcrp-climate.org/WGNE/BlueBook/2015/individual-articles/05\\_Aranami\\_K  
910 ohei\\_asuca.pdf](https://www.wcrp-climate.org/WGNE/BlueBook/2015/individual-articles/05_Aranami_Kohei_asuca.pdf).]

911 Arshinov, Y., S. Bobrovnikov, I. Serikov, A. Ansmann, U. Wandinger, D. Althausen, I. Mattis,  
912 and D. Müller, 2005: Daytime operation of a pure rotational Raman lidar by use of a

913 Fabry–Perot interferometer. *Appl. Opt.*, **44**, 3593–3603.

914 Barker, D. M., W. Huang, Y.-R. Guo, A. J. Bourgeois, and Q. N. Xiao, 2004: A  
915 Three-Dimensional Variational Data Assimilation system for MM5: Implementation and  
916 initial results. *Mon. Wea. Rev.*, **132**, 897–914.

917 Bauer, H.-S., T. Schwitalla, V. Wulfmeyer, A. Bakhshaii, U. Ehret, M. Neuper, and O.  
918 Caumont, 2015: Quantitative precipitation estimation based on high-resolution  
919 numerical weather prediction and data assimilation with WRF – A performance test.  
920 *Tellus*, **67**, 25047, doi:10.3402/tellusa.v67.25047.

921 Behrendt, A., and J. Reichardt, 2000: Atmospheric temperature profiling in the presence of  
922 clouds with a pure rotational Raman lidar by use of an interference-filter-based  
923 polychromator. *Appl. Opt.*, **39**, 1372–1378, doi.

924 Behrendt, A., T. Nakamura, and T. Tsuda, 2004: Combined temperature lidar for  
925 measurements in the troposphere, stratosphere, and mesosphere. *Appl. Opt.*, **43**,  
926 2930, doi:10.1364/ao.43.002930.

927 Behrendt, A., V. Wulfmeyer, A. Riede, G. Wagner, S. Pal, H. Bauer, M. Radlach, and F.  
928 Späth, 2009: Three-dimensional observations of atmospheric humidity with a scanning  
929 differential absorption Lidar. *Remote Sens. Clouds Atmos. XIV*, **7475**, 74750L,  
930 doi:10.1117/12.835143.

931 Behrendt, A., V. Wulfmeyer, E. Hammann, S. K. Muppa, and S. Pal, 2015: Profiles of  
932 second- to fourth-order moments of turbulent temperature fluctuations in the

933 convective boundary layer: First measurements with rotational Raman lidar. *Atmos.*  
934 *Chem. Phys.*, **15**, 5485–5500.

935 Benjamin, S. G., S. S. Weygandt, J. M. Brown, T. L. Smith, T. Smirnova, W. R. Moninger, B.  
936 Schwartz, E. J. Szoke, and K. Brundage, 2004: An hourly assimilation-forecast cycle:  
937 The RUC. *Mon. Wea. Rev.*, **132**, 495–518.

938 Benjamin, S. G., S. S. Weygandt, J. M. Brown, M. Hu, C. R. Alexander, T. G. Smirnova, J. B.  
939 Olson, E. P. James, D. C. Dowell, G. A. Grell, and H. Lin, 2016: A North American  
940 hourly assimilation and model forecast cycle: The rapid refresh. *Mon. Wea. Rev.*, **144**,  
941 1669–1694.

942 Berre, L., 2000: Estimation of synoptic and mesoscale forecast error covariances in a  
943 limited-area model. *Mon. Wea. Rev.*, **128**, 644–667.

944 Berre, L., S. E. Ştefănescu, and M. B. Pereira, 2006: The representation of the analysis  
945 effect in three error simulation techniques. *Tellus*, **58**, 196–209.

946 Bhawar, R., P. Di Girolamo, D. Summa, C. Flamant, D. Althausen, A. Behrendt, C. Kiemle, P.  
947 Bosser, M. Cacciani, C. Champollion, T. Di Iorio, R. Engelmann, C. Herold, D. Müller, S.  
948 Pal, M. Wirth, and V. Wulfmeyer, 2011: The water vapour intercomparison effort in the  
949 framework of the Convective and Orographically-induced Precipitation Study:  
950 Airborne-to-ground-based and airborne-to-airborne lidar systems. *Quart. J. Roy.*  
951 *Meteor. Soc.*, **137**, 325–348.

952 Bielli, S., M. Grzeschik, E. Richard, C. Flamant, C. Champollion, C. Kiemle, M. Dorninger,

953 and P. Brousseau, 2012: Assimilation of water-vapour airborne lidar observations:  
954 Impact study on the COPS precipitation forecasts. *Quart. J. Roy. Meteor. Soc.*, **138**,  
955 1652–1667.

956 Blumberg, W. G., D. D. Turner, U. Löhnert, and S. Castleberry, 2015: Ground-based  
957 temperature and humidity profiling using spectral infrared and microwave observations.  
958 Part II: Actual retrieval performance in clear-sky and cloudy conditions. *J. Appl. Meteor.*  
959 *Climatol.*, **54**, 2305–2319.

960 Bolton, D., 1980: The computation of equivalent potential temperature. *Mon. Wea. Rev.*,  
961 **108**, 1046–1053.

962 Bösenberg, J., 1998: Ground-based differential absorption lidar for water-vapor and  
963 temperature profiling: Methodology. *Appl. Opt.*, **37**, 3845–3860.

964 Brocard, E., R. Philipona, A. Haefele, G. Romanens, A. Mueller, D. Ruffieux, V. Simeonov,  
965 and B. Calpini, 2013: Raman lidar for meteorological observations, RALMO - Part 2:  
966 Validation of water vapor measurements. *Atmos. Meas. Tech.*, **6**, 1347–1358.

967 Brousseau, P., L. Berre, F. Bouttier, and G. Desroziers, 2011: Background-error covariances  
968 for a convective-scale data-assimilation system: AROME-France 3D-Var. *Quart. J. Roy.*  
969 *Meteor. Soc.*, **137**, 409–422.

970 Browning, K. A., A. M. Blyth, P. A. Clark, U. Corsmeier, C. J. Morcrette, J. L. Agnew, S. P.  
971 Ballard, D. Bamber, C. Barthlott, L. J. Bennett, and K. M. Beswick, 2007: The  
972 convective storm initiation project. *Bull. Amer. Meteor. Soc.*, **88**, 1939–1955.

973 Cadeddu, M. P., G. E. Peckham, and C. Gaffard, 2002: The vertical resolution of  
974 ground-based microwave radiometers analyzed through a multiresolution wavelet  
975 technique. *IEEE Trans. Geosci. Remote Sens.*, **40**, 531–540.

976 Cooney, J., 1972: Measurement of atmospheric temperature profiles by Raman backscatter.  
977 *J. Appl. Meteor.*, **11**, 108–112.

978 Courtier, P., E. Andersson, W. Heckley, D. Vasiljevic, M. Hamrud, A. Hollingsworth, F.  
979 Rabier, M. Fisher, and J. Pailleux, 1998: The ECMWF implementation of  
980 three-dimensional variational assimilation (3D-Var). I: Formulation. *Quart. J. Roy.  
981 Meteor. Soc.*, **124**, 1783–1807.

982 Crook, N. A., 1996: Sensitivity of moist convection forced by boundary layer processes to  
983 low-level thermodynamic fields. *Mon. Wea. Rev.*, **124**, 1767–1785.

984 Dailey, P. S., and R. G. Fovell, 1999: Numerical simulation of the interaction between the  
985 sea-breeze front and horizontal convective rolls. Part I: Offshore ambient flow. *Mon.  
986 Wea. Rev.*, **127**, 858–878.

987 Di Girolamo, P., R. Marchese, D. N. Whiteman, and B. B. Demoz, 2004: Rotational Raman  
988 Lidar measurements of atmospheric temperature in the UV. *Geophys. Res. Lett.*, **31**,  
989 L01106, doi:10.1029/2003GL018342.

990 Dinoev, T., V. B. Simeonov, Y. Arshinov, S. Bobrovnikov, P. Ristori, B. Calpini, M. Parlange,  
991 and H. van den Bergh, 2013: Raman Lidar for meteorological observations, RALMO -  
992 Part 1: Instrument description. *Atmos. Meas. Tech.*, **6**, 1329–1346.

993 Dixon, M., Z. Li, H. Lean, N. Roberts, and S. Balland, 2009: Impact of data assimilation on  
994 forecasting convection over the United Kingdom using a high-resolution version of the  
995 met office unified model. *Mon. Wea. Rev.*, **137**, 1562–1584.

996 Donlon, C. J., M. Martin, J. Stark, J. Roberts-Jones, E. Fiedler, and W. Wimmer, 2012: The  
997 Operational Sea Surface Temperature and Sea Ice Analysis (OSTIA) system. *Remote*  
998 *Sens. Environ.*, **116**, 140–158.

999 Engelbart, D. A. M., and E. Haas, 2006: LAUNCH-2005-International Lindenberg campaign  
1000 for assessment of humidity and cloud profiling systems and its impact on  
1001 high-resolution modelling. *7th International Symposium on Tropospheric profiling:*  
1002 *Needs and technologies*, 11–17.

1003 Evensen, G., 2003: The Ensemble Kalman Filter: Theoretical formulation and practical  
1004 implementation. *Ocean Dyn.*, **53**, 343–367.

1005 Fischer, L., 2013: Statistical characterisation of water vapour variability in the troposphere.  
1006 *(Doctoral dissertation, Imu)*.

1007 Geerts, B., D. Parsons, C. L. Ziegler, T. M. Weckwerth, M. I. Biggerstaff, R. D. Clark, M. C.  
1008 Coniglio, B. B. Demoz, R. A. Ferrare, W. A. Gallus, Jr., K. Haghi, J. M. Hanesiak, P. M.  
1009 Klein, K. R. Knupp, K. Kosiba, G. M. McFarquhar, J. A. Moore, A. R. Nehrir, M. D.  
1010 Parker, J. O. Pinto, R. M. Rauber, R. S. Schumacher, D. D. Turner, Q. Wang, X. Wang,  
1011 Z. Wang, and J. Wurman, 2017: The 2015 plains elevated convection at night field  
1012 project. *Bull. Amer. Meteor. Soc.*, **98**, 767–786.

1013 Goldsmith, J. E. M., F. H. Blair, S. E. Bisson, and D. D. Turner, 1998: Turn-key Raman lidar  
1014 for profiling atmospheric water vapor, clouds, and aerosols. *Appl. Opt.*, **37**, 4979–4990.

1015 Grzeschik, M., H. S. Bauer, V. Wulfmeyer, D. Engelbart, U. Wandinger, I. Mattis, D.  
1016 Althausen, R. Engelmann, M. Tesche, and A. Riede, 2008: Four-dimensional  
1017 variational data analysis of water vapor Raman lidar data and their impact on  
1018 mesoscale forecasts. *J. Atmos. Oceanic Technol.*, **25**, 1437–1453.

1019 Gustafsson, N., T. Janjić, C. Schraff, D. Leuenberger, M. Weissmann, H. Reich, P.  
1020 Brousseau, T. Montmerle, E. Wattrelot, A. Bučánek, and M. Mile, 2018: Survey of data  
1021 assimilation methods for convective-scale numerical weather prediction at operational  
1022 centres. *Quart. J. Roy. Meteor. Soc.*, **144**, 1218–1256.

1023 Hammann, E., A. Behrendt, F. Le Mounier, and V. Wulfmeyer, 2015: Temperature profiling  
1024 of the atmospheric boundary layer with rotational Raman lidar during the HD(CP)<sup>2</sup>  
1025 Observational Prototype Experiment. *Atmos. Chem. Phys.*, **15**, 2867–2881.

1026 Harnisch, F., M. Weissmann, C. Cardinali, and M. Wirth, 2011: Experimental assimilation of  
1027 DIAL water vapour observations in the ECMWF global model. *Quart. J. Roy. Meteor.*  
1028 *Soc.*, **137**, 1532–1546.

1029 Honda, Y., M. Nishijima, K. Koizumi, Y. Ohta, K. Tamiya, T. Kawabata, and T. Tsuyuki, 2006:  
1030 A pre-operational variational data assimilation system for a non-hydrostatic model at  
1031 the Japan Meteorological Agency: Formulation and preliminary results. *Quart. J. Roy.*  
1032 *Meteor. Soc.*, **131**, 3465–3475.

1033 Hong, S.-Y., H. Park, H. B. Cheong, J. E. E. Kim, M. S. Koo, J. Jang, S. Ham, S. O. Hwang,  
1034 B. K. Park, E. C. Chang, and H. Li, 2013: The global/regional integrated model system  
1035 (GRIMs). *Asia-Pacific J. Atmos. Sci.*, **49**, 219–243.

1036 Horváth, Á., O. Hautecoeur, R. Borde, H. Deneke, and S. A. Buehler, 2017: Evaluation of  
1037 the EUMETSAT global AVHRR wind product. *J. Appl. Meteor. Climatol.*, **56**,  
1038 2353–2376.

1039 Hu, M., M. Xue, and K. Brewster, 2006: 3DVAR and cloud analysis with WSR-88D level-II  
1040 data for the prediction of the Fort Worth, Texas, tornadic thunderstorms. Part I: Cloud  
1041 analysis and its impact. *Mon. Wea. Rev.*, **134**, 675–698.

1042 Hu, M., S. G. Benjamin, T. T. Ladwig, D. C. Dowell, S. S. Weygandt, C. R. Alexander, and J.  
1043 S. Whitaker, 2017: GSI three-dimensional ensemble-variational hybrid data  
1044 assimilation using a global ensemble for the regional rapid refresh model. *Mon. Wea.*  
1045 *Rev.*, **145**, 4205–4225.

1046 Huang, X. Y., Q. Xiao, D. M. Barker, X. Zhang, J. Michalakes, W. Huang, T. Henderson, J.  
1047 Bray, Y. Chen, Z. M. J. Dudhia, Y. Guo, X. Zhang, D.-J. Won, H.-C. Lin, and Y.-H. Kuo,  
1048 2009: Four-dimensional variational data assimilation for WRF: Formulation and  
1049 preliminary results. *Mon. Wea. Rev.*, **137**, 299–314.

1050 Iacono, M. J., J. S. Delamere, E. J. Mlawer, M. W. Shephard, S. A. Clough, and W. D.  
1051 Collins, 2008: Radiative forcing by long-lived greenhouse gases: Calculations with the  
1052 AER radiative transfer models. *J. Geophys. Res.*, **113**, D13103,



1053 doi:10.1029/2008JD009944.

1054 Ingleby, B., 2017: An assessment of different radiosonde types 2015/2016. *ECMWF Tech.*  
1055 *Memo.*, 69 pp, doi:10.21957/0nje0wpsa.

1056 Ingleby, N. B., A. C. Lorenc, K. Ngan, F. Rawlins, and D. R. Jackson, 2013: Improved  
1057 variational analyses using a nonlinear humidity control variable. *Quart. J. Roy. Meteor.*  
1058 *Soc.*, **139**, 1875–1887.

1059 Ismail, S., and E. V Browell, 1989: Airborne and spaceborne lidar measurements of water  
1060 vapor profiles: a sensitivity analysis; erratum. *Appl. Opt.*, **28**, 4981,  
1061 doi:10.1364/ao.28.004981.

1062 Janjic, Z. I., 2003: A nonhydrostatic model based on a new approach. *Meteor. Atmos. Phys.*,  
1063 **82**, 271–285.

1064 Kalthoff, N., B. Adler, A. Wieser, M. Kohler, K. Träumner, J. Handwerker, U. Corsmeier, S.  
1065 Khodayar, D. Lambert, A. Kopmann, N. Kunka, G. Dick, M. Ramatschi, J. Wickert, and  
1066 C. Kottmeier, 2013: KITcube - A mobile observation platform for convection studies  
1067 deployed during HyMeX. *Meteor. Z.*, **22**, 633–647.

1068 Kingsmill, D. E., 1995: Convection initiation associated with a sea-breeze front, a gust front,  
1069 and their collision. *Mon. Wea. Rev.*, **123**, 2913–2933.

1070 Lange, D., A. Behrendt, and V. Wulfmeyer, 2018: Compact automatic rotational Raman lidar  
1071 system for continuous day- and nighttime temperature and humidity mapping. *EGU*  
1072 *General Assembly Conference Abstracts*, **20**, 9114.

1073 Lee, B. D., R. D. Farley, and M. R. Hjelmfelt, 1991: A numerical case study of convection  
1074 initiation along colliding convergence boundaries in northeast Colorado. *J. Atmos. Sci.*,  
1075 **48**, 2350–2366.

1076 Lenschow, D. H., V. Wulfmeyer, and C. Senff, 2000: Measuring second- through  
1077 fourth-order moments in noisy data. *J. Atmos. Oceanic Technol.*, **17**, 1330–1347.

1078 Lorenc, A. C., 2003: The potential of the ensemble Kalman filter for NWP - A comparison  
1079 with 4D-Var. *Quart. J. Roy. Meteor. Soc.*, **129**, 3183–3203, doi:10.1256/qj.02.132.

1080 Metzendorf, S., 2019: 10 W-Average-Power Single-Frequency Ti:sapphire laser with tuning  
1081 agility- A breakthrough in high-resolution 3D water-vapor measurement. (*Doctoral*  
1082 *Dissertation, uhoh*).

1083 Muppa, S. K., A. Behrendt, H.-S. Bauer, F. Späth, R. Heinze, C. Moseley, and V. Wulfmeyer,  
1084 2018: Characterizing the turbulent higher-order moments in the convective boundary  
1085 layer: Evaluation of large eddy simulations with high-resolution lidar observations.  
1086 *EGU General Assembly Conference Abstracts*, **20**, 14632.

1087 Muppa, S. K., A. Behrendt, F. Späth, V. Wulfmeyer, S. Metzendorf, and A. Riede, 2016:  
1088 Turbulent humidity fluctuations in the convective boundary layer: Case studies using  
1089 water vapour differential absorption lidar measurements. *Bound.-Layer Meteor.*, **158**,  
1090 43–66.

1091 Murphey, H. V., R. M. Wakimoto, C. Flamant, and D. E. Kingsmill, 2006: Dryline on 19 June  
1092 2002 during IHOP. Part I: Airborne Doppler and LEANDRE II analyses of the thin line

1093 structure and convection initiation. *Mon. Wea. Rev.*, **134**, 406–430.

1094 Nakanishi, M., and H. Niino, 2006: An improved Mellor-Yamada Level-3 model: Its  
1095 numerical stability and application to a regional prediction of advection fog.  
1096 *Bound.-Layer Meteor.*, **119**, 397–407.

1097 Nakanishi, M., and H. Niino, 2009: Development of an improved turbulence closure model  
1098 for the atmospheric boundary layer. *J. Meteor. Soc. Japan*, **87**, 895–912.

1099 Niu, G. Y., Z. L. Yang, K. E. Mitchell, F. Chen, M. B. Ek, M. Barlage, A. Kumar, K. Manning,  
1100 D. Niyogi, E. Rosero, M. Tewari, and Y. Xia 2011: The community Noah land surface  
1101 model with multiparameterization options (Noah-MP): 1. Model description and  
1102 evaluation with local-scale measurements. *J. Geophys. Res. Atmos.*, **116**, D12109,  
1103 doi:10.1029/2010JD015139.

1104 Powers, J. G., J. B. Klemp, W. C. Skamarock, C. A. Davis, J. Dudhia, D. O. Gill, J. L. Coen,  
1105 D. J. Gochis, R. Ahmadov, S. E. Peckham, and G. A. Grell, J. Michalakes, S. Trahan, S.  
1106 G. Benjamin, C. R. Alexander, G. J. Dimego, W. Wang, C. S. Schwartz, G. S. Romine, Z.  
1107 Liu, C. Snyder, F. Chen, M. J. Barlage, W. Yu, and M. G. Duda, 2017: The weather  
1108 research and forecasting model: Overview, system efforts, and future directions. *Bull.*  
1109 *Amer. Meteor. Soc.*, **98**, 1717–1737.

1110 Radlach, M., A. Behrendt, and V. Wulfmeyer, 2008: Scanning rotational Raman lidar at 355  
1111 nm for the measurement of tropospheric temperature fields. *Atmos. Chem. Phys.*, **8**,  
1112 159–169.

1113 Reichardt, J., U. Wandinger, V. Klein, I. Mattis, B. Hilber, and R. Begbie, 2012: RAMSES:  
1114 German Meteorological Service autonomous Raman lidar for water vapor, temperature,  
1115 aerosol, and cloud measurements. *Appl. Opt.*, **51**, 8111–8131.

1116 Richard, E., A. Buzzi, and G. Zängl, 2007: Quantitative precipitation forecasting in the Alps:  
1117 The advances achieved by the Mesoscale Alpine Programme. *Quart. J. Roy. Meteor.*  
1118 *Soc.*, **133**, 831–846.

1119 Santanello, J. A., P. A. Dirmeyer, C. R. Ferguson, K. L. Findell, A. B. Tawfik, A. Berg, M. Ek,  
1120 P. Gentine, B. P. Guillod, C. van Heerwaarden, J. Roundy and V. Wulfmeyer, 2018:  
1121 Land-atmosphere interactions: The LoCo perspective. *Bull. Amer. Meteor. Soc.*, **99**,  
1122 1253–1272.

1123 Savitzky, A., and M. J. E. Golay, 1964: Smoothing and differentiation of data by simplified  
1124 least squares procedures. *Anal. Chem.*, **36**, 1627–1639.

1125 Schraff, C., H. Reich, A. Rhodin, A. Schomburg, K. Stephan, A. Perriáñez, and R. Potthast,  
1126 2016: Kilometre-scale ensemble data assimilation for the COSMO model (KENDA).  
1127 *Quart. J. Roy. Meteor. Soc.*, **142**, 1453–1472.

1128 Schwitalla, T., and V. Wulfmeyer, 2014: Radar data assimilation experiments using the IPM  
1129 WRF Rapid Update Cycle. *Meteor. Z.*, **23**, 79–102.

1130 Schwitalla, T., H. S. Bauer, V. Wulfmeyer, and F. Aoshima, 2011: High-resolution simulation  
1131 over central Europe: Assimilation experiments during COPS IOP 9c. *Quart. J. Roy.*  
1132 *Meteor. Soc.*, **137**, 156–175.

1133 Schwitalla, T., H. S. Bauer, V. Wulfmeyer, and K. Warrach-Sagi, 2017: Continuous  
1134 high-resolution midlatitude-belt simulations for July-August 2013 with WRF. *Geosci.*  
1135 *Model Dev.*, **10**, 2031–2055.

1136 Skamarock, W. C., J. B. Klemp, J. Dudhia, D. O. Gill, D. M. Barker, W. Wang, and J. G.  
1137 Powers, 2008: A description of the advanced research WRF Version 3 (No.  
1138 NCAR/TN-475+STR). University Corporation for Atmospheric Research, 113 pp,  
1139 doi:10.5065/D68S4MVH.

1140 Späth, F., A. Behrendt, S. K. Muppa, S. Metzendorf, A. Riede, and V. Wulfmeyer, 2014:  
1141 High-resolution atmospheric water vapor measurements with a scanning differential  
1142 absorption lidar. *Atmos. Chem. Phys. Discuss.*, **14**, 29057–29099.

1143 Späth, F., A. Behrendt, S. Kumar Muppa, S. Metzendorf, A. Riede, and V. Wulfmeyer, 2016:  
1144 3-D water vapor field in the atmospheric boundary layer observed with scanning  
1145 differential absorption lidar. *Atmos. Meas. Tech.*, **9**, 1701–1720.

1146 Späth, F., S. Metzendorf, S. ~K. Muppa, A. Behrendt, and V. Wulfmeyer, 2018: Investigation  
1147 of Humidity Structures from the Land-Surface to the Lower Troposphere Using a  
1148 Scanning DIAL. *EGU General Assembly Conference Abstracts*, **20**, 15198.

1149 Spuler, S. M., K. S. Repasky, B. Morley, D. Moen, M. Hayman, and A. R. Nehrir, 2015:  
1150 Field-deployable diode-laser-based differential absorption lidar (DIAL) for profiling  
1151 water vapor. *Atmos. Meas. Tech.*, **8**, 1073–1087.

1152 Stevens, B., and S. Bony, 2013: What are climate models missing? *Science*, **340**,

1153 1053–1054.

1154 Talbot, C., E. Bou-Zeid, and J. Smith, 2012: Nested mesoscale large-eddy simulations with  
1155 WRF: Performance in real test cases. *J. Hydrometeor.*, **13**, 1421–1441.

1156 Thompson, G., P. R. Field, R. M. Rasmussen, and W. D. Hall, 2008: Explicit forecasts of  
1157 winter precipitation using an improved bulk microphysics scheme. Part II:  
1158 Implementation of a new snow parameterization. *Mon. Wea. Rev.*, **136**, 5095–5115.

1159 Turner, D. D., and J. E. M. Goldsmith, 1999: 24-Hour Raman lidar measurements during  
1160 the Atmospheric Radiation Measurement program’s 1996 and 1997 water vapor  
1161 intensive observation periods. *J. Atmos. Oceanic Technol.*, **16**, 1062–1076.

1162 Turner, D. D., and U. Löhner, 2014: Information content and uncertainties in  
1163 thermodynamic profiles and liquid cloud properties retrieved from the ground-based  
1164 Atmospheric Emitted Radiance Interferometer (AERI). *J. Appl. Meteor. Climatol.*, **53**,  
1165 752–771.

1166 Wagner, G., V. Wulfmeyer, and A. Behrendt, 2011: Detailed performance modeling of a  
1167 pulsed high-power single-frequency Ti:sapphire laser. *Appl. Opt.*, **50**, 5921–5937.

1168 Wagner, G., A. Behrendt, V. Wulfmeyer, F. Späth, and M. Schiller, 2013: High-power  
1169 Ti:sapphire laser at 820 nm for scanning ground-based water–vapor differential  
1170 absorption lidar. *Appl. Opt.*, **52**, 2454–2469.

1171 Weckwerth, T. M., and D. B. Parsons, 2006: A review of convection initiation and motivation  
1172 for IHOP\_2002. *Mon. Wea. Rev.*, **134**, 5–22.

1173 Weckwerth, T. M., J. W. Wilson, and R. M. Wakimoto, 1996: Thermodynamic variability  
1174 within the convective boundary layer due to horizontal convective rolls. *Mon. Wea.*  
1175 *Rev.*, **124**, 769–784.

1176 Weckwerth, T. M., V. Wulfmeyer, R. M. Wakimoto, R. M. Hardesty, J. W. Wilson, and R. M.  
1177 Banta, 1999: NCAR--NOAA lower-tropospheric water vapor workshop. *Bull. Amer.*  
1178 *Meteor. Soc.*, **80**, 2339–2357.

1179 Weckwerth, T. M., K. J. Weber, D. D. Turner, and S. M. Spuler, 2016: Validation of a water  
1180 vapor micropulse differential absorption lidar (DIAL). *J. Atmos. Oceanic Technol.*, **33**,  
1181 2353–2372.

1182 Wei, J., O. Branch, H.-S. Bauer, H.-D. Wizemann, and V. Wulfmeyer, 2017: Impact of  
1183 enhanced hydrological processes on land-atmosphere feedbacks for the Attert  
1184 catchment in Luxembourg - LES runs with WRF-Hydro-NOAH-MP vs. WRF-NOAH-MP.  
1185 *EGU General Assembly Conference Abstracts*, **19**, 16392.

1186 Weisman, M. L., C. Davis, W. Wang, K. W. Manning, and J. B. Klemp, 2008: Experiences  
1187 with 0-36-h explicit convective forecasts with the WRF-ARW model. *Wea. Forecasting*,  
1188 **23**, 407–437.

1189 Wu, W. S., D. F. Parrish, E. Rogers, and Y. Lin, 2017: Regional ensemble-variational data  
1190 assimilation using global ensemble forecasts. *Wea. Forecasting*, **32**, 83–96.

1191 Wulfmeyer, V., and J. Bösenberg, 1998: Ground-based differential absorption lidar for  
1192 water-vapor profiling: assessment of accuracy, resolution, and meteorological

1193 applications. *Appl. Opt.*, **37**, 3825–3844.

1194 Wulfmeyer, V., H. S. Bauer, M. Grzeschik, A. Behrendt, F. Vandenberghe, E. V. Browell, S.  
1195 Ismail, and R. A. Ferrare, 2006: Four-dimensional variational assimilation of water  
1196 vapor differential absorption lidar data: The first case study within IHOP\_2002. *Mon.*  
1197 *Wea. Rev.*, **134**, 209–230, doi:10.1175/MWR3070.1.

1198 Wulfmeyer, V., A. Behrendt, C. Kottmeier, U. Corsmeier, C. Barthlott, G. C. Craig, M. Hagen,  
1199 D. Althausen, F. Aoshima, M. Arpagaus, H. S. Bauer, L. Bennett, A. Blyth, C. Brandau,  
1200 C. Champollion, S. Crewell, G. Dick, P. D. Girolamo, M. Dorninger, Y. Dufournet, R.  
1201 Eigenmann, R. Engelmann, C. Flamant, T. Foken, T. Gorgas, M. Grzeschik, J.  
1202 Handwerker, C. Hauck, H. Höller, W. Junkermann, N. Kalthoff, C. Kiemle, S. Klink, M.  
1203 König, L. Krauss, C. N. Long, F. Madonna, S. Mobbs, B. Neininger, S. Pal, G. Peters, G.  
1204 Pigeon, E. Richard, M. W. Rotach, H. Russchenberg, T. Schwitalla, V. Smith, R.  
1205 Steinacker, J. Trentmann, D. D. Turner, J. V. Baelen, S. Vogt, H. Volkert, T. Weckwerth,  
1206 H. Wernli, A. Wieser, and M. Wirth, 2011: The Convective and Orographically-induced  
1207 Precipitation Study (COPS): The scientific strategy, the field phase, and research  
1208 highlights. *Quart. J. Roy. Meteor. Soc.*, **137**, 3–30.

1209 Wulfmeyer, V., R. M. Hardesty, D. D. Turner, A. Behrendt, M. P. Cadetdu, P. Di Girolamo, P.  
1210 Schlüssel, J. Van Baelen, and F. Zus, 2015: A review of the remote sensing of lower  
1211 tropospheric thermodynamic profiles and its indispensable role for the understanding  
1212 and the simulation of water and energy cycles. *Rev. Geophys.*, **53**, 819–895.



1213 Wulfmeyer, V., S. K. Muppa, A. Behrendt, E. Hammann, F. Späth, Z. Sorbjan, D. D. Turner,  
1214 and R. M. Hardesty, 2016: Determination of convective boundary layer entrainment  
1215 fluxes, dissipation rates, and the molecular destruction of variances: Theoretical  
1216 description and a strategy for its confirmation with a novel lidar system synergy. *J.*  
1217 *Atmos. Sci.*, **73**, 667–692.

1218 Wulfmeyer, V., D. D. Turner; B. Baker, R. Banta, A. Behrendt, T. Bonin, W. A. Brewer, M.  
1219 Buban, A. Choukulkar, E. Dumas R., M. Hardesty, T. Heus, J. Ingwersen, D. Lange, T.  
1220 R. Lee, S. Metzendorf, S. K. Muppa, T. Meyers, R. Newsom, M. Osman, S. Raasch, J.  
1221 Santanello, C. Senff, F. Späth, T. Wagner, and T. Weckwerth, 2018: A new research  
1222 approach for observing and characterizing land–atmosphere feedback. *Bull. Amer.*  
1223 *Meteor. Soc.*, **99**, 1639–1667.

1224 Yang, Z. L., G.-Y. Niu, K. E. Mitchell, K. E. Mitchell, F. Chen, M. B. Ek, M. Barlage, L.  
1225 Longuevergne, K. Manning, D. Niyogi, M. Tewari, and Y. Xia, 2011: The community  
1226 Noah land surface model with multiparameterization options (Noah-MP): 2. Evaluation  
1227 over global river basins. *J. Geophys. Res. Atmos.*, **116**, D12110,  
1228 doi:10.1029/2010JD015140.

1229 Yoshida, S., S. Yokota, H. Seko, T. Sakai, and T. Nagai, 2020: Observation system  
1230 simulation experiments of water vapor profiles observed by Raman lidar using LETKF  
1231 system. *SOLA*, **16**, 43–50.

1232  
1233

1234

## List of Tables

1235

1236 Table 1. Details of assimilated observations with their corresponding observation operators.

1237

1238 Table 2. WRF physics configuration used for the experiments.

1239

1240

## Tables

Type	Conventional Observations									TRL	WVDIAL
Observation Operator	AMDAR	AMV	GNSS-ZTD	METAR	PROFL*	SYNOP	SHIP	BUOY	TEMP*	TEMP*	AIRSRET*
Assimilated observations	1374-1875	2045-3095	1050-1076	261-310	52-57	968-1128	77-104	7-9	0-26	1	1
Average number	1624	2570	1063	286	54	1048	90	8	13	1	1

\*Profile observations

1241

1242 Table 1. Details of assimilated observations with their corresponding observation operators.

1243

1244

Physics	Options implemented
Long wave radiation	RRTMG(Iacono et al., 2008)
Short wave radiation	RRTMG(Iacono et al., 2008)
Cloud microphysics	Thompson scheme(Thompson, Field, Rasmussen, & Hall, 2008)
Planetary boundary layer	MYNN(Nakanishi & Niino, 2006)
Land surface scheme	NOAH-MP LSM(Niu et al., 2011)

1245

1246 Table 2. WRF physics configuration used for the experiments.

1247

1248

## List of figures

1249

1250 Fig. 1. The WRF model domain at a horizontal resolution of 2.5 km with orography and the  
1251 location of the TRL and WVDIAL of UHOH during the HOPE campaign.

1252 Fig. 2. Absolute humidity time series from the WVDIAL with a vertical resolution of 15 m and  
1253 a temporal resolution of 60 s between 09 UTC and 18 UTC on 24 April 2013.

1254

1255 Fig. 3. Temperature time series from the TRL with a vertical resolution of 3.75 m and a  
1256 temporal resolution of 60 s between 09 UTC and 18 UTC on 24 April 2013.

1257

1258 Fig. 4. Observation types and their locations for the assimilation time-step 09 UTC 24 April  
1259 2013. Black: surface stations (SYNOP+METAR), blue: ship observations (SHIP), green:  
1260 aircraft observations and atmospheric motion vectors from satellite (AMDAR+SATOB), red:  
1261 GPS zenith total delay, yellow: radiosondes (TEMP), and brown: wind profiler (PROFL).

1262

1263 Fig. 5. Schematic of the 3DVAR rapid update cycle initialized from the ECMWF analysis. A  
1264 spin-up of 18 hours was performed until 06 UTC on 24 April 2013. Five experiments with  
1265 different setups were performed. NO\_DA (black) is the run with no data assimilation,  
1266 CONV\_DA (green) is the control run assimilating conventional data from 06 UTC to 18 UTC,  
1267 RH\_DA (olive green) is the assimilation with WVDIAL and conventional data from 09 UTC  
1268 to 18 UTC using the RH operator, T\_DA (blue) is the assimilation with TRL and  
1269 conventional data from 09 UTC to 18 UTC, Q\_DA (dark purple) is the assimilation with  
1270 WVDIAL and conventional data from 09 UTC to 18 UTC using the TDLIDAR operator, and  
1271 QT\_DA (red) is the assimilation with WVDIAL, TRL, and conventional data from 09 UTC to  
1272 18 UTC using the TDLIDAR operator.

1273

1274 Fig. 6. Vertical profiles and spatial distribution of analysis increments from single  
1275 observation tests (SOTs) performed for a WVMR increment of  $1 \text{ g kg}^{-1}$  and 1-K temperature  
1276 increment at model level 10 (255 m AGL). (a) Vertical profile, (b) and (c) spatial distribution  
1277 of the analysis increments resulting from the WVMR SOT. (c), (e) and (f) results of the  
1278 temperature SOT.

1279

1280

1281 Fig. 7. Vertical profiles of the WVMR from 09 UTC, 11 UTC, 13 UTC, and 15 UTC on 24  
1282 April 2013 for the QE1 and QE4 experiments along with WVDIAL observations and  
1283 associated error bars. The solid line represents the analysis profile and the dashed line the  
1284 background profile.

1285

1286 Fig. 8. Temperature profiles of TRL, radiosondes, and analyses at (a) 09 UTC, (b) 11 UTC,  
1287 (c) 13 UTC, and (d) 15 UTC. The TRL observations (orange) along with their total errors  
1288 shown by error bars are plotted up to 3000 m AGL. Radiosonde observations (violet) which  
1289 were not assimilated are plotted for reference. Black: NO\_DA, green: CONV\_DA, olive  
1290 green: RH\_DA, dark purple: Q\_DA, blue: T\_DA, and red: QT\_DA.

1291

1292 Fig. 9. Temperature RMSE of the analyses compared to local radiosonde data not  
1293 assimilated into the model together with assimilated TRL observations. (a) Comparison of  
1294 the RMSE at the four assimilation time-steps (09, 11, 13, 15 UTC) with respect to the  
1295 radiosonde data and (b) comparison of the RMSE with respect to the TRL observations at  
1296 the 10 assimilation time-steps from 09 UTC to 18 UTC 24 April 2013. (c) and (d)  
1297 comparison of the overall temperature RMSE for the corresponding time-steps for (a) and  
1298 (b), respectively. (e) and (f) depict the relative change in the average RMSE of (c) and (d),  
1299 respectively, compared to the RMSE of CONV\_DA.

1300

1301 Fig. 10. WVMR profiles of WVDIAL, radiosondes, and analyses at (a) 09 UTC, (b) 11 UTC,  
1302 (c) 13 UTC, and (d) 15 UTC. The WVDIAL observations (orange) along with their total  
1303 errors shown by error bars are plotted up to 2500 m AGL. Radiosonde observations (violet)  
1304 which were not assimilated are plotted for reference. Black: NO\_DA, green: CONV\_DA,  
1305 olive green: RH\_DA, dark purple: Q\_DA, blue: T\_DA, and red: QT\_DA are shown.

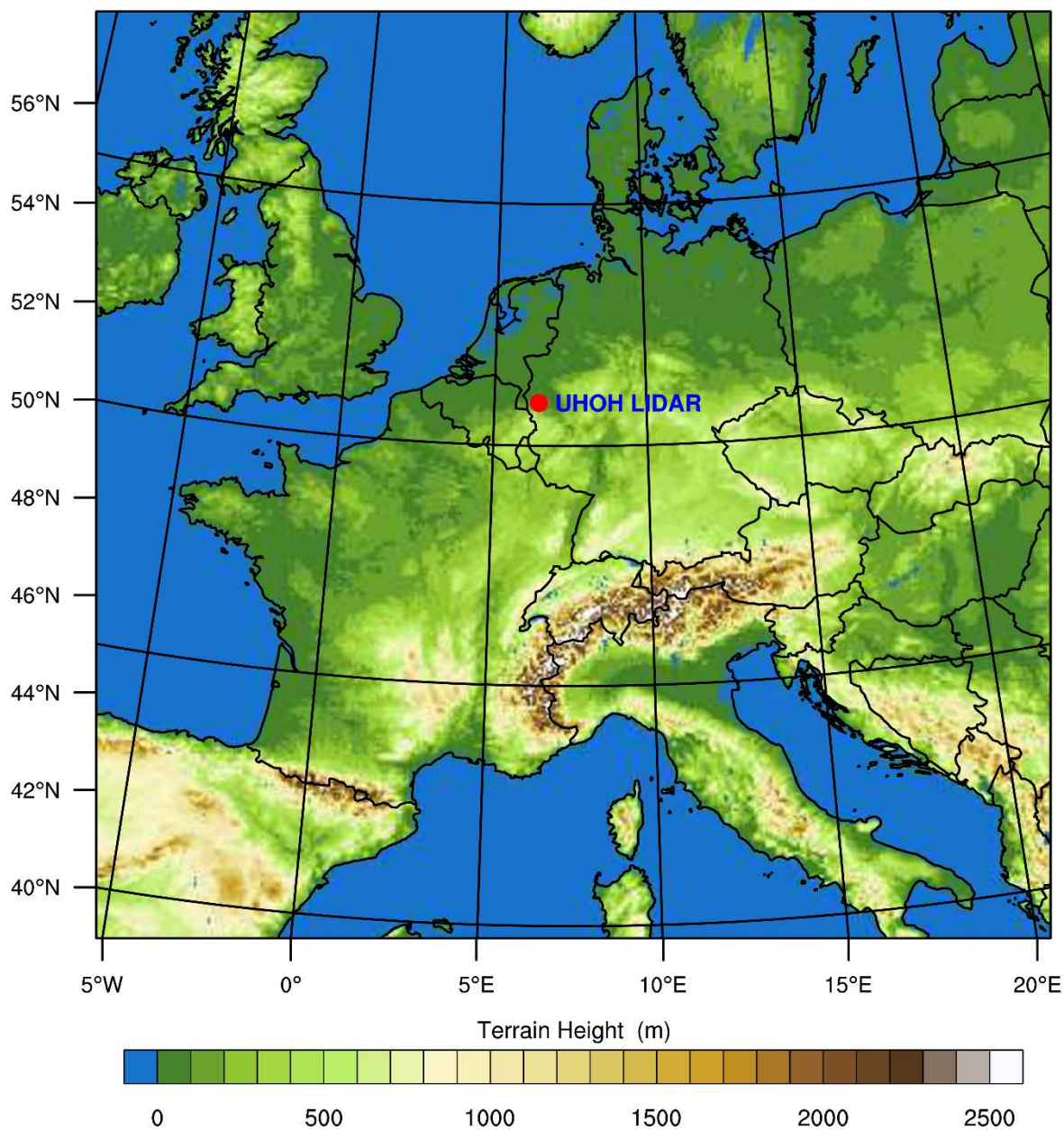
1306

1307 Fig. 11. WVMR RMSE of the analyses compared to local radiosonde data not assimilated  
1308 into the model together with assimilated WVDIAL observations. (a) Comparison of the  
1309 RMSE at the four assimilation time-steps (09, 11, 13, 15 UTC) with respect to the  
1310 radiosonde data and (b) comparison of the RMSE with respect to the WVDIAL observations  
1311 at the 10 assimilation time-steps from 09 UTC to 18 UTC 24 April 2013. (c) and (d) compare  
1312 the overall WVMR RMSE for the corresponding time-steps for (a) and (b), respectively. (e)  
1313 and (f) depict the relative change in the average RMSE of (c) and (d) respectively,  
1314 compared to the RMSE of CONV\_DA.

1315

1316 Fig. 12. Analysis of the difference between QT\_DA and CONV\_DA at (a) 09 UTC and (b) 18  
1317 UTC 24 April 2013; (c) shows the vertical cross section of the difference, valid at 09 UTC;  
1318 (d) is the six-hour forecast difference between QT\_DA and CONV\_DA initiated from 18  
1319 UTC. The spatial distributions are valid at a height of 2000 m ASL.

1320



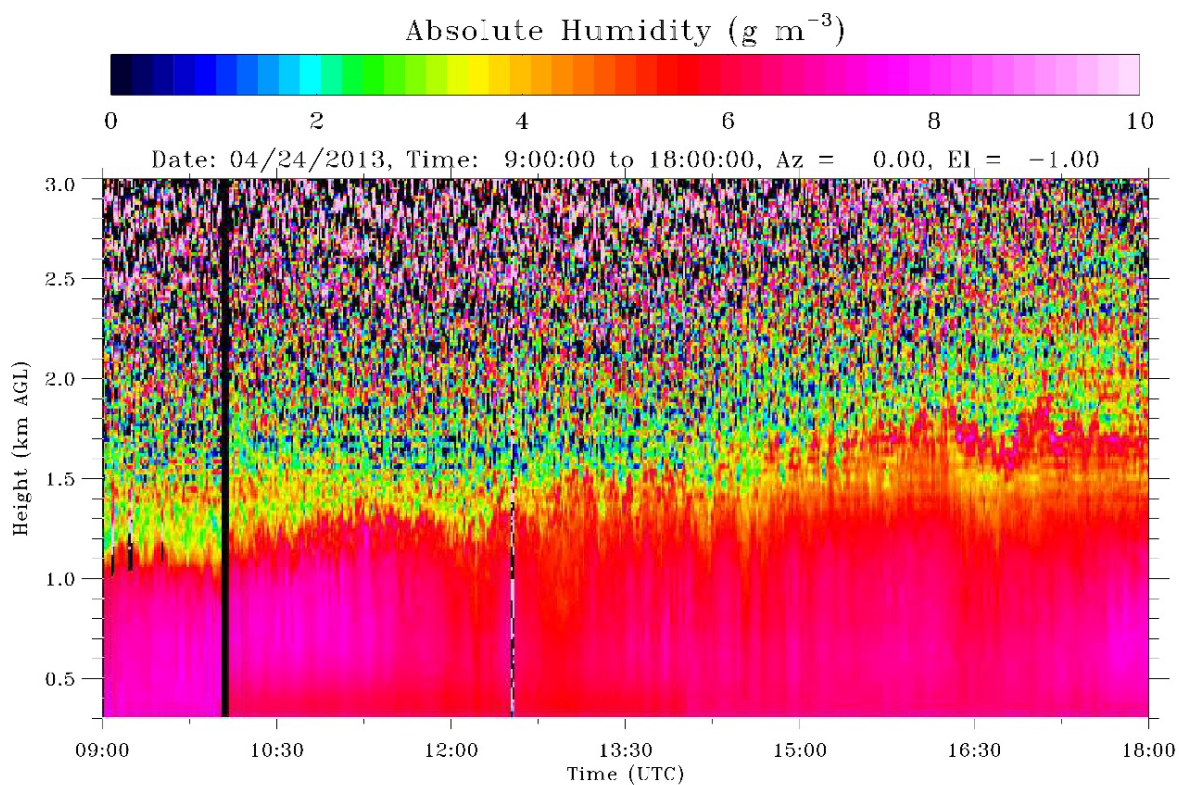
1322

1323

1324

1325

Fig. 1. The WRF model domain at a horizontal resolution of 2.5 km with orography and the location of the TRL and WVDIAL of UHOH during the HOPE campaign.



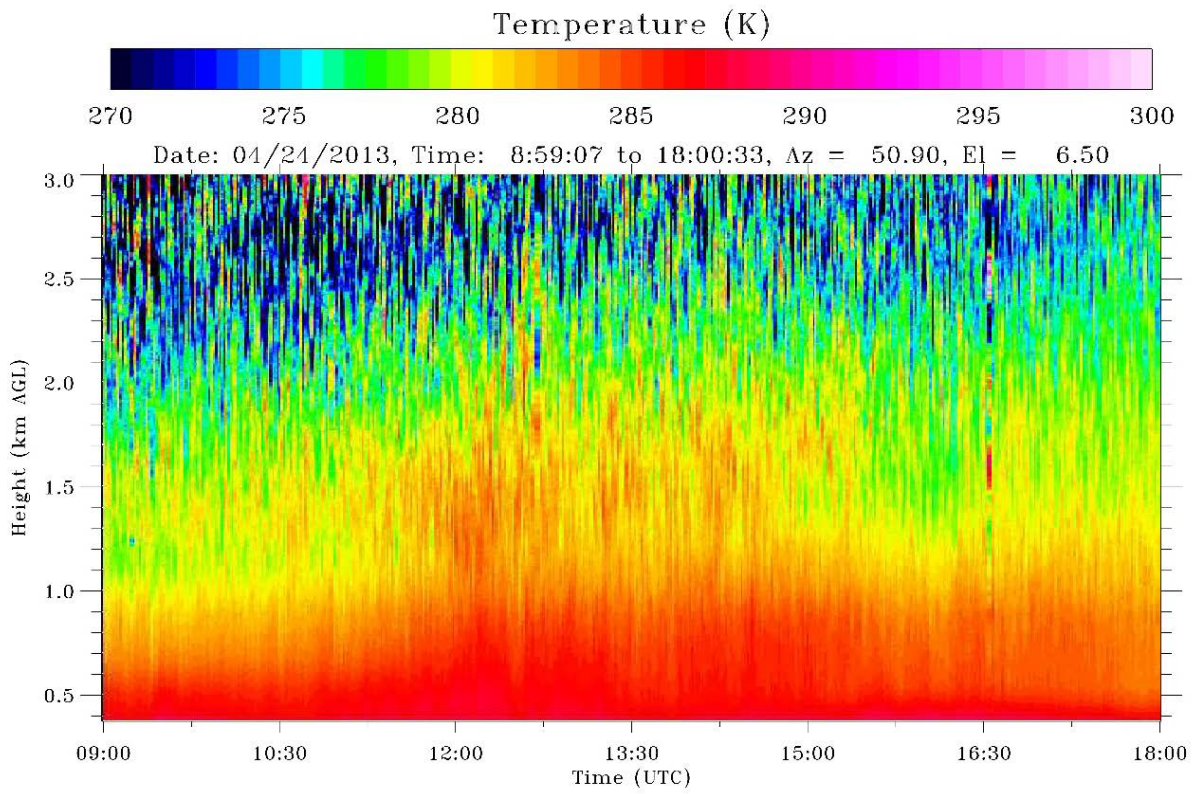
1327

1328

1329

1330

Fig. 2. Absolute humidity time series from the WVDIAL with a vertical resolution of 15 m and a temporal resolution of 60 s between 09 UTC and 18 UTC on 24 April 2013.



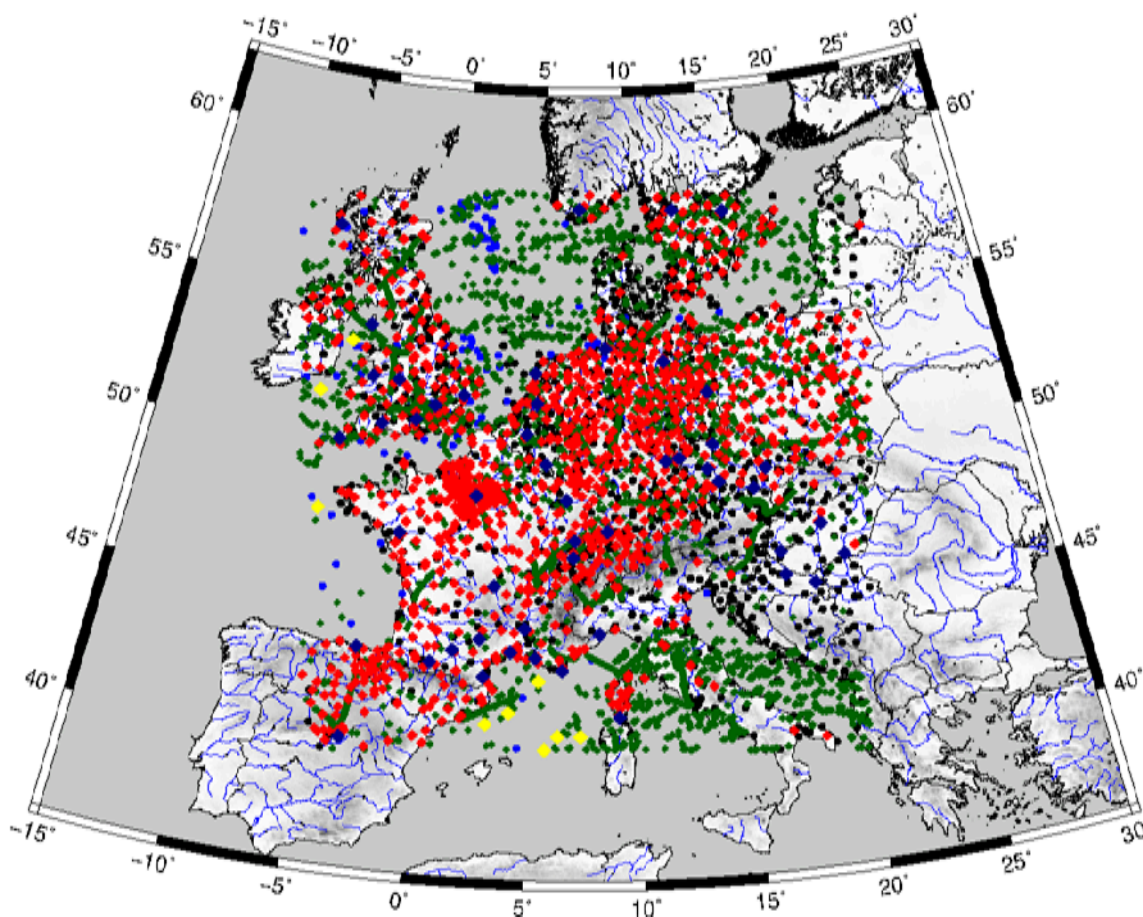
1331

1332 Fig. 3. Temperature time series from the TRL with a vertical resolution of 3.75 m and a  
1333 temporal resolution of 60 s between 09 UTC and 18 UTC on 24 April 2013.

1334



1335



1336

1337

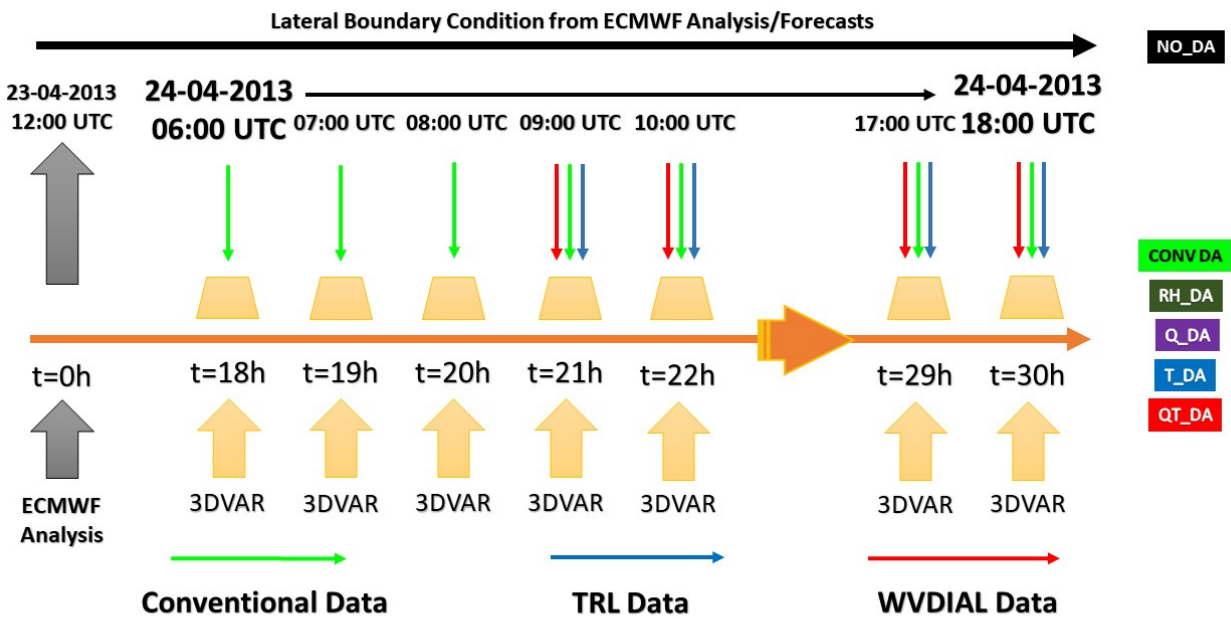
1338

1339

1340

1341

Fig. 4. Observation types and their locations for the assimilation time-step 09 UTC 24 April 2013. Black: surface stations (SYNOP+METAR), blue: ship observations (SHIP), green: aircraft observations and atmospheric motion vectors from satellite (AMDAR+SATOB), red: GPS zenith total delay, yellow: radiosondes (TEMP), and brown: wind profiler (PROFL).

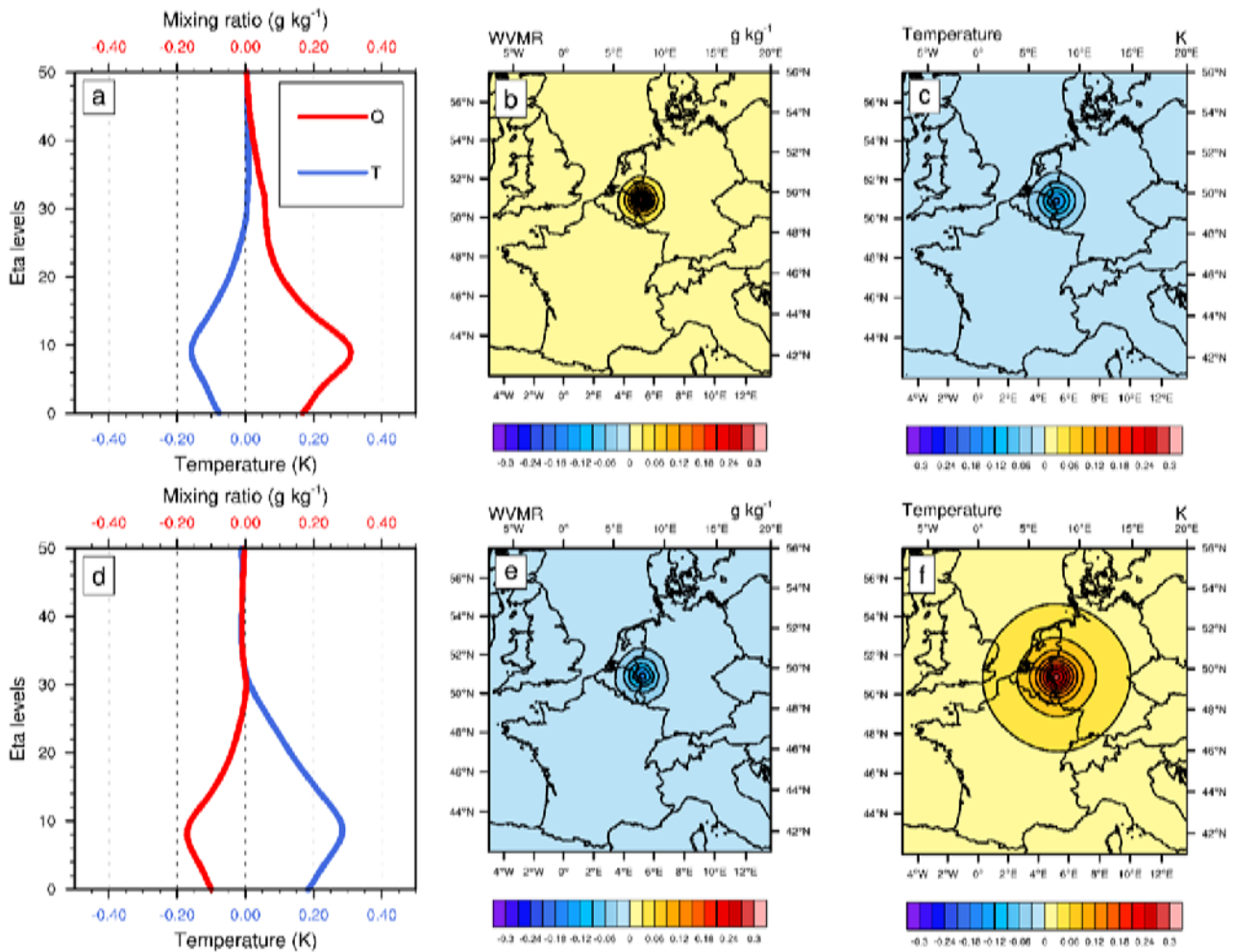


1343

1344 Fig. 5. Schematic of the 3DVAR rapid update cycle initialized from the ECMWF analysis. A  
 1345 spin-up of 18 hours was performed until 06 UTC on 24 April 2013. Five experiments with  
 1346 different setups were performed. NO\_DA (black) is the run with no data assimilation,  
 1347 CONV\_DA (green) is the control run assimilating conventional data from 06 UTC to 18 UTC,  
 1348 RH\_DA (olive green) is the assimilation with WVDIAL and conventional data from 09 UTC  
 1349 to 18 UTC using the RH operator, T\_DA (blue) is the assimilation with TRL and  
 1350 conventional data from 09 UTC to 18 UTC, Q\_DA (dark purple) is the assimilation with  
 1351 WVDIAL and conventional data from 09 UTC to 18 UTC using the TDLIDAR operator, and  
 1352 QT\_DA (red) is the assimilation with WVDIAL, TRL, and conventional data from 09 UTC to  
 1353 18 UTC using the TDLIDAR operator.

1354

1355

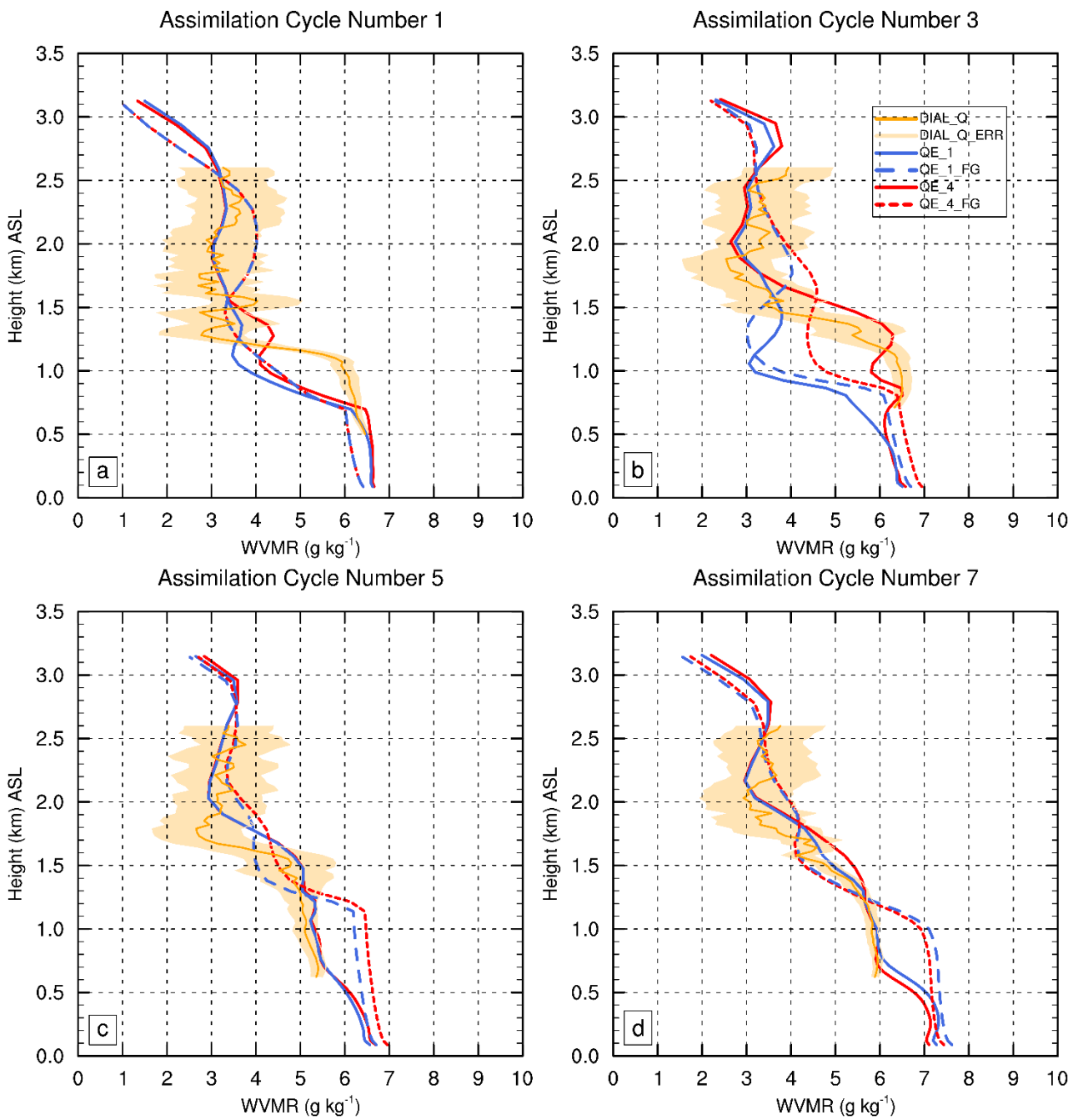


1356  
 1357  
 1358  
 1359  
 1360  
 1361  
 1362

Fig. 6. Vertical profiles and spatial distribution of analysis increments from single observation tests (SOTs) performed for a WVMR increment of  $1 \text{ g kg}^{-1}$  and 1-K temperature increment at model level 10 (255 m AGL). (a) Vertical profile, (b) and (c) spatial distribution of the analysis increments resulting from the WVMR SOT. (c), (e) and (f) results of the temperature SOT.

1363

1364



1365

1366

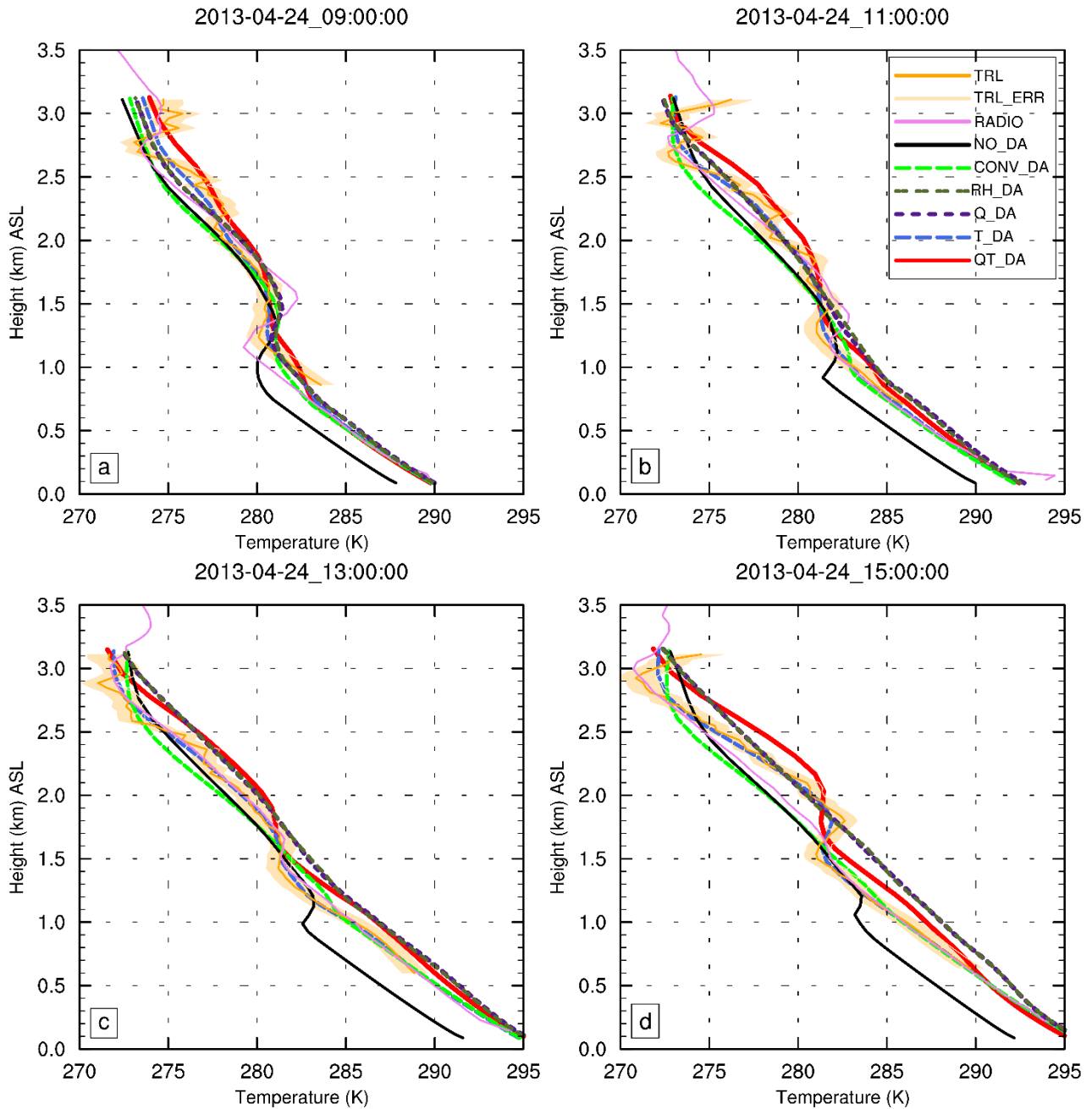
1367

1368

1369

1370

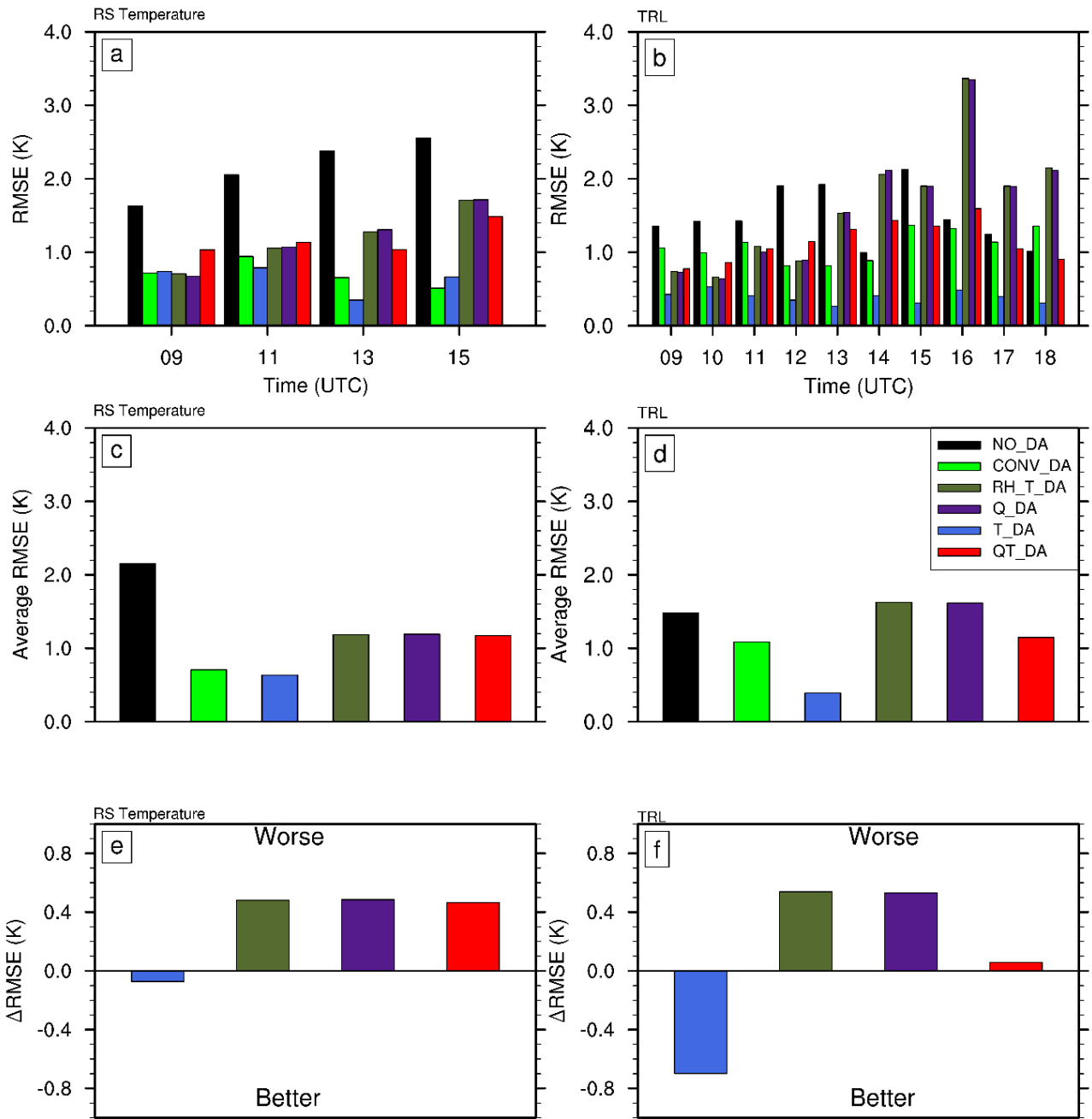
Fig. 7. Vertical profiles of the WVMR from 09 UTC, 11 UTC, 13 UTC, and 15 UTC on 24 April 2013 for the QE1 and QE4 experiments along with WVDIAL observations and associated error bars. The solid line represents the analysis profile and the dashed line the background profile.



1372

1373 Fig. 8. Temperature profiles of TRL, radiosondes, and analyses at (a) 09 UTC, (b) 11 UTC,  
 1374 (c) 13 UTC, and (d) 15 UTC. The TRL observations (orange) along with their total errors  
 1375 shown by error bars are plotted up to 3000 m AGL. Radiosonde observations (violet) which  
 1376 were not assimilated are plotted for reference. Black: NO\_DA, green: CONV\_DA, olive  
 1377 green: RH\_DA, dark purple: Q\_DA, blue: T\_DA, and red: QT\_DA.

1378



1380

1381

1382

1383

1384

1385

1386

1387

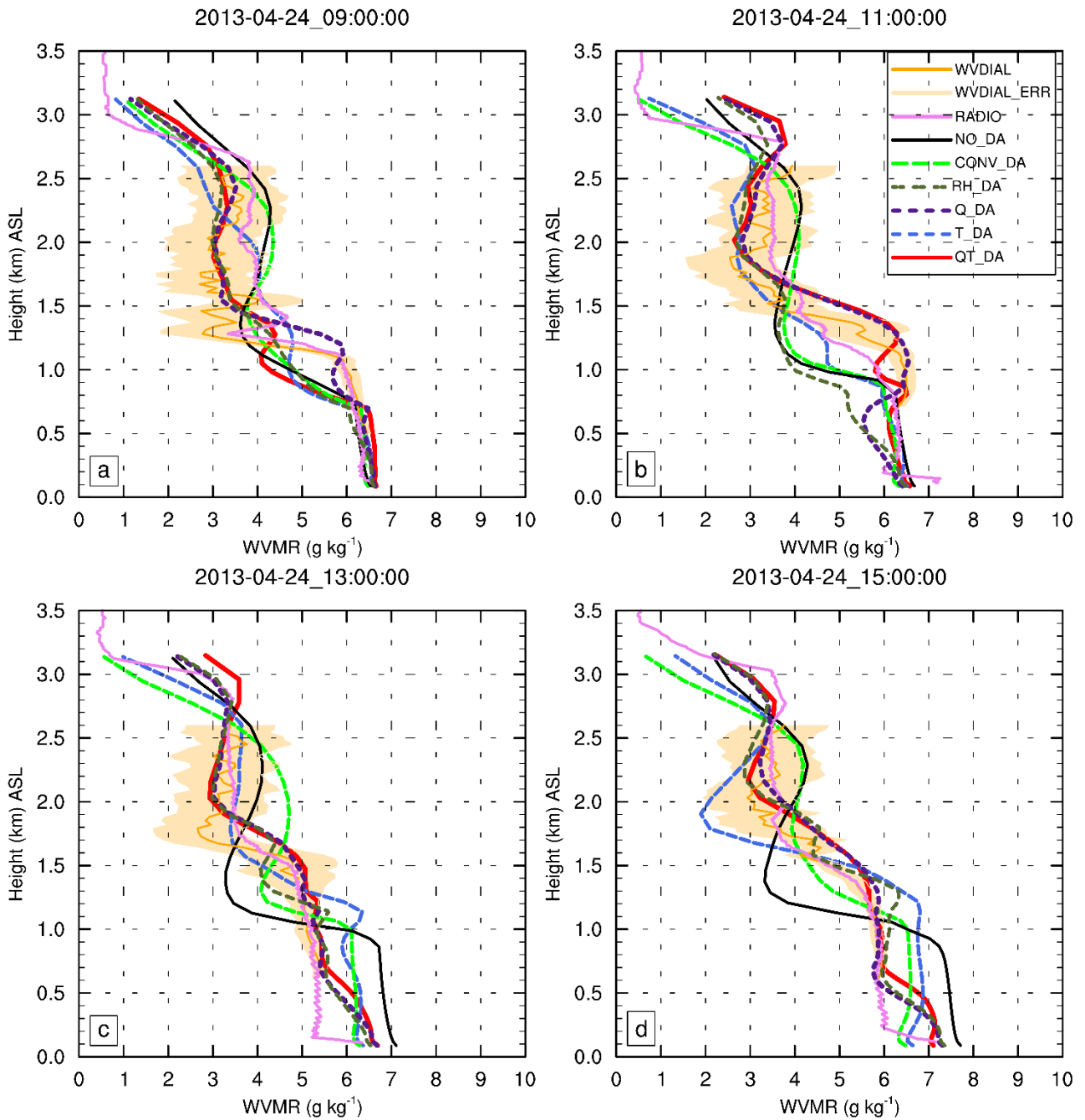
1388

1389

Fig. 9. Temperature RMSE of the analyses compared to local radiosonde data not assimilated into the model together with assimilated TRL observations. (a) Comparison of the RMSE at the four assimilation time-steps (09, 11, 13, 15 UTC) with respect to the radiosonde data and (b) comparison of the RMSE with respect to the TRL observations at the 10 assimilation time-steps from 09 UTC to 18 UTC 24 April 2013. (c) and (d) comparison of the overall temperature RMSE for the corresponding time-steps for (a) and (b), respectively. (e) and (f) depict the relative change in the average RMSE of (c) and (d), respectively, compared to the RMSE of CONV\_DA.

1390

1391



1392

1393

1394

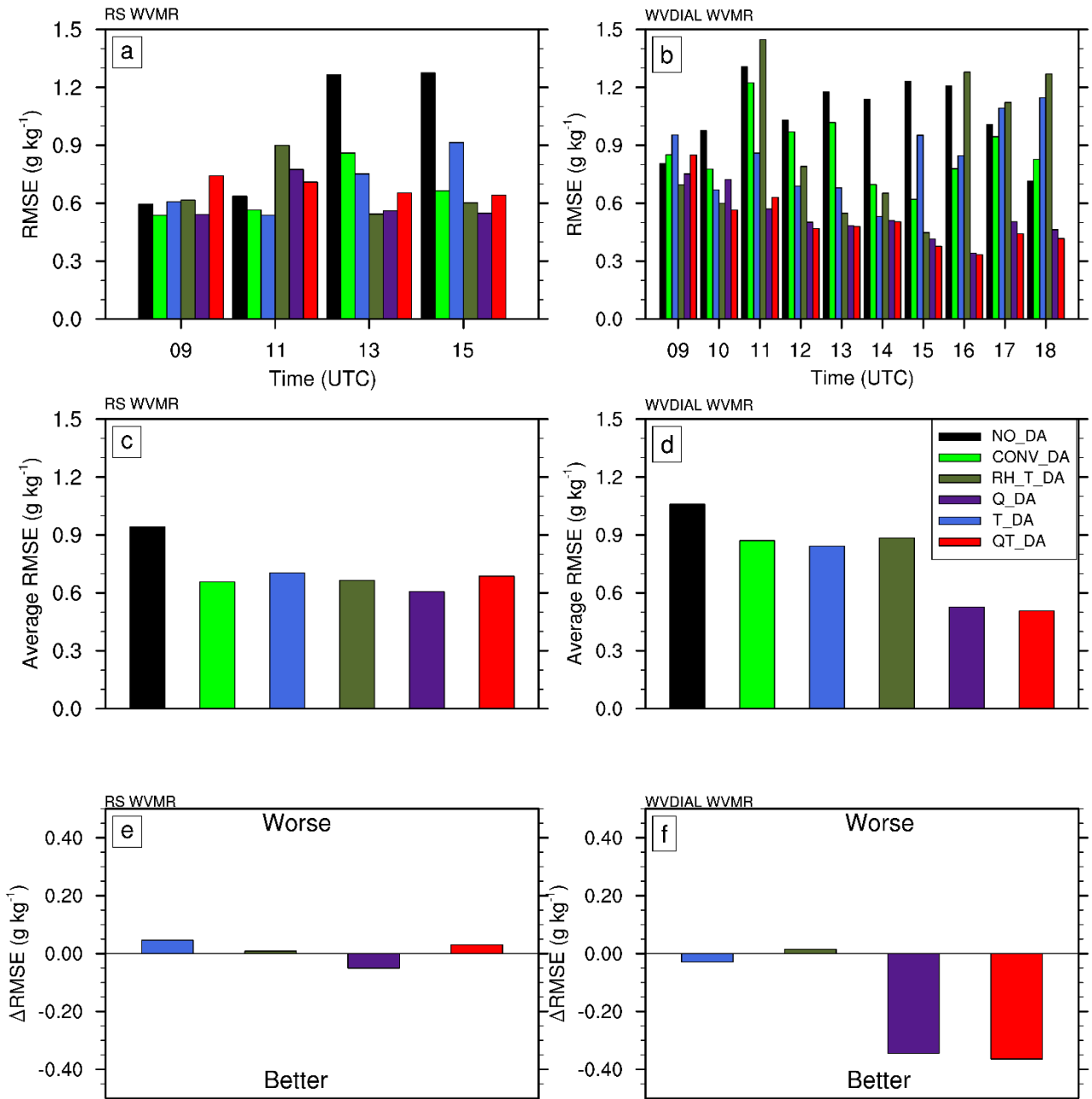
1395

1396

1397

1398

Fig. 10. WVMR profiles of WVDIAL, radiosondes, and analyses at (a) 09 UTC, (b) 11 UTC, (c) 13 UTC, and (d) 15 UTC. The WVDIAL observations (orange) along with their total errors shown by error bars are plotted up to 2500 m AGL. Radiosonde observations (violet) which were not assimilated are plotted for reference. Black: NO\_DA, green: CONV\_DA, olive green: RH\_DA, dark purple: Q\_DA, blue: T\_DA, and red: QT\_DA are shown.

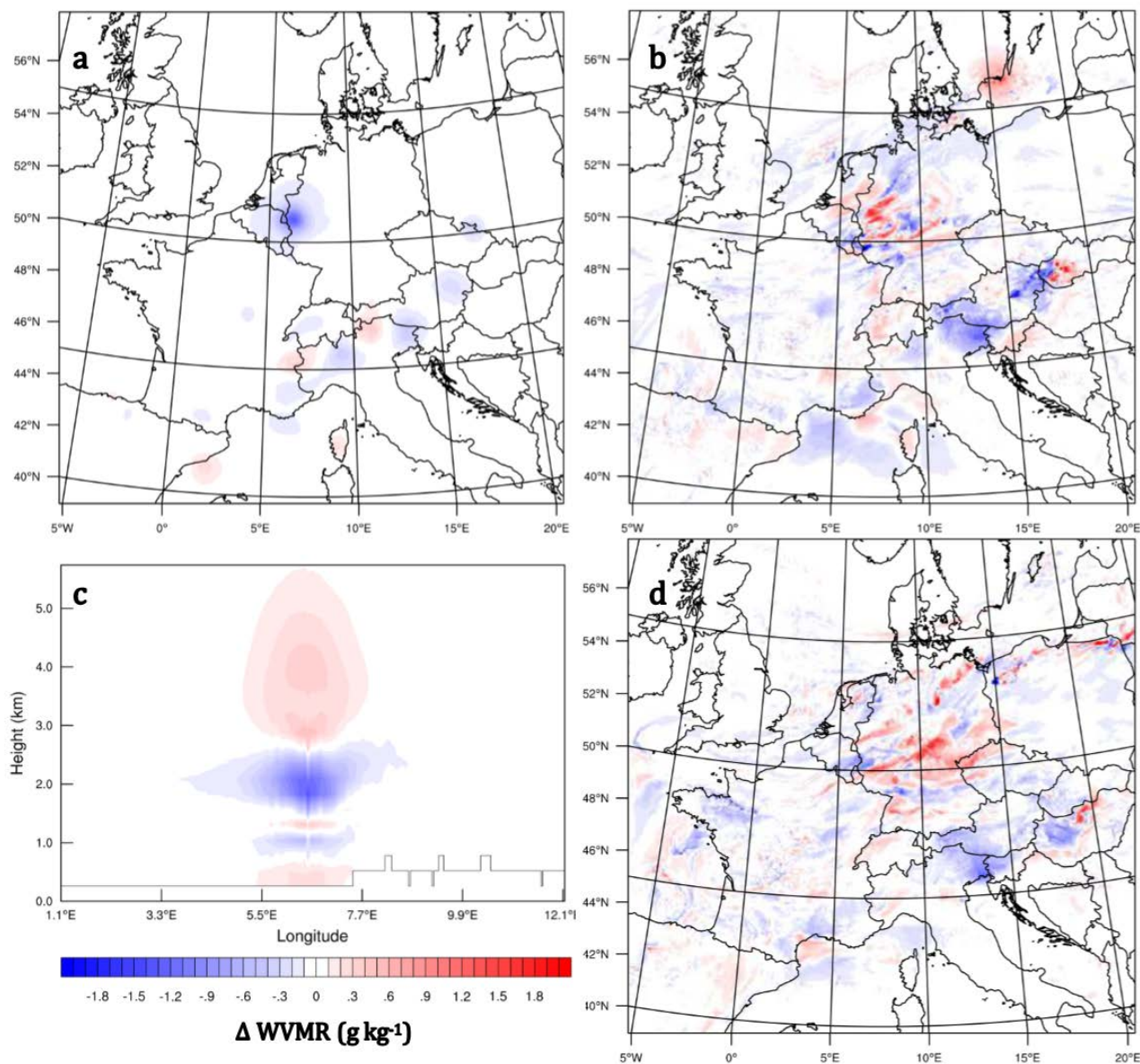


1400

1401 Fig. 11. WVMR RMSE of the analyses compared to local radiosonde data not assimilated  
 1402 into the model together with assimilated WVDIAL observations. (a) Comparison of the  
 1403 RMSE at the four assimilation time-steps (09, 11, 13, 15 UTC) with respect to the  
 1404 radiosonde data and (b) comparison of the RMSE with respect to the WVDIAL observations  
 1405 at the 10 assimilation time-steps from 09 UTC to 18 UTC 24 April 2013. (c) and (d) compare  
 1406 the overall WVMR RMSE for the corresponding time-steps for (a) and (b), respectively. (e)  
 1407 and (f) depict the relative change in the average RMSE of (c) and (d) respectively,  
 1408 compared to the RMSE of CONV\_DA.

1409





1411

1412 Fig. 12. Analysis of the difference between QT\_DA and CONV\_DA at (a) 09 UTC and (b) 18  
 1413 UTC 24 April 2013; (c) shows the vertical cross section of the difference, valid at 09 UTC;  
 1414 (d) is the six-hour forecast difference between QT\_DA and CONV\_DA initiated from 18  
 1415 UTC. The spatial distributions are valid at a height of 2000 m ASL.