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The DOI for this manuscript is

DOI:10.2151/jmsj.2020-059

J-STAGE Advance published date: August 3rd 2020

The final manuscript after publication will replace the preliminary version at the above DOI once it is available.

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# Marine Low Clouds and Their Parameterization in Climate Models

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January 24, 2020

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## Abstract

This review paper aims to provide readers with a broad range of meteorological backgrounds with basic information on marine low clouds and the concept of their parameterizations used in global climate models. The first part of the paper presents basic information on marine low clouds and their importance in climate simulations in a comprehensible way. It covers the global distribution and important physical processes related to the clouds, typical examples of observational and modeling studies of such clouds, and the considerable importance of changes in low cloud for climate simulations. In the latter half of the paper, the concept of cloud parameterizations that determine cloud fraction and cloud water content in global climate models, which is sometimes called cloud “macrophysics”, is introduced. In the parameterizations, the key element is how to assume or determine the inhomogeneity of water vapor and cloud water content in model grid boxes whose size is several tens to several hundreds of kilometers. Challenges related to cloud representation in such models that must be tackled in the next couple of decades are discussed.

**Keywords** low cloud; climate model; cloud parameterization; climate change

## 51 **1. Introduction**

52 Marine low clouds (MLCs), or marine boundary layer clouds (MBLCs), are low-level  
53 clouds prevalent over the ocean. Optically thick MLCs typically prevail over oceans with low  
54 sea surface temperature (SST) and high lower-tropospheric stability (e.g., Klein and  
55 Hartmann 1993). Although they are not associated with heavy rain or strong wind, MLCs  
56 are important for the global radiation budget because of their large shortwave radiative  
57 effects. Recent studies have shown that uncertainties in predicted temperature increases in  
58 global warming simulations can be mainly attributed to the representation of MLCs in global  
59 climate models (GCMs) (e.g., Stephens 2005, Bony and Dufresne 2005, Bony et al. 2006,  
60 Boucher et al. 2013, Zelinka et al. 2020).

61 The purpose of this review paper is to provide fundamental knowledge of low clouds and  
62 their parameterizations in GCMs to readers with a wide variety of meteorological  
63 backgrounds, rather than providing experts in this area with a summary of recent related  
64 studies. An introduction to marine low clouds, including their global distribution and  
65 important physical processes related to the clouds, is given in Section 2. Some  
66 observational and modeling studies of these clouds are introduced in Section 3. The  
67 importance of low cloud change on climate simulations is then introduced in Section 4.

68 For climate simulations, we need global atmospheric models coupled with ocean models.  
69 However, because the model grid boxes are generally several tens to several hundreds of  
70 kilometers in size, the models need a cloud parameterization that represents the

71 subgrid-scale inhomogeneity of clouds and humidity (and temperature). This is often  
72 termed cloud macrophysics and the main purpose is to determine the cloud fraction and  
73 cloud water content of the model grid cells. The latter half of this paper provides a basic  
74 review of such parameterizations and discussions of some difficulties related to the  
75 representation of clouds in GCMs (Section 5). Although turbulence schemes, schemes for  
76 shallow convection, and cloud microphysics also affect the representation of marine low  
77 clouds in GCMs, they are beyond the scope of this review paper. In Section 6, other topics  
78 that exert significant influences on climate simulations are briefly introduced, including the  
79 difficulties and uncertainty in representing cloud phase and aerosol–cloud interactions in  
80 GCMs. Sections 5 and 6 would be useful for those who wish to tackle cloud  
81 parameterizations in GCMs or those who are not modelers but who analyze cloud data  
82 from climate simulations such as the Coupled Model Intercomparison Project (CMIP)  
83 (Meehl et al. 2000).

84

85

## 86 **2. Brief Overview of Marine Low Clouds**

87 The characteristics of MLCs are completely different from mid-level clouds or high-level  
88 clouds. Typically, low-level approximately refers to 700 hPa or lower, high-level to 400 hPa  
89 or higher, and mid-level to the intermediate heights (e.g., Rossow and Schiffer 1999). Mid-  
90 and high-level clouds are often associated with deep convection or the warm front of

91 extra-tropical cyclones, where updrafts play an important role in condensing water vapor  
92 into clouds. On the other hand, optically thick MLCs typically form under high pressure  
93 systems, accompanied by the subsidence of air, for example under subtropical high  
94 pressure systems and the Okhotsk high pressure system. While mid- and high-level clouds  
95 climatologically tend to develop over areas with high SST, MLCs typically occur over the  
96 ocean where SST is low. In contrast to mid- and high-level clouds, which are often  
97 associated with precipitation, MLCs typically generate either no precipitation or only drizzle.  
98 Therefore, the roles of mid- and high-level clouds and MLCs in the Earth's atmosphere are  
99 entirely different. While deep clouds, which are accompanied by precipitation, heat or cool  
100 the surrounding atmosphere through latent heat release or evaporative cooling (e.g.,  
101 Houze 1982, 2004, Shige et al. 2004, Sui et al. 2020), MLCs, especially stratus and  
102 stratocumulus, mainly exert an influence through the radiative effect, which is discussed in  
103 Section 2.2.

104

### 105 *2.1 Global Distribution of MLCs*

106 An image of MLCs over the subtropical north eastern Pacific (an area renowned for the  
107 frequent occurrence of MLCs and a clear transition of MLC regimes) is shown in Fig. 1. The  
108 visible image was taken by the Moderate Resolution Imaging Spectroradiometer (MODIS).  
109 Flat and homogeneous clouds off the coast of California are stratus. A transition of MLC  
110 regimes from stratus to stratocumulus, which has a clear meso-scale structure (Wood

111 2012), is observed in a west-southwestward direction. Farther west-southwestward, the  
112 MLC regime eventually changes from stratocumulus to cumulus, where cloud amount is  
113 much smaller than in areas dominated by stratus and stratocumulus; note that cloud  
114 amount or cloud cover is defined as the proportion of cloud covering an area. As clearly  
115 shown in Fig. 1, MLCs such as marine stratus and stratocumulus are characterized by high  
116 albedo.

117 Such optically thick MLCs generally prevail over the subtropics and parts of the tropics off  
118 the west coast of continents. Klein and Hartmann (1993) reported the global distribution of  
119 low stratiform cloud, which consists of stratus, stratocumulus, and sky-obscuring fog (Fig.  
120 2). It is clear from the figure that boundary layer stratiform cloud amount is very large over  
121 the subtropical oceans off California, Peru, Namibia, and Mauritania. This study also found  
122 that Lower Tropospheric Stability (LTS), defined as the difference in potential temperature  
123 between 700 hPa and the surface, has a high correlation with boundary layer stratiform  
124 cloud amount and the global distribution of LTS corresponds closely to that of stratiform  
125 clouds. High stability over subtropical oceans off the west coast of continents is attributed to  
126 the fact that SST is low in those areas compared with other oceans at similar latitudes,  
127 although air temperature at 700 hPa is approximately uniform zonally (Fig. 3). The low SST  
128 is caused by horizontal cold advection from higher latitudes driven by subtropical gyre with  
129 the eastern boundary current (e.g., Colling 2001). Coastal upwelling of cold water also  
130 contributes to the low SST, especially near the coast. The physical mechanism for the high

131 correlation between low cloud amount and stability is explained in Section 2.3.

132

## 133 *2.2 Importance of MLCs in Climate and Weather*

134 MLCs, including stratus and stratocumulus, are one of the most important cloud  
135 contributors to the global radiation budget because of their large shortwave radiative effects  
136 (e.g., Klein and Hartmann 1993). MLCs in the subtropics are especially important because  
137 solar insolation is relatively large in these regions compared with the mid or high latitudes.  
138 MLCs exert a significant control on global average temperature because of their significant  
139 influence on global albedo.

140 However, a realistic representation of marine stratocumulus clouds off the west coast of  
141 continents in global climate models (GCMs) has been a major issue in climate modeling for  
142 a long time (e.g., Duynkerke and Teixeira 2001, Siebesma et al. 2004). Current GCMs still  
143 have some deficiencies in representing subtropical marine stratocumulus clouds off the  
144 west coast of continents compared with observations (e.g., Nam et al. 2012, Caldwell et al.  
145 2013, Su et al. 2013, Koshiro et al. 2018). Lauer and Hamilton (2013) showed that total  
146 cloud cover simulated in CMIP3 and CMIP5 multi-models is significantly underestimated  
147 over subtropical stratocumulus regions and there are large biases in shortwave cloud  
148 radiative effect over these regions (Fig. 4); these biases are astonishingly similar in the  
149 CMIP3 and CMIP5 multi-model means. Overestimates of SST of ~5 K off the west coast of  
150 continents are possible in ocean–atmosphere coupled models partly due to the poor



151 representation of marine stratocumulus over these areas (e.g., Ma et al. 1996, Duynkerke  
152 and Teixeira 2001).

153 In fact, there are two kinds of importance associated with MLCs from a climate  
154 perspective. One is related to the representation of the present climate system as  
155 described above. The SST bias over areas with frequent MLC cover is a serious problem  
156 not just because it affects local SST. It can deteriorate the representation of the ocean  
157 general circulation, because, for instance, strong stabilization of the ocean occurs over  
158 areas with coastal upwelling. This would exert a major influence on the representation of  
159 the global climate system. The other importance associated with MLCs is related to climate  
160 change simulations. This issue, which is a hot topic whose importance has become evident  
161 since the 2000s, is explained in detail in Section 4.

162 Although they do not bring heavy rain or strong wind, MLCs are important not only for  
163 global climate systems but also for local and short-lived phenomena. A typical phenomenon  
164 that occurs in and around Japan is the Yamase cloud event in which MLCs accompany the  
165 Yamase winds (e.g., Kodama 1997, Kodama et al. 2009, Koseki et al. 2012, Shimada et al.  
166 2014). When the Okhotsk high pressure system appears in summer, it causes northeasterly  
167 winds along the Pacific coast of the Tohoku region. Stratocumulus is formed off Tohoku  
168 under northeasterly winds (e.g., Shimada and Iwasaki 2015) and is continually advected  
169 over coastal areas (Fig. 5; e.g., Eguchi et al. 2014). The temperature in the area decreases  
170 dramatically due to the blocking of solar insolation in addition to cool air advection from the

171 ocean. Until a few hundred years ago, large numbers of people even starved to death  
172 because of poor crop harvests caused by low temperatures. However, MLCs related to  
173 Yamase are also difficult to reproduce in atmospheric models, including numerical weather  
174 prediction (NWP) models.

175 In the next section, the reasons for the difficulty in reproducing MLCs realistically in  
176 atmospheric models are explained.

177

### 178 *2.3 Mechanisms for the Formation and Maintenance of MLCs*

179 While condensation due to the upward motion of an air mass is a primary factor in  
180 producing mid- and high-level clouds, MLCs are formed and maintained by a subtle  
181 balance between complicated physical processes (e.g., Duynkerke and Teixeira 2001,  
182 Wood 2012). Figure 6 shows a schematic diagram (modified from fig. 2 in de Roode and  
183 Duynkerke 1997) of the complicated physical processes that affect MLCs. For instance, the  
184 right edge of the figure might correspond to an area adjacent to California (Peru) where  
185 SST is lower, and the left edge to an area near Hawaii (far west of Peru) where SST is  
186 higher.

187 Subtropical high pressure systems over subtropical oceans are accompanied by  
188 subsidence in the free atmosphere. Subsidence generates a temperature inversion at the  
189 top of the boundary layer, which is very strong when SST is relatively low (near the right  
190 edge of Fig. 6). Stability is extremely high at the inversion layer, and the inversion prevents

191 water vapor from escaping into the free atmosphere. Therefore, water vapor is confined in  
192 the boundary layer and condenses into clouds. Because stratus and stratocumulus clouds  
193 have high optical thickness and strong cloud top cooling, longwave radiative cooling plays  
194 an important role in developing and maintaining the cloud layer. The strong cloud top  
195 cooling destabilizes the boundary layer just below the inversion, promotes water vapor  
196 transport from the sea surface, and maintains the well-mixed layer and cloud layer. It can  
197 even strengthen the temperature inversion just above the cloud top.

198 The temperature inversion is weaker in areas where SST is higher by several degrees.  
199 Cloud top entrainment occurs in these areas, which is the process of taking dry and warm  
200 air into the mixed layer from the free atmosphere. Figure 7 shows a schematic illustration of  
201 cloud top entrainment (Randall 1980, Yamaguchi and Randall 2008). When a dry and warm  
202 air parcel enters the cloud layer from the free atmosphere, cloud water evaporates into the  
203 dry parcel and the temperature of the parcel is lowered. If the decrease of temperature is  
204 large enough to overcome the temperature gap (inversion) at the top of the cloud layer, the  
205 parcel can have negative buoyancy. In this case, dry and warm air can continuously intrude  
206 into the mixed layer. A weaker temperature inversion and/or larger gap of humidity at the  
207 cloud top are more favorable for cloud top entrainment. Drying of the mixed layer due to  
208 cloud top entrainment contributes to the break-up of the cloud layer (Deardorff 1980,  
209 Randall 1980). The cloud top entrainment and the role have been discussed based on  
210 observational or modeling studies by many researchers since the concept was proposed

211 (e.g., Kuo and Schubert 1988, Betts and Boers 1990, MacVean and Mason 1990, MacVean  
212 1993, Yamaguchi and Randall 2008, Lock 2009, Noda et al. 2013). In addition, higher SST  
213 causes shallow convection, which is observed as cumulus (e.g., Chung et al. 2012).  
214 Shallow convection forms a decoupled layer above the lifting condensation level that  
215 suppresses upward turbulent transport of water vapor to an upper part of a boundary layer  
216 (e.g., Sandu and Stevens 2011, de Roode et al. 2016), and they vent water vapor in the  
217 boundary layer to the free atmosphere (e.g., Stull 1988). Active shallow convection is more  
218 efficient at suppressing optically thick stratocumulus occurrence when SST is higher.

219 Thus, stratus and stratocumulus prevail in subtropical oceans adjacent to the west coast  
220 of continents, gradually break up westward, and disappear far from these landmasses (see  
221 Fig. 1). The cloud regimes change from solid stratus to stratocumulus to closed-cell  
222 convection, open-cell convection, and then scattered cumulus as SST increases with  
223 increasing distance from the coast. As explained above, the temperature inversion is an  
224 important factor controlling MLCs. The high correlation between low cloud amount and LTS  
225 (Section 2.1) is attributed to the high correlation between low cloud amount and  
226 temperature inversion strength, because there must be a correlation between LTS and  
227 temperature inversion strength. Wood and Bretherton (2006) modified LTS and developed  
228 a more sophisticated index, estimated inversion strength (EIS), which estimates the  
229 temperature inversion strength at the top of a mixed layer from LTS, assuming a moist  
230 adiabatic lapse rate in a free atmosphere. They showed that the correlation of low cloud

231 amount with EIS is even higher than with LTS. Subsequently, Kawai et al. (2017) developed  
232 an index for low cloud amount, the estimated cloud-top entrainment index (ECTEI), which is  
233 a modification of EIS that considers the effect of cloud top entrainment. Figure 8 shows the  
234 relationships between low cloud amount and the stability indexes, LTS, EIS, and ECTEI. It  
235 shows that ECTEI has the best correlation with low cloud amount among the three indices,  
236 although EIS also has a high correlation.

237 There are clear diurnal variations in cloud amount and the liquid water path of stratus and  
238 stratocumulus, which reach a maximum in the early morning and a minimum in the early  
239 afternoon (e.g., Blaskovic et al. 1991, Albrecht et al. 1995, Rozendaal et al. 1995,  
240 Duynderke and Teixeira 2001, de Szoeker et al. 2012, Burleyson et al. 2013); an example is  
241 shown in Fig. 9 below. During the daytime, solar insolation heats the cloud layer. Shortwave  
242 heating reduces net radiative cooling and weakens water vapor transport. In addition,  
243 shortwave radiation penetrates the cloud layer to some extent and heats the inside of the  
244 cloud layer, while longwave cooling only occurs several tens of meters from the cloud top.  
245 The difference in the heating and cooling heights causes decoupling of the mixed layer and  
246 prevents water vapor transport (e.g., Betts 1990, Blaskovic et al. 1991). The interactions of  
247 the related physical processes are even more complicated. For example, condensation of  
248 water vapor heats the inside of the cloud layer, longwave radiation from the sea surface  
249 heats the cloud base, and evaporation of drizzle cools the air below the cloud base. All of  
250 these processes affect the vertical profile of the cloud-topped boundary layer. Various

251 physical processes that control MLCs and their complicated interactions are discussed in  
252 more detail in some review papers (e.g., Wood 2012, Nuijens and Siebesma 2019).

253 However, despite this complexity, the vertical resolution of GCMs is fairly low, and the  
254 thickness of model layers around the top of a mixed layer or cloud top of MLCs is 200–300  
255 m, while the observed thickness of MLCs can be as small as 50 m during the daytime (Betts  
256 1990, Duynkerke and Teixeira 2001). The lack of vertical resolution in GCMs is one of the  
257 major causes of the difficulty in reproducing MLCs, and the complicated physical  
258 interactions related to MLCs are extremely difficult to represent appropriately in current  
259 GCMs.

260

### 261 **3. Observational and Modeling Studies**

262 There are two methods for investigating MLCs. One is to obtain information from  
263 observational data, such as shipboard observations, satellite data, and field campaign data  
264 (including aircraft data). Another is to use models, including cloud resolving models (CRMs)  
265 and large eddy simulation (LES) models.

266

#### 267 *3.1 Observational Studies*

268 Shipboard observations (e.g., Warren et al. 1988, Hahn and Warren 2009; Eastman et al.  
269 2011) have been used to reveal the global distribution of MLCs. Although data are obtained  
270 from visual observation, and are consequently subjective to some extent, the advantages

271 are large areal coverage (almost global), a long history (>50 years), and the fact that  
272 observations are made from below the cloud base. One of the most renowned  
273 observational studies is that of Klein and Hartmann (1993) (see Section 2.1). Subsequently,  
274 Norris (1998a, b) and Norris and Klein (2000) investigated the global distribution and the  
275 characteristics of each MLC regime using shipboard observational data.

276 Satellite data have also been used for studies of MLCs. The International Satellite Cloud  
277 Climatology Project (ISCCP) (e.g., Rossow and Schiffer 1999) is a dataset obtained from  
278 satellites that is frequently used for global studies related to clouds. Clouds are classified  
279 into cloud regimes, such as stratus, stratocumulus, cumulus, cirrus, and cumulonimbus,  
280 using infrared and visible channel data from geostationary satellites. For example,  
281 controlling factors for MLCs were investigated using satellite data including ISCCP data,  
282 and the sensitivities of MLCs to meteorological parameters including EIS, SST, subsidence,  
283 and surface temperature advections were revealed (e.g., Myers and Norris 2013, Myers  
284 and Norris 2015, Myers and Norris 2016, Qu et al. 2015, Seethala et al. 2015). However,  
285 though there are many advantages in using data from geostationary satellites, including the  
286 broad spatial area, high frequency (better than every three hours), and homogeneity of the  
287 observations, estimates of the cloud top height based on infrared data have a large  
288 uncertainty (Garay et al. 2008).

289 Several field campaigns have been carried out to reveal the detailed characteristics of  
290 MLCs (see Table 1), and the findings of these studies have resulted in a better

291 understanding of the structures of MLCs and related processes. FIRE (First ISCCP  
292 Regional Experiment) was a field campaign undertaken in June and July 1987 to examine  
293 Californian coastal stratocumulus (Albrecht et al. 1988). ASTEX (the Atlantic Stratocumulus  
294 Transition Experiment) studied stratocumulus and subtropical trade cumulus over the  
295 northeast Atlantic Ocean during June 1992 (Albrecht et al. 1995). The EPIC (East Pacific  
296 Investigation of Climate) field campaign for stratocumulus off Peru was conducted in  
297 September and October of 2001 (Bretherton et al. 2004b). VOCALS-REx [the Variability of  
298 American monsoon systems (VAMOS) Ocean–Cloud–Atmosphere–Land Study Regional  
299 Experiment] was performed in October and November of 2008 to examine stratocumulus  
300 off Peru (Wood et al. 2011, Bretherton et al. 2010). A field campaign EUREC<sup>4</sup>A (Elucidate  
301 the Couplings Between Clouds, Convection and Circulation) was conducted over the  
302 tropical Atlantic Ocean in January and February 2020 to investigate the relationships  
303 between trade cumulus and the large-scale environment (Bony et al. 2017). These field  
304 campaigns used various observational methods, including ceilometers, radiosondes, sodar,  
305 and aircraft, to observe the vertical structure of MLCs in detail, including cloud top and base  
306 heights, the liquid water path, and their diurnal variations. For instance, diurnal variations in  
307 liquid water path and cloud-top and cloud-base heights observed in the field campaign  
308 FIRE during July 1987 are shown in Fig. 9 (Blaskovic et al. 1991). Clear diurnal variation in  
309 liquid water path is observed, which reaches a maximum in the early morning and a  
310 minimum in the afternoon, as discussed in Section 2.3. The diurnal variation in cloud depth



311 (the difference between cloud top and cloud base heights) is also captured, showing a  
312 minimum in the afternoon.

313

### 314 *3.2 Modeling Studies*

315 CRMs have been used in the past to understand the detailed characteristics of MLCs and  
316 the interactions of the related physical processes. LESs have been used more recently  
317 (e.g., Noda and Nakamura 2008), and have typical resolutions of 25–50 m horizontally and  
318 5–10 m vertically. The advantage of using these models is that all variables, including cloud  
319 water content, temperature, and humidity, can be obtained completely and analyzed in  
320 detail. Another advantage is that many sensitivity tests can be conducted to understand the  
321 mechanisms of interactions between a variety of physical processes. For instance,  
322 Yamaguchi and Randall (2008) investigated cloud top entrainment for a cloud-topped  
323 mixed layer in detail using LES, and revealed the contributions to cloud formation and  
324 dissipation of the temperature inversion and humidity gap at the cloud top, longwave  
325 radiative cooling, and the surface latent heat flux. Noda et al. (2014) investigated  
326 responses of marine stratocumulus to various large-scale factors using LES, and  
327 concluded that gaps of humidity and temperature at the top of a boundary layer are the  
328 most dominant factors that control stratocumulus. Lock (2009) investigated factors that  
329 influence the cloud cover of shallow cumulus clouds using LES and found that the cloud-top  
330 entrainment parameter has a high correlation with cloud cover. Several intercomparison

331 studies have evaluated the representation of MLCs in LESs. For instance, de Roode et al.  
332 (2016) showed that six LESs produced consistent simulations of the stratocumulus–  
333 cumulus transitions based on four different cases, including an example from the ASTEX  
334 field campaign. On the other hand, Sato et al. (2015) reported that the different  
335 microphysics schemes in an LES model cause significant differences in simulations of  
336 shallow cumulus. Furthermore, it has been shown that cloud cover of stratocumulus  
337 (Matheou and Teixeira 2019) and shallow cumulus (Sato et al. 2018b) simulated by LES  
338 does not converge until the vertical and horizontal resolutions of the model reach 5 m and  
339 about 10 m, respectively.

340

## 341 **4. Climate Change Studies and MLCs**

### 342 *4.1 Uncertainty in Climate Change*

343 Future climate change is one of the most important topics for climate and meteorological  
344 studies. However, there is a wide spread in predicted increases in surface temperature in  
345 global warming simulations by various climate models, and this spread has not narrowed  
346 even in recent years (e.g., Flato et al. 2013). It is widely recognized that a major part of this  
347 spread arises from large variations in cloud feedback (e.g., Soden and Held 2006, Soden et  
348 al. 2008). The term ‘cloud feedback’ is defined as a change in the radiative effects of clouds  
349 in response to an external climate perturbation, such as increased CO<sub>2</sub> [see Bony et al.  
350 (2006) for a more formal definition]. This feedback refers to the extent that changes in

351 clouds amplify or dampen a change in surface air temperature caused directly by external  
352 forcing.

353 A substantial part of the spread in cloud feedback can be attributed to variability in  
354 predictions of low clouds, which have a large shortwave radiative effect (e.g., Stephens  
355 2005, Bony et al. 2006, Zelinka et al. 2012a, 2012b, 2013, 2020). Generally speaking,  
356 increases (decreases) in low cloud cover or cloud optical thickness in future climates lead  
357 to decreases (increases) in solar insolation reaching the surface, thereby mitigating  
358 (enhancing) the temperature increase. Figure 10 shows estimates of surface temperature  
359 increase under doubled CO<sub>2</sub> concentrations from a number of models that participated in  
360 the CMIP. It also shows changes in low clouds for two models that fall at either end of the  
361 projected warming range (Stephens 2005). The Atmospheric Model version 2 (AM2) from  
362 the Geophysical Fluid Dynamics Laboratory (GFDL) and the National Center for  
363 Atmospheric Research (NCAR) Community Atmosphere Model (CAM) 2.0 have climate  
364 sensitivities of more than 4.5 K and less than 2 K, respectively. The difference in changes in  
365 low-level cloud amount in these two models is significant. A version of AM2 shows a strong  
366 decrease in subtropical low cloud, leading to albedo decreases and a positive cloud  
367 feedback, while CAM2.0 shows an increase in the low-level cloud amount and a negative  
368 feedback (Bretherton et al. 2004a). Note that positive (negative) cloud feedback  
369 corresponds to a change in cloud that amplifies (dampens) the change in surface air  
370 temperature due to external forcing.

371 Bony and Dufresne (2005) and Bony et al. (2006) divided coupled ocean–atmosphere  
372 GCMs participating in the Intergovernmental Panel on Climate Change (IPCC) Fourth  
373 Assessment Report (AR4) into two groups: those with positive cloud feedbacks over the  
374 tropics and those with negative feedbacks. They found that differences in the two groups  
375 are caused mainly by cloud regimes that form under strong subsidence, and that shortwave  
376 cloud radiative effect (CRE) rather than longwave CRE is responsible for the difference (Fig.  
377 11). This means that changes in low cloud regimes, which have high albedo, have a  
378 dominant control on cloud feedback. This result is related to the fact that changes in low  
379 cloud regimes have a large impact on the net CRE due to the large shortwave radiative  
380 effect and small longwave CRE. On the other hand, changes in deep cloud regimes have a  
381 small impact on net CRE because an increase (decrease) in deep cloud amount causes  
382 more (less) reflection of solar radiation and comparably more (less) absorption of infrared  
383 emission from the surface. This corresponds to a negative (positive) impact on shortwave  
384 CRE and a positive (negative) impact on longwave CRE so that the effects almost cancel  
385 each other out (e.g., Zelinka et al. 2012a, 2013). Consequently, changes in deep cloud  
386 regimes do not have a large influence on cloud feedback. Although thin cirrus clouds have  
387 weak positive net CRE due to larger longwave CRE (positive) than shortwave CRE  
388 (negative), actual contribution of thin clouds to cloud feedback is not dominant (e.g., Zelinka  
389 et al. 2012a, 2013). More recently, it has also been confirmed that the spread of low cloud  
390 feedback dominantly contributes to the spread of net total cloud feedback based on

391 simulation results using CMIP5 multi-models (Zelinka et al. 2013) and CMIP6 multi-models  
392 (Zelinka et al. 2020).

393 Therefore, to obtain reliable cloud feedback for low clouds and narrow the spread in the  
394 predicted increases in surface temperature, MLCs must be represented accurately in  
395 GCMs. The interactions of physical processes related to MLCs should be represented as  
396 well as possible, although it will not be easily achieved, as discussed in Section 2.3.  
397 Unfortunately, LESs cannot be used for global climate simulations due to limitations on  
398 computer resources. Although there is a remarkably pioneering study of incorporating a  
399 cloud resolving model with fine resolution (e.g., the vertical resolution is 20m and the  
400 horizontal resolution: 250m in Parishani et al. 2017) into a GCM to explicitly capture  
401 boundary layer turbulence (“ultraparameterization”: Parishani et al. 2017), the  
402 computational cost is incomparably higher than conventional GCMs. Since the only option  
403 is to use GCMs for such studies, the representation of MLCs must be improved and  
404 changes in MLCs must be represented realistically in GCMs.

405

#### 406 *4.2 Various Studies Related to Future Changes in MLCs*

407 Changes in low clouds in a warmer climate and low cloud feedback have been studied  
408 extensively in recent years, particularly with respect to tropical and subtropical low cloud. In  
409 particular, the CMIP project (CMIP5: Taylor et al. 2012, CMIP6: Eyring et al. 2016) and the  
410 Cloud Feedback Model Intercomparison Project (CFMIP2: Bony et al. 2011, CFMIP3:

411 Webb et al. 2017) proposed various experiments (listed in Table 2) that resulted in  
412 significant progress in understanding cloud feedback mechanisms and future changes in  
413 low clouds. Though atmosphere–ocean coupled models are used for climate projections, it  
414 is difficult to understand the mechanisms of cloud changes from such coupled simulations,  
415 because different changes in atmospheric circulation caused by differently simulated SST  
416 make the understanding of cloud changes highly complicated. Therefore, various  
417 simulations using atmospheric components, where SST is given as a boundary condition,  
418 were proposed to reveal the mechanisms. Atmospheric model simulations forced by SST  
419 observed in the past decades, known as the Atmospheric Model Intercomparison Project  
420 (AMIP), are conducted as a basic experiment. In addition, a simulation of AMIP with a  
421 globally uniform 4 K increase in SST, where CO<sub>2</sub> concentration is not changed, is  
422 performed to examine the effect of increased SST only; AMIP with a composite  
423 geographical pattern of SST rise obtained from CMIP3 coupled GCMs under CO<sub>2</sub> increase  
424 is performed to detect the effect of changes in SST patterns; and AMIP with quadrupled  
425 CO<sub>2</sub> is performed to isolate the cloud response to changes in CO<sub>2</sub> alone without changes in  
426 SST. An aqua planet experiment is performed, as well as that with a 4 K uniform increase in  
427 SST, and with quadrupled CO<sub>2</sub> under constant SST. This approach eliminates influences  
428 from land and topography, and can be used to isolate the effect of the oceans. To  
429 investigate the effects of aerosols, runs are performed using climatological SST with  
430 pre-industrial aerosols, with aerosols from the year 2000, and with sulfate aerosols from the

431 year 2000 and other aerosols in the pre-industrial era. For instance, these AMIP series data  
432 with SST perturbations were used by Webb and Lock (2013) and Webb et al. (2015) for  
433 studies related to cloud feedback, and by Kawai et al. (2016, 2018) for studies of future  
434 changes in marine fog. AMIP experiments with quadrupled CO<sub>2</sub> were used by Kamae et al.  
435 (2015) to investigate the cloud response to increasing CO<sub>2</sub> without SST changes. This  
436 direct cloud response to increased greenhouse gas concentration is called ‘cloud  
437 adjustment’, in which the effect of changes in surface air temperature is mostly excluded, in  
438 contrast to cloud feedback (Kamae et al. 2015). They found that a downward shift in the  
439 low-cloud layer and a reduction in low cloud occur as a result of the adjustment. Zelinka et  
440 al. (2014) used simulation data with pre-industrial and year 2000 aerosols, and quantified  
441 components of aerosol–cloud–radiation interactions in CMIP5 multi models. For instance,  
442 they found that roughly 25% of the ensemble mean shortwave radiation change comes  
443 from radiation changes due directly to aerosol changes, and 75% comes from radiation  
444 changes through changes in clouds.

445 In fact, even when atmospheric simulations conducted using atmospheric components of  
446 CMIP5 climate models with a common SST field are intercompared, it is still difficult to  
447 elucidate the different mechanisms associated with cloud changes in different models in  
448 detail. This is because large-scale meteorological fields, including vertical velocity and  
449 horizontal advection, change differently in the atmospheric models, even if a common SST  
450 and SST perturbation are used for such simulations. A model intercomparison case, CGILS

451 [CFMIP-GCSS Intercomparison of Large-Eddy and Single-Column Models, where GCSS  
452 stands for GEWEX (Global Energy and Water Cycle Experiment) Cloud System Study],  
453 was designed by Zhang et al. (2010, 2012), based on Zhang and Bretherton (2008), to  
454 understand in detail the cloud feedback mechanism of marine low clouds in climate models.  
455 A single column model (SCM) is a vertical one-dimensional model without a dynamics  
456 scheme, which is extracted from a three-dimensional climate model, and it has the same  
457 physical schemes as the original climate model. SCMs are the most simplified versions of  
458 GCMs and used to simplify the circumstances by controlling the forcing and to understand  
459 the behavior of MLCs simulated in GCMs. Generally, horizontal advection tendencies of  
460 temperature and water vapor and the vertical velocity are given as forcings (also horizontal  
461 wind field itself or geostrophic wind is given), and temperature and water vapor profiles are  
462 calculated by the models. In the intercomparison case, three different marine low-level  
463 cloud regimes (shallow cumulus, stratocumulus, and stratus) are simulated under a control  
464 climate forcing and a future climate forcing with a 2 K increase in SST. Zhang et al. (2013)  
465 found, from the analysis of CGILS using SCMs, that SCMs in which the shallow convection  
466 scheme is active (inactive) tend to have positive (negative) cloud feedback for  
467 stratocumulus regimes (Fig. 12). They showed that shallow convection becomes more  
468 vigorous and transports more water vapor from the boundary layer to a free atmosphere in  
469 a warmer climate for models in which the shallow convection scheme is active. Brient and  
470 Bony (2013) performed several sensitivity experiments utilizing this case and discussed the



471 relationship between changes in low-level clouds and changes in the vertical gradient of  
472 moist static energy. Blossey et al. (2013) analyzed LES results from CGILS and discussed  
473 the detailed behavior of changes in low clouds under warmer climates by decomposing  
474 roles of increased SST and weakened subsidence. Several other LES studies have  
475 investigated the responses of low clouds to global warming in other settings. Bretherton  
476 (2015) and Bretherton and Blossey (2014) discussed mechanisms related to the low cloud  
477 feedback: cloudiness reduction due to surface warming (thermodynamic effect), cloudiness  
478 reduction due to CO<sub>2</sub>- and H<sub>2</sub>O-induced increase in atmospheric emissivity aloft (radiative  
479 effect), cloudiness increase due to increased lower tropospheric stratification (stability  
480 effect), and cloudiness increase due to reduced subsidence (dynamic effect). They  
481 concluded that cloud decreases in warmer climates and the low cloud feedback is positive  
482 as results of the four mechanisms.

483 Recent studies based on observational relationships and GCMs also tend to support  
484 decreases in low cloud cover in warmer climates and the positive low cloud feedback (e.g.,  
485 Klein et al. 2017, Nuijens and Siebesma 2019). It is shown that decrease in low cloud cover  
486 in warmer climates is plausible based on CMIP5 multi-model simulation data (Qu et al.  
487 2014, 2015) and observational relationships (e.g. Kawai et al. 2017). It is also revealed that  
488 majorities of CMIP5 multi-models (Zelinka et al. 2013) and CMIP 6 multi-models (Zelinka et  
489 al. 2020) show positive low cloud feedback.

490

## 491 **5. Parameterization of MLCs**

### 492 *5.1 Parameterization of Clouds*

493 A typical horizontal width of a grid box in GCMs is 100 to 200 km, and that in global NWP  
494 models is 15 to 50 km (note that the actual shape of a grid box is like a thin plate that has a  
495 horizontal size of ~100 km and ~0.2 km thick rather than a box). However, clouds can be  
496 much smaller than this and may only partly cover such model grid boxes, as shown in Fig.  
497 13. In addition, the actual effective resolution of atmospheric models is 4–6 times larger  
498 than the model grid box (e.g., Skamarock 2004, Frehlich and Sharman 2008). Therefore,  
499 the concept of cloud fraction, which is defined as a fraction of a model grid box covered by  
500 clouds, should be used instead of assigning “completely clear” or “completely cloudy” to  
501 each model grid box. The most important purpose of cloud parameterization is to determine  
502 cloud fraction and cloud water content, which is the mass ratio of cloud water to moist air,  
503 for each model grid box. Cloud water content is the sum of liquid water content and ice  
504 water content. This part of GCMs, in which subgrid-scale variability of physical variables  
505 including water vapor is essential, is sometimes called cloud “macrophysics” in contrast to  
506 cloud microphysics that refers to micro-scale physical processes related to clouds including  
507 phase change, conversion to rain, and nucleation. For instance, in the case of relative  
508 humidity of 97%, cloud fraction of the grid box can vary from 0% to near 100% (e.g. 80%)  
509 depending on the assumed subgrid-scale variability in the grid box, accompanied by the  
510 corresponding cloud water content.

511

512 *a. Calculation of cloud fraction and cloud water content*

513 There are three ways to determine a pair of cloud fraction and cloud water content values  
514 for each model grid. The first is to calculate cloud water content prognostically and  
515 determine cloud fraction diagnostically (e.g., Sundqvist et al. 1989):

516 
$$\frac{\partial \overline{q_c}}{\partial t} = \text{adv}(\overline{q_c}) + S_{\text{conv}} + S_{\text{str}} - E - G, \quad (1)$$

517 
$$A = f(\overline{\text{RH}}), \text{ or } f(\overline{\text{RH}}, \overline{q_c}) \text{ etc.}, \quad (2)$$

518 where  $q_c$  ( $\text{kg kg}^{-1}$ ) is cloud water content;  $\text{adv}(\ )$  is an advection term;  $S_{\text{conv}}$  and  $S_{\text{str}}$  ( $\text{kg kg}^{-1}$   
519  $\text{s}^{-1}$ ) are production terms related to convection and stratiform, respectively;  $E$  and  $G$  ( $\text{kg}$   
520  $\text{kg}^{-1} \text{s}^{-1}$ ) are dissipation terms due to evaporation and conversion into precipitation,  
521 respectively;  $A$  (non-dimensional) is the cloud fraction; and  $\text{RH}$  (non-dimensional) is relative  
522 humidity. To clearly distinguish grid-box-average and sub-grid-box values, overbars are  
523 used to denote the spatial average in each model grid box. In this method, cloud water  
524 content is integrated timestep-by-timestep using the equation of temporal differentiation,  
525 and the cloud fraction is calculated simply as a function of, for example, relative humidity.

526 The second way is to calculate both cloud water content and cloud fraction prognostically  
527 (e.g., Tiedtke 1993, Mannoji 1995):

528 
$$\frac{\partial \overline{q_c}}{\partial t} = \text{adv}(\overline{q_c}) + S_{\text{conv}} + S_{\text{str}} - E - G, \quad (3)$$

529 
$$\frac{\partial A}{\partial t} = \text{adv}(A) + AS_{\text{conv}} + AS_{\text{str}} - AE - AG, \quad (4)$$

530 where  $AS_{\text{conv}}$ ,  $AS_{\text{str}}$ ,  $AE$ , and  $AG$  ( $\text{s}^{-1}$ ) are similar to  $S_{\text{conv}}$ ,  $S_{\text{str}}$ ,  $E$ , and  $G$  but for cloud fraction,

531 respectively. In this method, both cloud water content and cloud fraction are integrated  
532 using the differential equations in time, respectively.

533 The third way to calculate cloud fraction and cloud water content is a cloud scheme in  
534 which the prognostic variables are total water content  $\overline{q}_t$  ( $= \overline{q} + \overline{q}_c$ ) ( $\text{kg kg}^{-1}$ ) and liquid-  
535 frozen water temperature  $\overline{T}_L$  ( $= \overline{T} - L/c_p \cdot \overline{q}_c$ ) (K), where  $q$  ( $\text{kg kg}^{-1}$ ) is specific humidity,  $T$   
536 (K) is temperature,  $L$  ( $\text{J kg}^{-1}$ ) is latent heat (the sum of latent heat of evaporation and fusion  
537 is used as for ice clouds), and  $c_p$  ( $\text{J K}^{-1} \text{kg}^{-1}$ ) is the specific heat at constant pressure. The  
538 set of variables  $\overline{q}_t$  and  $\overline{T}_L$  is used because they are conserved during phase changes of  
539 cloud water ('cloud-conserved variables'; Smith 1990). These variables do not change even  
540 when clouds evaporate or form from water vapor, or when liquid clouds freeze or ice clouds  
541 melt in the grid box. A pair of cloud water content and cloud fraction values is then  
542 mathematically deduced from these variables using assumed probability density functions  
543 (PDFs) (e.g., Mellor 1977, Sommeria and Deardorff 1977, Smith 1990, Le Treut and Li  
544 1991). Calculations using this method are as follows:

$$545 \quad \overline{q}_c = f_1(\overline{q}_t, \overline{T}_L), \quad (5)$$

$$546 \quad A = f_2(\overline{q}_t, \overline{T}_L), \quad (6)$$

547 where  $f_1$  and  $f_2$  are uniquely determined using assumed PDF shapes for  $q_t$  and  $T_L$ . A  
548 schematic of this PDF-based cloud scheme is shown in Fig. 14. Cloud fraction is calculated  
549 as an area of the PDF where  $q_t$  is larger than the saturation specific humidity  $\overline{q}_s$  ( $\text{kg kg}^{-1}$ ).  
550 Cloud water content is calculated as the integrated value of  $q_t - \overline{q}_s$  weighted by the PDF of

551  $q_t$  (the first moment of the PDF of  $q_t$ ) for  $q_t$  larger than the saturation specific humidity, as  
552 shown in the equation in Fig. 14. Here, we ignore the subgrid-scale inhomogeneity of  
553 temperature (or liquid–frozen water temperature) for simplicity, and discuss the  
554 inhomogeneity of humidity only. In these types of scheme, the PDF of total water content is  
555 a key element and is necessary for the calculations. Furthermore, the PDFs of water vapor  
556 and cloud water are implicitly assumed as well in the first and second methods described  
557 above, where  $\overline{q_c}$  is a prognostic variable. As shown in Fig. 15, for instance, the Sundqvist  
558 scheme assumes delta functions for both the clear part and the cloudy part, while the  
559 Tiedtke scheme assumes a uniform top hat function for the clear part and a delta function  
560 for the cloudy part.

561 Generally, in the state-of-the-art GCMs and operational global weather prediction models,  
562 their cloud macrophysics are still based on one of these three ways, although they have  
563 liquid and ice water contents as separated prognostic variables and some of the models  
564 have prognostic number concentrations of droplets and ice crystals. For instance, the Max  
565 Planck Institute for Meteorology Earth System Model version 1.2 (MPI-ESM1.2) (Mauritsen  
566 et al. 2019) utilizes Sundqvist et al. (1989) scheme as their cloud macrophysics, and it is  
567 based on the aforementioned first way. A GCM MRI-ESM2 (Yukimoto et al. 2019) and the  
568 European Centre for Medium-Range Weather Forecasts (ECMWF) operational global  
569 model Integrated Forecasting System (IFS) (ECMWF 2019) basically utilize Tiedtke (1993)  
570 scheme, and the Met Office climate model HadGEM3 (Williams et al. 2018, Walters et al.

571 2017) adopts Wilson et al. (2008) scheme as their cloud macrophysics, and they are based  
572 on the aforementioned second way. A GCM MIROC6 (Tatebe et al. 2019) utilizes Watanabe  
573 et al. (2009) scheme and the JMA operational global model Global Spectral Model (JMA  
574 2019) adopts Smith (1990) scheme, and they are based on the aforementioned third way.  
575 As examples of the third way, there are advanced attempts to unify cloud macrophysics,  
576 boundary layer turbulence, and shallow convection schemes using common PDFs, such as  
577 the Cloud Layers Unified by Binormals (CLUBB) scheme (e.g., Guo et al. 2014, Guo et al.  
578 2015, Bogenschutz et al. 2013). In a version of CLUBB, not only PDFs of total water  
579 content and liquid-frozen water temperature, but also sub-grid PDFs of vertical velocity are  
580 explicitly taken into account (Guo et al. 2014): vertical velocity PDFs are used for  
581 calculation of aerosol activation that determines cloud droplet number concentration.

582

### 583 *b. Probability density functions*

584 The PDFs have been given just as assumed ones in many previous studies related to  
585 cloud parameterization (e.g., a Gaussian distribution: Sommeria and Deardorff 1977, Mellor  
586 1977; a triangular distribution: Smith 1990; a uniform distribution: Le Treut and Li 1991).  
587 Other studies have examined PDF shapes using CRMs or LES models (e.g., Laplace and  
588 exponential distributions: Bougeault 1981, Xu and Randall 1996; a gamma distribution:  
589 Bougeault 1982; a beta distribution: Tompkins 2002; binormal distributions: Lewellen and  
590 Yoh 1993; a skewed-triangular distribution: Watanabe et al. 2009). Several studies have

591 investigated these PDFs based on observations such as aircraft data (e.g., Wood and Field  
592 2000, Larson et al. 2002) or satellite data (e.g., Considine et al. 1997, Wood and Hartmann  
593 2006). For instance, Kawai and Teixeira (2010, 2012) used satellite data to show that the  
594 PDFs vary depending on the cloud regimes (Fig. 16) and the shape of the PDFs is highly  
595 correlated with the stabilities of the lower troposphere.

596 Not only the shape of PDFs but also the width of the PDFs is important in PDF-based  
597 cloud schemes. In the original concept of PDF based cloud schemes (e.g. Sommeria and  
598 Deardorff 1977, Mellor 1977) the widths of PDFs were supposed to be obtained from  
599 turbulence schemes. However, such widths from turbulence schemes are too small for  
600 PDF-based cloud schemes used in GCMs or NWP models, because the widths are not  
601 determined by the fluctuations at the turbulence scale but mainly by meso-scale  
602 fluctuations. Therefore, it is impossible to obtain PDF information from turbulence schemes  
603 and more practical ways are adopted in GCMs and NWP models (e.g., Smith 1990). In fact,  
604 it is difficult to determine the widths simply, because the widths must vary depending on  
605 structures or morphologies of cloud regimes, altitude, and meteorological conditions as well  
606 as the shape of PDFs.

607

### 608 *c. Calculations of precipitation and radiation from clouds*

609 In cloud parameterizations, the dissipation terms of cloud water content such as those  
610 due to conversion into precipitation must be calculated in addition to the terms associated

611 with cloud formation. In PDF-based cloud schemes, these dissipation terms are calculated  
612 after cloud water content is determined by Eq. (5). As an example of such terms,  
613 autoconversion is commonly used to calculate conversion of cloud water content to  
614 precipitation in large-scale models (e.g., Sundqvist 1978, Rotstayn 1997). The  
615 autoconversion rate (the conversion rate of cloud water content to precipitation), is  
616 assumed to be proportional to the  $\alpha$ th power of cloud water content. The cloud water  
617 content and cloud fraction thus obtained are used not only in moist processes, but also  
618 radiation processes; for instance, shortwave reflectance, which is the ratio of reflected  
619 radiation to incident radiation, is calculated from vertically integrated cloud water content.

620 Grid-box-average values of cloud water content have been commonly used to calculate  
621 autoconversion rate. Generally, grid-box-average values of integrated cloud water content  
622 are also used for the calculation of shortwave reflectance in a radiation process. This  
623 means that horizontal homogeneity of cloud water content is assumed for those  
624 calculations, even though cloud water content is in fact horizontally inhomogeneous.  
625 However, inhomogeneously distributed cloud water content in a model grid-box gives  
626 different autoconversion rates of cloud water to precipitation in the moist processes (e.g.,  
627 Larson et al. 2001, Wood et al. 2002, Kawai and Teixeira 2012) and a different albedo in the  
628 radiation processes (e.g., based on observations: Cahalan et al. 1994, Barker et al. 1996,  
629 Pincus et al. 1999, Oreopoulos and Cahalan 2005, Kawai and Teixeira 2012; based on  
630 large eddy simulations: Kogan et al. 1995, Bäuml et al. 2004, de Roode and Los 2008) from



631 the homogeneously distributed case, even though the average cloud water content in the  
632 model grid box is the same. Thus, PDF information is needed for two steps in model  
633 calculations (Fig. 17): PDFs of humidity (and temperature) are required to determine a pair  
634 of cloud fraction and cloud water content at the first step, and PDFs of cloud water content  
635 to determine the inhomogeneity effect on, for instance, calculations of autoconversion and  
636 albedo, at the second step.

637 Several studies have investigated inhomogeneity effects of cloud microphysics including  
638 autoconversion rate and radiation calculation in GCMs. For instance, Morrison and  
639 Gettelman (2008) implemented an inhomogeneity effect of cloud microphysics in their GCM  
640 assuming a gamma function, and their cloud microphysics is also used in Guo et al. (2014).  
641 Hotta et al. (2020) investigated an inhomogeneity effect of autoconversion rate in their  
642 GCM using a triangular function that is also used for their cloud macrophysics. Hill et al.  
643 (2015) investigated inhomogeneity effects both of cloud microphysics and radiation  
644 calculation in their GCM using a parameter of inhomogeneity obtained from satellite  
645 observation, which depends on the cloud regimes. However, at present, these PDFs used  
646 for cloud macrophysics and inhomogeneity effects for cloud microphysics and radiation  
647 process are not treated consistently in many GCMs and global NWP models.

648

## 649 *5.2 Difficulties in Parameterization of MLCs*

650 Even when the cloud schemes introduced in Section 5.1 are applied, MLCs are not easily

651 reproduced in GCMs and NWP models. The main reason for this is that interactions of the  
652 many physical processes related to MLCs are complicated, and the model layers are not  
653 thin enough in the vertical to represent processes related to MLCs (as discussed in Section  
654 2.3). Mid- and high-level clouds can be represented by the aforementioned cloud schemes  
655 to some extent because the cloud fraction is generally related to relative humidity in such  
656 schemes and mid- and high-level clouds in nature have some correlation with grid-scale  
657 relative humidity. However, even very small tendencies in the formation and dissipation  
658 terms can form or destroy MLCs, and furthermore, relative humidity can be strongly  
659 controlled by cloud cover itself for MLCs, while updraft of air, which is determined mainly by  
660 large-scale convergence, controls relative humidity for mid- and high-level clouds.

661 Therefore, various specific schemes and treatments have been proposed to represent  
662 MLCs in models. For instance, Slingo (1980, 1987) and Teixeira and Hogan (2002)  
663 proposed diagnostic cloud amount schemes specialized for MLCs, which are incorporated  
664 into diagnostic cloud schemes based on relative humidity. They used inversion strength to  
665 determine stratocumulus cloud amount because stratocumulus clouds could not be  
666 reproduced by diagnostic cloud schemes based only on relative humidity. For instance,  
667 Kawai and Inoue (2006) showed that the representation of stratocumulus in GSM, which is  
668 a global operational model at the JMA, was dramatically improved by the implementation of  
669 a simple stratocumulus scheme based on Slingo (1980, 1987), although the model could  
670 not have represented any subtropical stratocumulus clouds until 2004.

671 To reproduce MLCs based on physics, it is particularly important to represent accurately  
672 the mixing of air at the top of clouds, including cloud top entrainment. Therefore, not only  
673 the cloud scheme, but also the turbulence scheme must be developed simultaneously or as  
674 a combination in order to represent MLCs. Figure 18 shows that subtropical stratocumulus  
675 is well represented in MRI-ESM2 (Yukimoto et al. 2019), in which turbulent mixing at the top  
676 of the cloud layer is strongly suppressed in conditions where stratocumulus is likely to form  
677 (Kawai et al. 2019). However, this figure shows that the stratocumulus disappears when  
678 this treatment (scheme) is turned off. Lock et al. (2000) proposed a boundary layer mixing  
679 scheme in which the boundary layer is classified into six types and the diffusion coefficient  
680 is calculated differently for each type; e.g., cumulus-capped, stratocumulus over cumulus,  
681 stratocumulus not over cumulus, and mixed layer with stratocumulus, with an explicit  
682 parameterization of cloud top entrainment.

683 Shallow convection schemes are also important because they significantly modify MLC  
684 coverage (e.g., Park and Bretherton 2009, Ogura et al. 2017); more active shallow  
685 convection results in smaller MLC coverage, as mentioned in Section 4.2. Zhao et al.  
686 (2018) showed that subtropical stratocumulus can be successfully increased by turning off  
687 shallow convection where EIS is larger than a threshold value (that is, favorable condition  
688 for stratocumulus) in Geophysical Fluid Dynamics Laboratory (GFDL) Global Atmosphere  
689 Model AM4.0. The ECMWF operational global model also uses this treatment (ECMWF  
690 2019). Kawai et al. (2019) showed that the vertical structure of low clouds in the area of

691 stratocumulus to cumulus transition is improved and low cloud cover is increased also in  
692 the Southern Ocean together with a reduction in the radiation bias by turning off shallow  
693 convection when ECTEI is larger than a threshold value in MRI-ESM2.

694 In recent years, it has been recognized that the occurrence frequency of tropical and  
695 subtropical marine low clouds is too low but the albedo of the cloudy part of such clouds is  
696 too high, although the radiative flux errors are compensated by these two errors. This is  
697 known as the ‘too few, too bright low-cloud problem’ (e.g., Zhang et al. 2005, Karlsson et al.  
698 2008, Nam et al. 2012). Some studies suggest that an insufficient vertical resolution in  
699 GCMs can cause this problem (e.g., Konsta et al. 2016). Several methods that compensate  
700 for insufficient vertical resolution have been developed, including the use of vertical  
701 sublevels (Wilson et al. 2007). Brooks et al. (2005) proposed the introduction of areal cloud  
702 fraction, which is different from volume cloud fraction, although these two cloud fractions  
703 are identical in conventional GCMs under the assumption of vertically homogeneous cloud  
704 in each model vertical layer.

705

706

## 707 **6. Other modeling issues related to MLCs in GCMs**

708 The main purpose in the parameterization part of this paper is to introduce the basics of  
709 cloud macrophysics that directly determine cloud fraction and cloud water content in GCMs.  
710 Obviously, changes in cloud fraction and cloud water content in warmer climates are

711 important for climate simulations. However, there are other factors related to low clouds that  
712 affect climate simulations. Figure 19 summarizes low cloud properties important for climate  
713 simulations and the physical processes that mainly determine them in GCMs. One of the  
714 major factors is a cloud phase change (ice to liquid) in warmer climates that is related to  
715 cloud microphysics in GCMs. Another is a change in radiative flux due to aerosol–cloud  
716 interaction in different aerosol climates. Therefore, we briefly mention these two issues in  
717 the context of parameterizations in GCMs and their difficulties.

718

### 719 *6.1 Liquid and ice clouds (Cloud microphysics)*

720 A significant lack of clouds and/or optical thickness over the Southern Ocean is a serious  
721 problem in most climate models, and it causes huge biases in shortwave radiative flux over  
722 the Southern Ocean, especially in the summer months (Trenberth and Fasullo 2010).  
723 Although the causes of this problem include a lack of cloud fraction and insufficient cloud  
724 number concentration due to a lack of cloud condensation nuclei, some studies have  
725 pointed out that the lack of supercooled liquid water in GCMs is a source of insufficient  
726 solar reflectance of clouds over the Southern Ocean (e.g., Bodas-Salcedo et al. 2016, Kay  
727 et al. 2016). At the temperature of the marine boundary layer over the Southern Ocean,  
728 liquid phase and ice phase clouds can coexist. Liquid clouds are optically thicker than ice  
729 clouds if the cloud (liquid + ice) water content is the same because the size ( $r_c$ ) of cloud  
730 droplets is much smaller than that of ice crystals and this corresponds to a larger number

731 concentration for cloud droplets. In this case, the sum of the scattering cross-sections of  
732 cloud particles that essentially determines optical thickness is increased, largely because  
733 the contribution of increased number concentration ( $\propto r_c^{-3}$ ) is more significant than that of  
734 decreased scattering cross-sections of each particle ( $\propto r_c^2$ ). In recent years, Cloud-  
735 Aerosol Lidar and Infrared Pathfinder Satellite Observations (CALIPSO; Winker et al. 2009)  
736 data have revealed that the ratio of liquid phase at the temperature of the mixed phase is  
737 much larger than expected (e.g., Hu et al. 2010, Cesana and Chepfer 2013). McCoy et al.  
738 (2015) compared the phase ratio in CMIP5 models and CALIPSO observations and found  
739 that the phase ratios in CMIP5 models vary widely and the ratio of liquid phase  
740 (supercooled water) in most models is much smaller than that observed.

741 Another issue is related to low cloud feedback especially over the Southern Ocean. If ice  
742 clouds change to liquid clouds in warmer climates due to increasing temperature, the  
743 optical thickness of clouds increases and suppresses the temperature increase due to  
744 greenhouse gases (negative cloud feedback). However, this negative feedback does not  
745 happen if the clouds are already liquid clouds in the present climate. Therefore, cloud  
746 phase is also an important factor for climate simulations and the importance of this  
747 feedback especially over the Southern Ocean has been studied by many researchers  
748 (Tsushima et al. 2006, McCoy et al. 2015, Bodas-Salcedo et al. 2016, Kay et al. 2016, Tan  
749 et al. 2016, Frey and Kay 2018).

750 A great amount of effort is being devoted to solve this issue of insufficient supercooled

751 liquid clouds by modelers. For instance, Forbes et al. (2011) successfully increased the  
752 ratio of supercooled liquid water and reduced shortwave radiation bias over the Southern  
753 Ocean in the ECMWF global model, by reduction in the ice deposition rate at cloud top in  
754 the cloud microphysics. In the Community Atmosphere Model CAM6, the shortwave  
755 radiation bias over the Southern Ocean due to insufficient supercooled liquid water was  
756 ameliorated by the new ice nucleation scheme and the new prognostic microphysics  
757 scheme (Bogenschutz et al. 2018). In the Met Office climate model HadGEM3, the similar  
758 radiation bias was improved due to increase in supercooled liquid water by introducing  
759 turbulent production of liquid water in mixed-phase clouds (Williams et al. 2018, Walters et  
760 al. 2017, Furtado et al. 2016). Kawai et al. (2019) achieved the increase in the ratio of  
761 supercooled liquid water by utilizing an observed relationship for determining the liquid-ice  
762 ratio in a source term of cloud water in MRI-ESM2. Zelinka et al. (2020) showed that the  
763 ratio of supercooled liquid water is increased in CMIP6 multi-models from CMIP5  
764 multi-models, and it could be a reason for larger temperature increase in CMIP6  
765 multi-models than in CMIP5 multi-models.

766 The cloud phase is generally calculated by the cloud microphysics in models. Although  
767 cloud microphysics is beyond the scope of this paper, some of the difficulties concerning  
768 the usage of microphysics schemes in GCMs or global NWP models are briefly introduced  
769 here. One problem is that a long time step is used in these models although cloud  
770 microphysics includes many processes that have short time scales. For instance, the time

771 step used in MRI-ESM2 (Yukimoto et al. 2019) for TL159 simulations submitted to CMIP6 is  
772 30 minutes. However, a time step should be less than several tens of seconds for an  
773 appropriate calculation of cloud microphysics (e.g., Barrett et al. 2019, Posselt and  
774 Lohmann 2008, Michibata et al. 2019). One solution to the problem of long time steps is for  
775 short time-scale processes including cloud microphysics and turbulence to be calculated  
776 several times using sub-time-steps within one model integration time step (e.g., Posselt  
777 and Lohmann 2008, Gettelman et al. 2015, Michibata et al. 2019). However, in practice it is  
778 difficult to adopt a sub-time-step that is short enough for cloud microphysics in climate  
779 simulations or operational global simulations due to their computational cost. Forbes et al.  
780 (2011) developed an implicit approach to calculate the microphysics process stably for a  
781 long time step in the ECMWF operational global model.

782 Another issue is that global NWP models and GCMs have large grid boxes of 20 to 200  
783 km and the microphysics cannot assume that a whole grid box has homogeneous  
784 grid-box-average values. Although it is obviously necessary to discriminate between cloudy  
785 and clear parts in a model grid box, this discrimination is far from sufficient. For instance,  
786 there should be mixed-phase parts, ice-only parts and liquid-only parts in the cloudy volume  
787 corresponding to the model grid box size (Tan and Storelvmo 2016). Wilson et al. (2008)  
788 developed a prognostic cloud fraction and condensation scheme, in which liquid only area,  
789 ice only area, mixed phase area, and clear area exist in one model grid box and three  
790 different cloud fractions corresponding to liquid only, ice only and mixed phase areas are



791 prognostic variables. Although this is already a complicated scheme, it still requires many  
792 simplifying assumptions. The complexity dramatically increases if we try to simulate clouds  
793 in a more realistic way. This is a very bothersome problem and we need to develop a  
794 parameterization that is simple enough to implement in GCMs and can still reproduce real  
795 clouds adequately.

796

## 797 *6.2 Aerosol cloud interactions*

798 In climate simulations, in addition to changes in clouds due to temperature increase  
799 caused by increased greenhouse gas concentration, the changes in clouds due to changes  
800 in aerosol concentration are important for estimating accurate temperature increase in the  
801 future climate. Because this topic is also beyond the scope of this paper, only the basic  
802 concept and the associated uncertainty are briefly introduced below.

803 Cloud particles are formed from aerosol particles, where aerosol particles work as cloud  
804 condensation or ice nuclei (e.g., Rogers and Yau 1996). Therefore, aerosol particles must  
805 be intrinsically important for cloud formation. Particularly from the viewpoint of climate  
806 studies and the effect on radiative flux, the influence of aerosols on clouds is referred to as  
807 aerosol–cloud interaction or the aerosol indirect effect (Lohmann and Feichter 2005). There  
808 are two kinds of aerosol–cloud interactions; one is referred to as the cloud-albedo effect or  
809 the first indirect effect, and another as the cloud-lifetime effect or the second indirect effect.  
810 When aerosols are abundant, the number concentration of cloud particles must increase. If

811 cloud water content does not change in the abundant aerosol case, the cloud water is  
812 distributed over many small particles and increases the optical thickness of the clouds  
813 (Twomey 1977). This is called the Twomey effect, cloud-albedo effect or the first indirect  
814 effect. If aerosols are abundant and consequently each cloud particle is small, the  
815 conversion rate of cloud particles to rain or snow must be slower and the lifetime of cloud  
816 particles and the liquid water path will increase (Albrecht 1989). This is called the  
817 cloud-lifetime effect or the second indirect effect. Note that although the term 'lifetime' is  
818 used, this effect is often defined by changes in liquid water path with respect to changes in  
819 the number concentration of aerosols or cloud droplets, because lifetime itself is not easily  
820 measured.

821 However, these aerosol–cloud interactions have not been implemented in operational  
822 global NWP models. For instance, the GSM of JMA does not incorporate them even now  
823 (JMA 2019), although the forecast skill of this model is relatively high. This is because  
824 relative humidity is the dominant factor determining cloud variations on hourly or daily time  
825 scales. On the other hand, aerosol–cloud interactions are critically important for climate  
826 simulations where the spatial cloud patterns evident in snapshots and temporal variations  
827 of clouds vanish with averaging. Because a change in global radiative flux of the order of no  
828 more than  $1 \text{ W m}^{-2}$  significantly influences the results in climate simulations (note that the  
829 radiative forcing of the  $\text{CO}_2$  increase in the past 100 years is less than  $2 \text{ W m}^{-2}$ ; Myhre et  
830 al. 2013), the slight change in optical thickness of clouds due to aerosol–cloud interactions

831 has a significant influence on such simulations. If we do not implement aerosol–cloud  
832 interactions in GCMs, the simulated surface temperature increase in the 20th century is  
833 overestimated because aerosols increased in the 20th century and the aerosol–cloud  
834 interactions should have suppressed the temperature increase to some extent. Therefore,  
835 many GCMs implement aerosol–cloud interactions. For instance, not only liquid and ice  
836 water content but also their number concentrations are prognostic variables in MRI-CGCM3  
837 (Yukimoto et al. 2012) and MRI-ESM2 (Yukimoto et al. 2019) and aerosol–cloud  
838 interactions are incorporated in the model. In contrast, the number concentrations of cloud  
839 droplets and ice crystals are not prognostic variables and the effective radii of cloud  
840 droplets are not affected by aerosol concentrations in the JMA GSM.

841 On the other hand, there are still large uncertainties associated with aerosol–cloud  
842 interactions. Recently, several studies using satellite observations showed that the  
843 cloud-lifetime effect for liquid clouds is much smaller than expected and almost all GCMs  
844 overestimate the effect (e.g., Quaas et al. 2009, Wang et al. 2012), although the magnitude  
845 of the cloud-albedo effect is consistent between observations and GCMs (e.g., Quaas et al.  
846 2009, Gryspeerdt et al. 2020). This inconsistency is currently being debated (e.g., Isaksen  
847 et al. 2009). Even the opposite effect has been proposed recently, in which a reduction in  
848 LWP (e.g., Michibata et al. 2016, Sato et al. 2018a) and a reduction in lifetime occur (e.g.,  
849 Haywood et al. 2009) when aerosols increase. Furthermore, aerosol–cloud interactions for  
850 ice clouds are less well understood than those for liquid clouds because the formation

851 process of ice crystals is much more complicated than that of cloud droplets. The aerosol–  
852 cloud interactions for liquid and ice clouds will be studied extensively by the climate and  
853 cloud communities over the next couple of decades.

854

855

## 856 **7. Conclusions**

857 One purpose of this review paper is to provide the basic knowledge of marine low clouds  
858 and explain the importance of such clouds in climate simulations for readers with a range of  
859 meteorological backgrounds who may not be as familiar with low clouds as they are with  
860 convective and precipitating clouds. Another purpose is to introduce the concept of  
861 parameterization of the clouds in GCMs and the associated difficulties.

862 An introduction to marine low clouds was provided in Section 2, including their global  
863 distribution, important physical processes related to the clouds such as cloud top  
864 entrainment, and basic characteristics such as diurnal variations. Some observational and  
865 modeling studies of such clouds were introduced in Section 3. Subsequently, in Section 4,  
866 the considerable importance of low cloud change for climate simulations was explained and  
867 some recent studies were introduced. The representation of MLCs in GCMs was confirmed  
868 to be the main source of uncertainties in predicted temperature increases in global warming  
869 simulations.

870 In the latter half of this paper, cloud parameterizations and some difficulties related to the

871 representations of clouds in GCMs were introduced. In Section 5, a basic review of cloud  
872 macrophysics was given in terms of the schemes to determine cloud fraction and cloud  
873 water content in each model grid box under the assumption of subgrid-scale inhomogeneity  
874 of water vapor and cloud water. In Section 6, other topics including the difficulties and the  
875 uncertainties in representing cloud phase and aerosol–cloud interactions in GCMs were  
876 briefly introduced, because they exert a significant influence on climate simulations. In  
877 Sections 5 and 6, we highlighted the difficulties of the parameterizations in GCMs that need  
878 to be tackled by this community in the coming decades as well as explaining the basic  
879 concepts. Efforts to develop these parameterizations are still absolutely necessary,  
880 because the horizontal resolution of GCMs is not improving rapidly: the horizontal resolution  
881 is still about 100 km in major CMIP models, though the resolution was several hundred  
882 kilometers a few decades ago. Although some of the issues introduced in this paper are  
883 particularly difficult, the representation of clouds in GCMs, including subtropical  
884 stratocumulus and the Southern Ocean clouds, has gradually been improved in recent  
885 decades through the untiring effort and ingenuity of modelers, as briefly explained in  
886 Sections 5.2 and 6.1. We hope that these sections will be helpful for researchers who are  
887 not modelers but who analyze cloud data from climate simulations such as CMIP data. In  
888 addition, we would be delighted if this paper motivates researchers to work on tackling  
889 these difficult issues and solving some of them to contribute to reducing the uncertainties of  
890 climate simulations.

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893

### Acknowledgments

894 This review paper was developed from the Introduction section of HK's Ph.D. thesis, and  
895 HK thanks his Ph.D. thesis committee members at Kyoto University. We thank the chief  
896 editor Dr. Masaki Satoh for giving us the opportunity to write this review paper. We  
897 acknowledge the editor Dr. Akira Noda and the two anonymous reviewers for their  
898 supportive and insightful comments. This study was partly supported by the Integrated  
899 Research Program for Advancing Climate Models: TOUGOU from the Ministry of Education,  
900 Culture, Sports, Science and Technology (MEXT), Japan. Additionally, it was supported by  
901 the Japan Society for the Promotion of Science (JSPS) KAKENHI Grant Numbers  
902 JP18H03363, JP19K03977, and JP19H05699. The ERA-Interim data were provided by  
903 ECMWF. The ISCCP data were obtained from the NASA Langley Atmospheric Science  
904 Data Center. Some processed data were provided by Tsuyoshi Koshiro. Mrs. Megumi  
905 Eguchi helped edit this manuscript.

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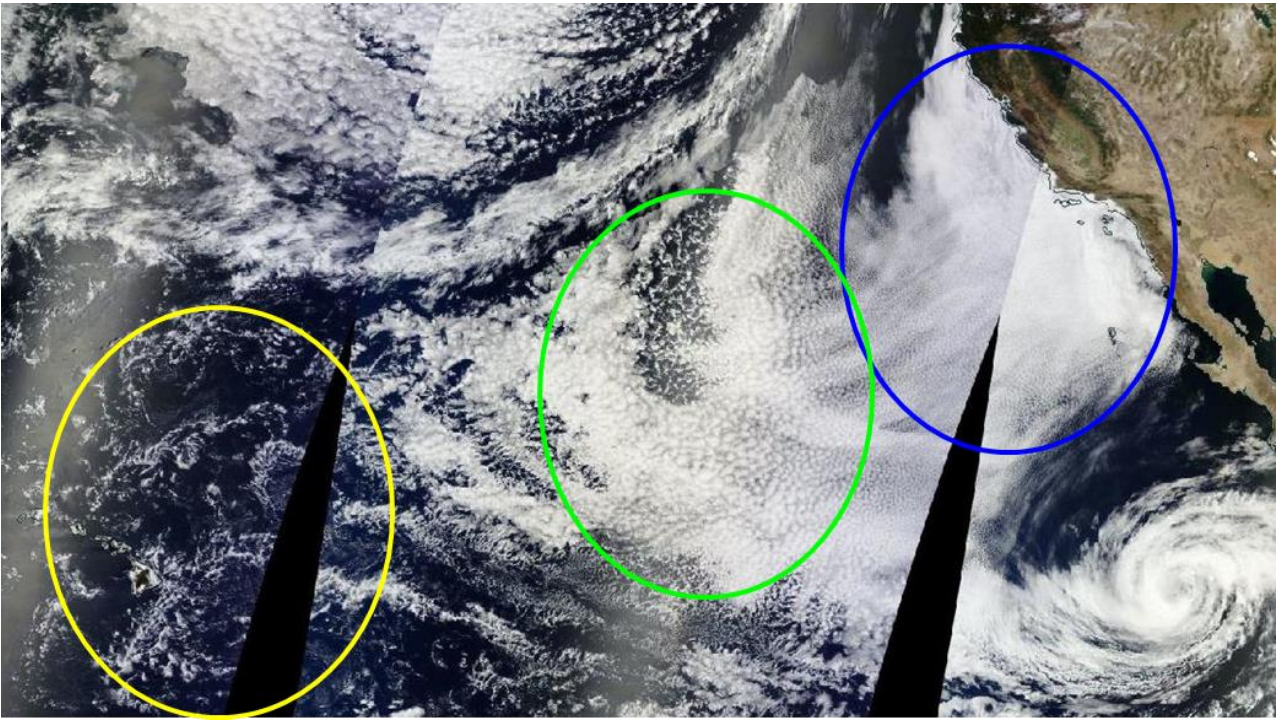
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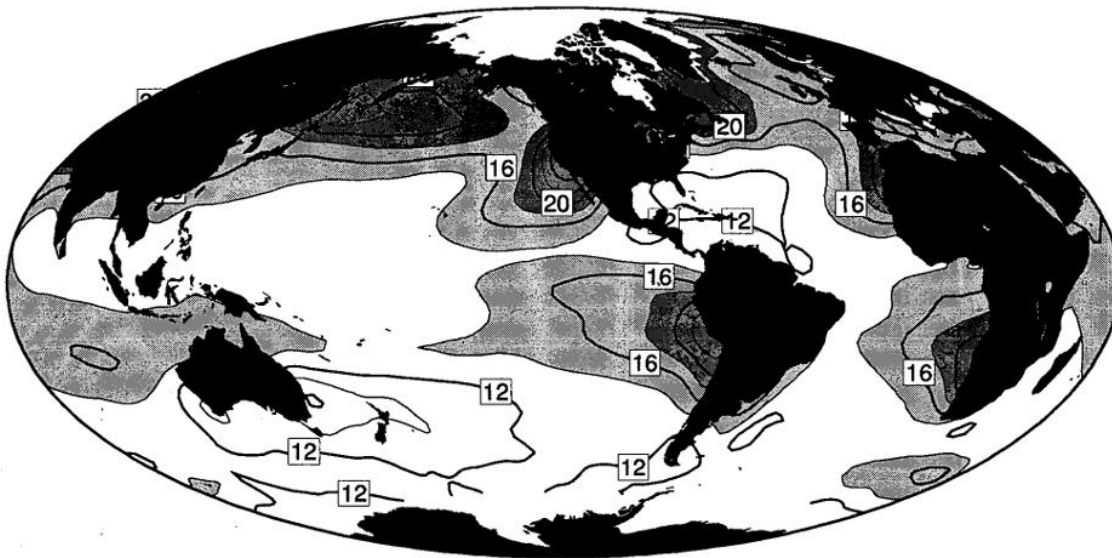
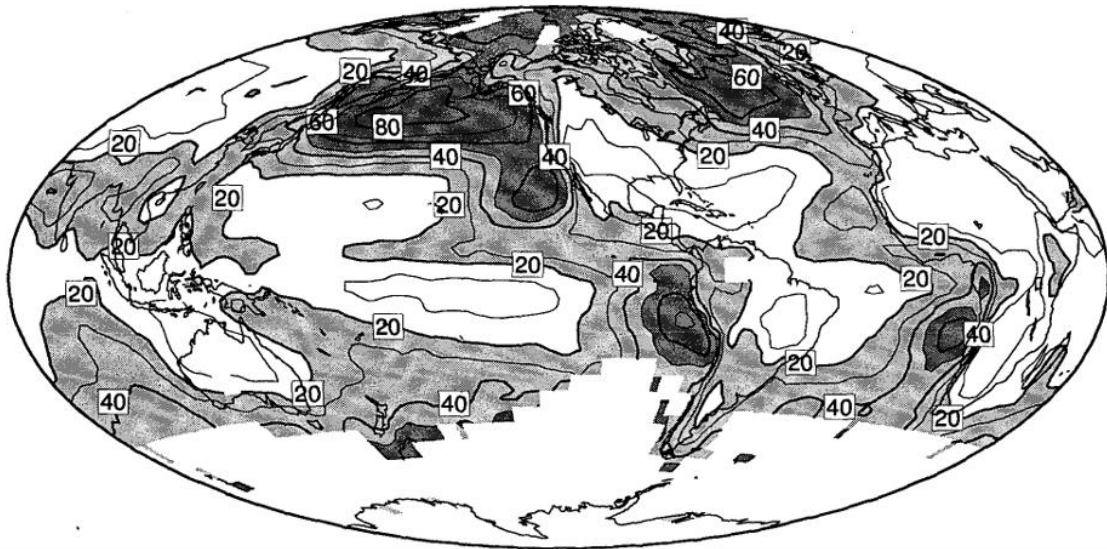
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1486 Fig. 1 Visible image of marine low clouds, including stratus (blue circle), stratocumulus  
1487 (green circle), and cumulus clouds (yellow circle), over an area from off the coast of  
1488 California to Hawaii, acquired by MODIS on July 1, 2014. Source: NASA Worldview.

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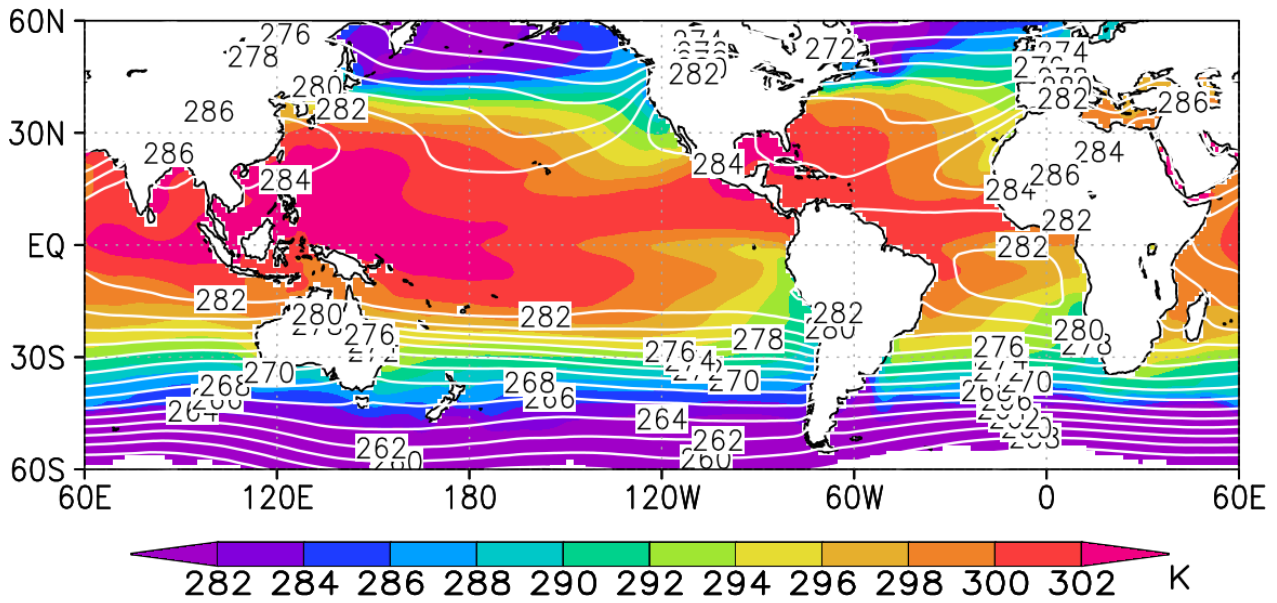
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1493 Fig. 2 Upper panel: Climatology (percent) of low stratiform cloud amount, which consists  
 1494 of stratus, stratocumulus, and sky-obscuring fog, as reported by surface-based  
 1495 observers in June, July, and August. Lower panel: Same as the upper panel but for lower  
 1496 tropospheric stability in Kelvin (Klein and Hartmann 1993). © American Meteorological  
 1497 Society. Used with permission.

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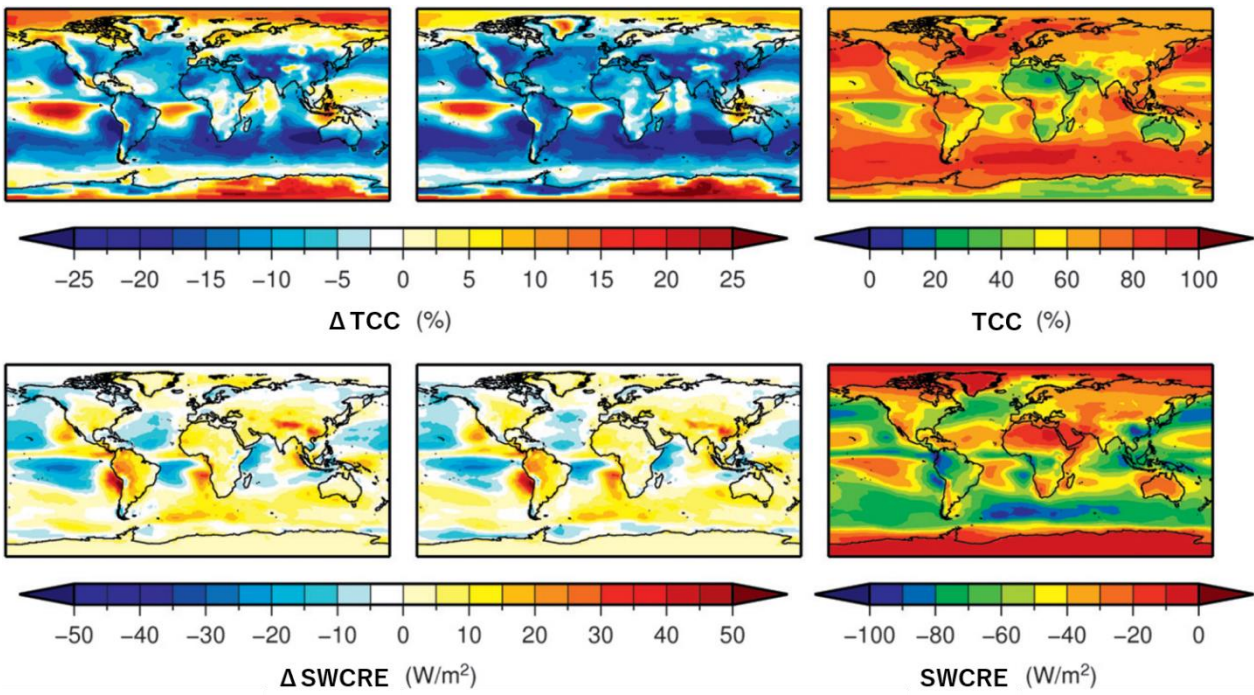
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1502 Fig. 3 Climatology of SST (K; shading) and temperature at 700 hPa (K; contours) for July  
 1503 over 1979–2008. The data are from the European Centre for Medium-Range Weather  
 1504 Forecasts (ECMWF) interim reanalysis (ERA-Interim) (Dee et al. 2011).

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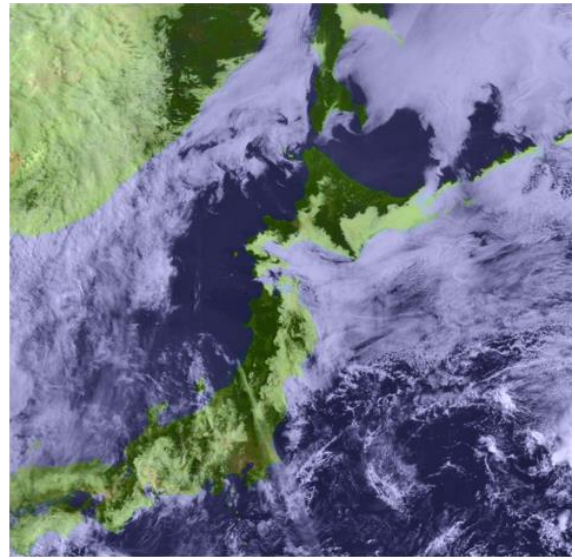
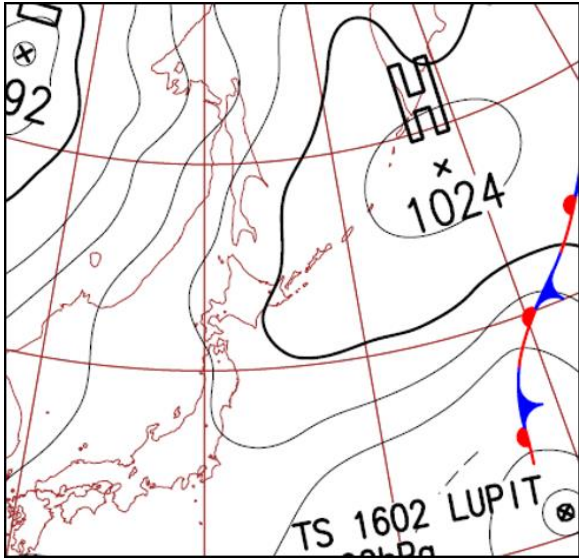
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1509 Fig. 4 Biases of (top) total cloud cover and (bottom) shortwave cloud radiative effect for  
 1510 the (left) CMIP3 and (middle) CMIP5 multimodel means with respect to (right) satellite  
 1511 observations. They are averaged over the 20 years 1986–2005. ISCCP data are used as  
 1512 observational data for total cloud cover and ISCCP-FD for the shortwave cloud radiative  
 1513 effect (modified after fig. 2 in Lauer and Hamilton 2013). © American Meteorological  
 1514 Society. Used with permission.

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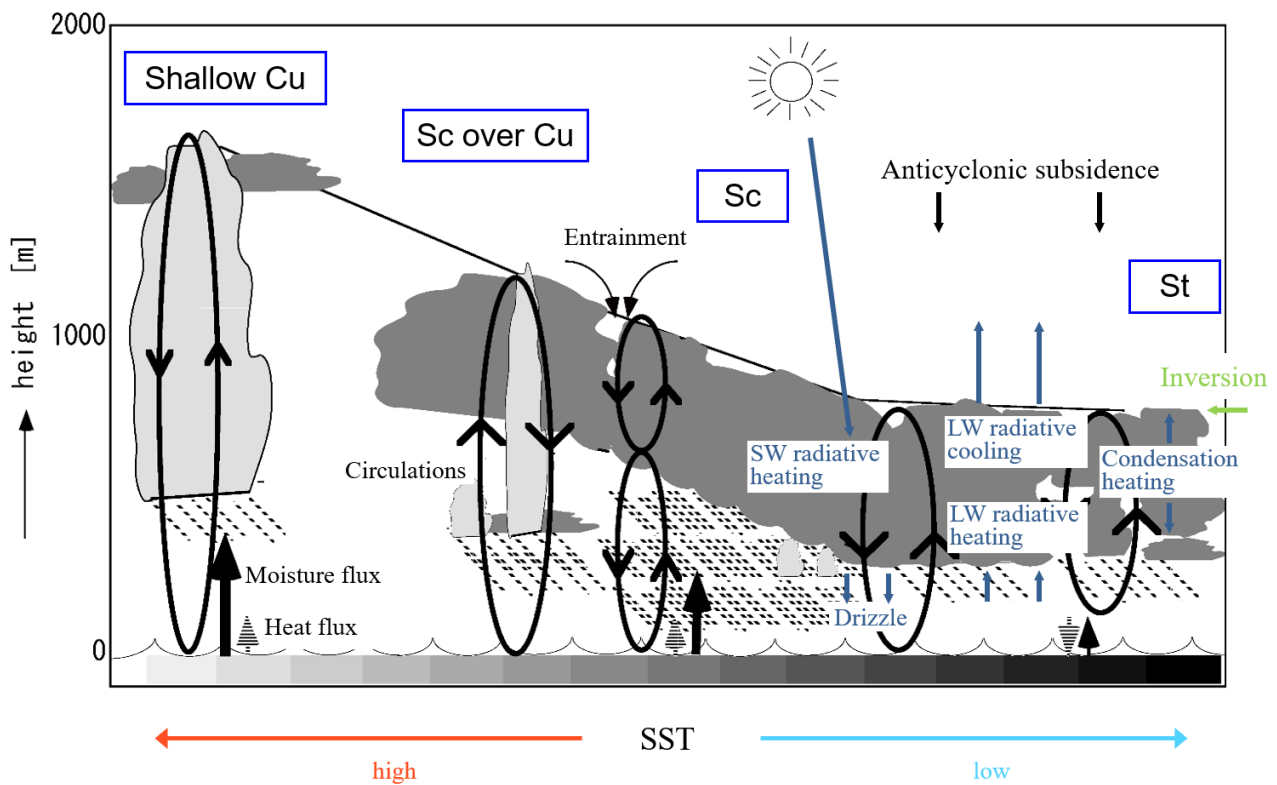
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1519 Fig. 5 (left) Surface weather chart and (right) Himawari-8 satellite visible image of a typical  
 1520 Yamase phenomenon at 0900 local time on July 24, 2016. The weather chart is from the  
 1521 JMA and the satellite image is provided by Kochi University (Weather Home), University  
 1522 of Tokyo, and the JMA.

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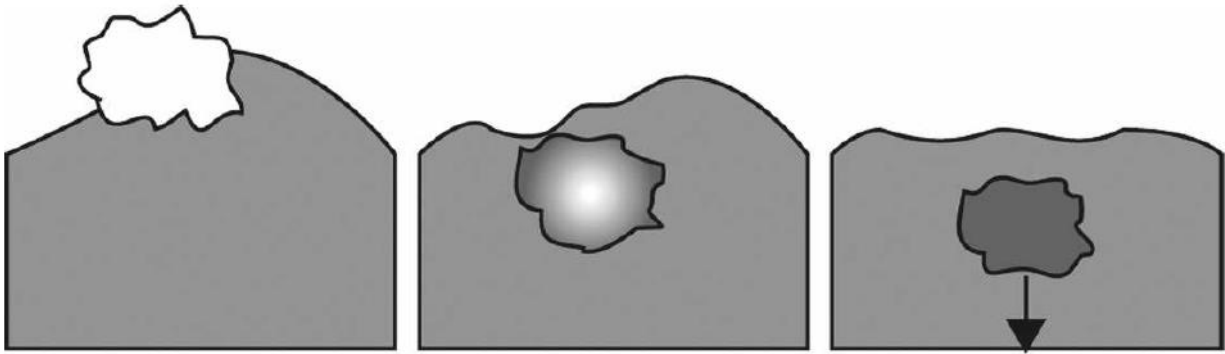
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1527 Fig. 6 Schematic of processes related to subtropical low clouds (modified after fig. 2 in de  
 1528 Roode and Duijnkerke 1997). Cloud regimes are denoted in blue rectangles: St for  
 1529 stratus, Sc for stratocumulus, and Cu for cumulus. © American Meteorological Society.

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Entrainment of  
unsaturated air  
into the cloud

Cooling and  
moistening of  
the parcel by  
evaporation

Downward  
acceleration of  
negatively  
buoyant parcel

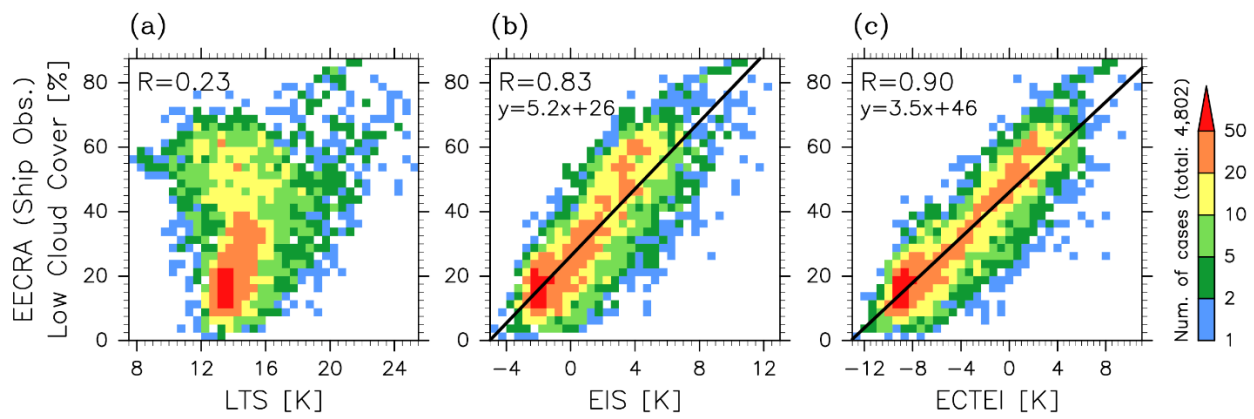
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1535 Fig. 7 Schematic of cloud top entrainment. The shaded area represents cloudy air (fig. 1  
1536 in Yamaguchi and Randall 2008, after Randall 1980). © American Meteorological Society.  
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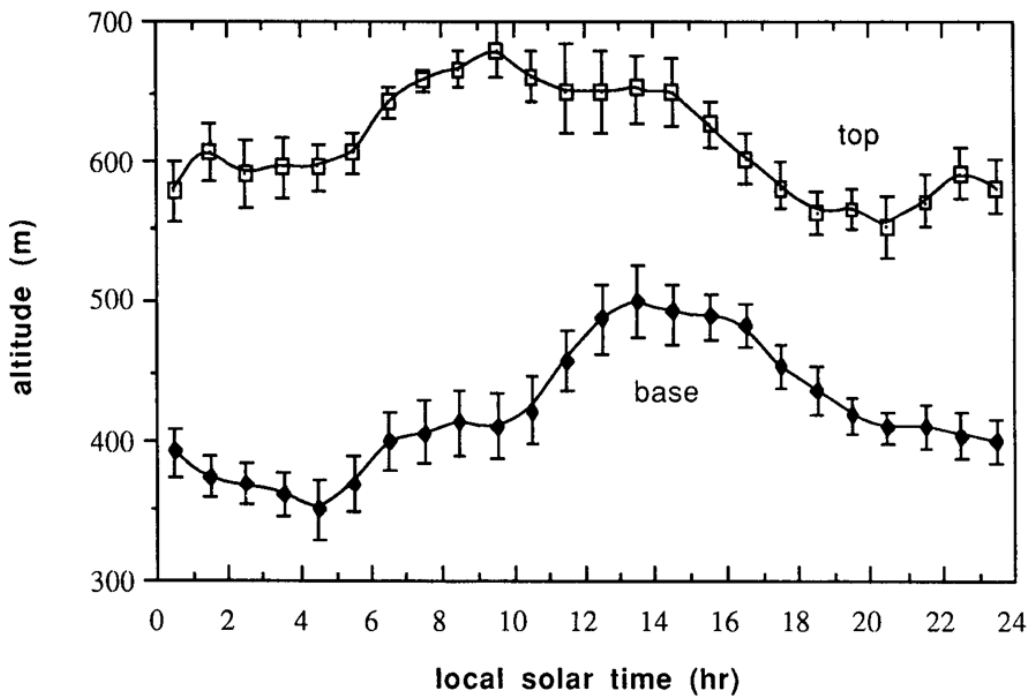
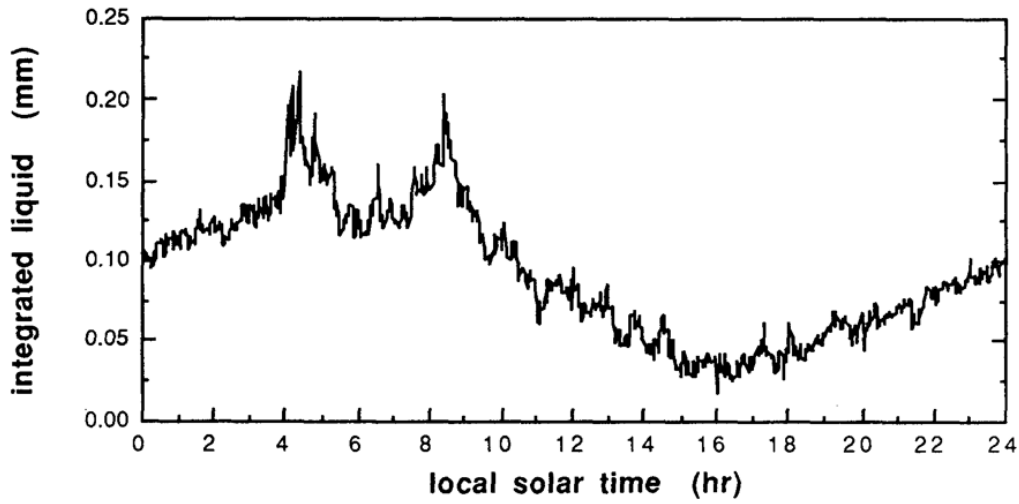
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1542 Fig. 8 Frequencies of occurrence of low stratiform cloud cover (combined cloud cover of  
 1543 stratocumulus, stratus, and sky-obscuring fog) sorted by (a) LTS, (b) EIS, and (c) ECTEI  
 1544 ( $\beta = 0.23$ ), based on all  $5^\circ \times 5^\circ$  seasonal climatology data. Cloud cover data were  
 1545 obtained from the extended edited cloud report archive (EECRA; Hahn and Warren,  
 1546 2009) shipboard observations. Stability indexes were calculated using the ECMWF  
 1547 40-year Re-Analysis (ERA-40) data (Uppala et al. 2005) (1957–2002). All the data  
 1548 between  $60^\circ\text{N}$  and  $60^\circ\text{S}$  for all seasons were used. Linear regression lines and the  
 1549 correlation coefficients are shown. From Kawai et al. (2019).

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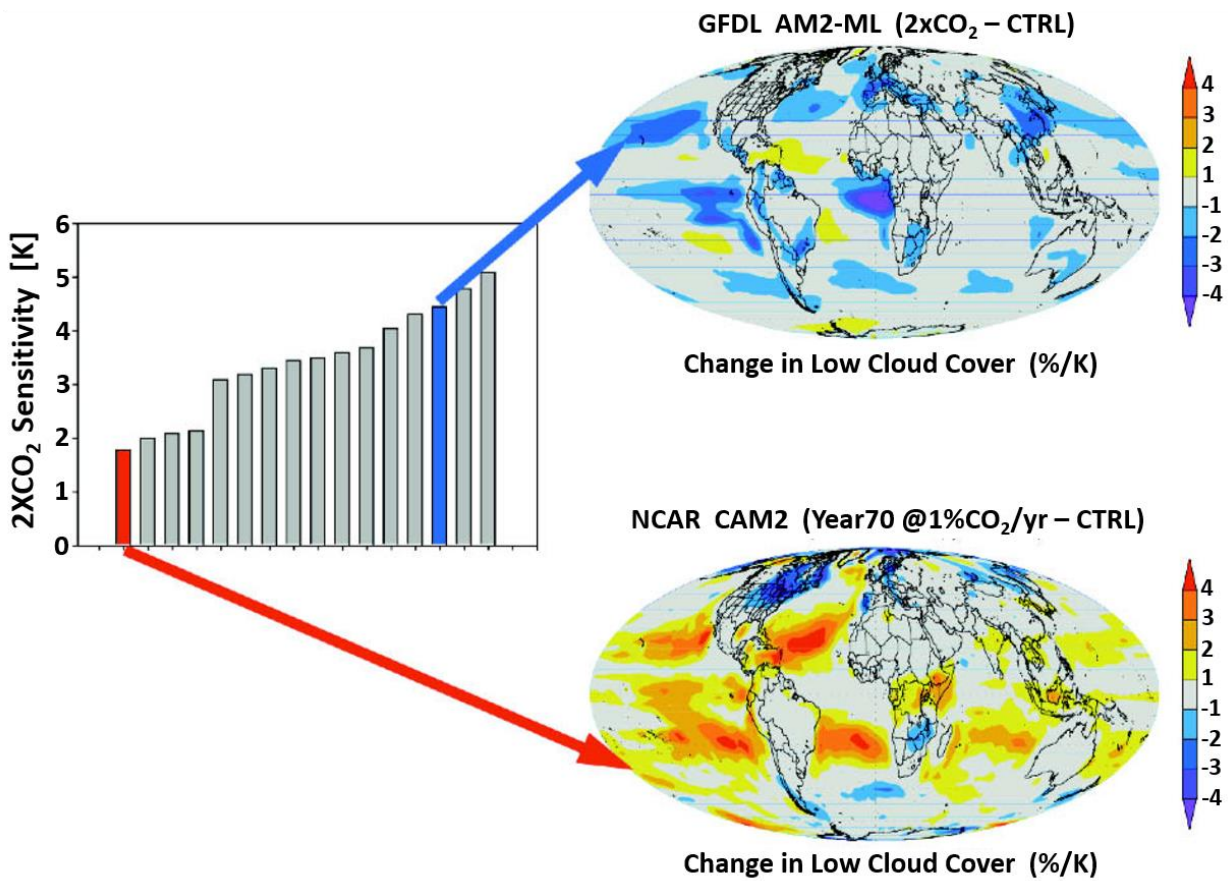
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1554 Fig. 9 Diurnal variations in (top) liquid water path and (bottom) cloud-top and cloud-base  
 1555 heights observed off the coast of California in FIRE (First ISCCP Regional Experiment)  
 1556 during July 1987 (fig. 2 and fig. 4 in Blaskovic et al. 1991). © American Meteorological  
 1557 Society. Used with permission.

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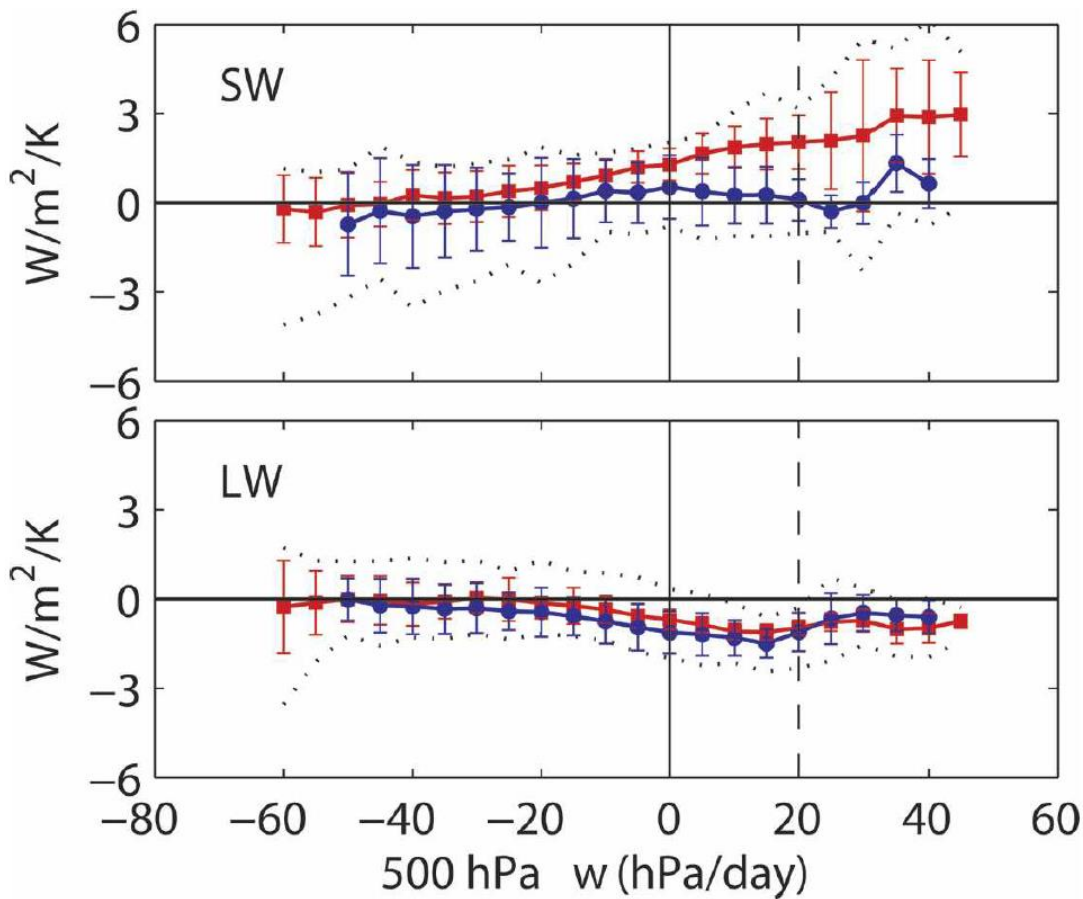
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1562 Fig. 10 (left) Surface warming estimates in doubled CO<sub>2</sub> climates from climate models  
 1563 developed for CMIP3. Simulation data forced by a 1% yr<sup>-1</sup> increase in CO<sub>2</sub> are used.  
 1564 Shown is the difference of the 20-yr average of the simulation with present (1961–80)  
 1565 and increasing CO<sub>2</sub> (corresponding broadly to a time of doubled CO<sub>2</sub> concentrations).  
 1566 (right) The changes in low cloud cover averaged over this same period for two models  
 1567 that fall on either end of the projected warming range (modified after fig. 1 in Stephens  
 1568 2005). © American Meteorological Society. Used with permission.

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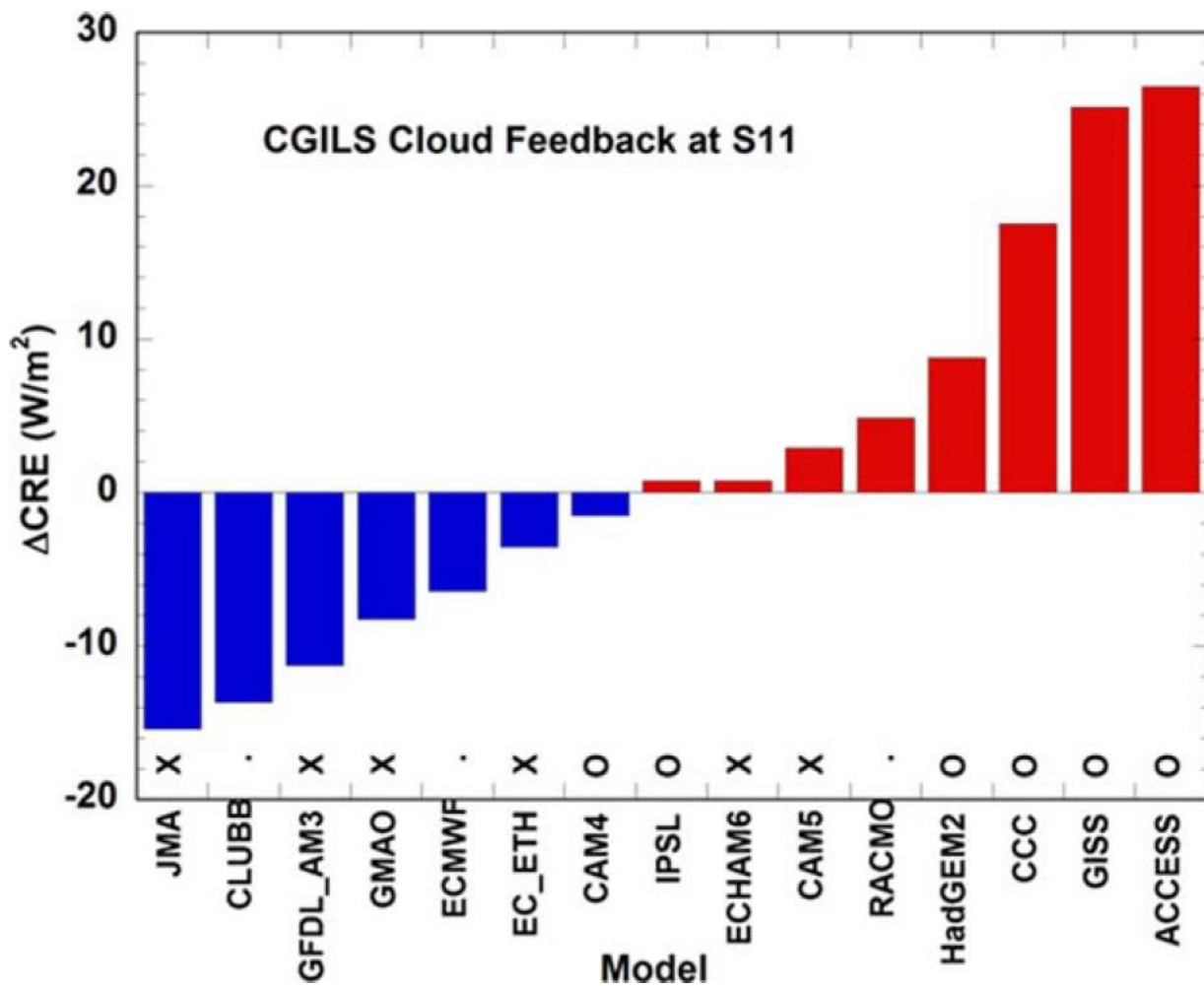
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1573 Fig. 11 Sensitivity ( $\text{W m}^{-2} \text{K}^{-1}$ ) of the tropical ( $30^{\circ}\text{S}$ – $30^{\circ}\text{N}$ ) shortwave and longwave cloud  
 1574 radiative effect to changes in SST associated with climate change (in a scenario in which  
 1575 the  $\text{CO}_2$  increases by  $1\% \text{ yr}^{-1}$ ) derived from 15 coupled ocean–atmosphere GCMs  
 1576 participating in the AR4. The sensitivity is computed for different large-scale atmospheric  
 1577 circulation regimes (the 500-hPa large-scale vertical pressure velocity is used as a proxy  
 1578 for large-scale motion). Results are presented for two groups of GCMs: models that  
 1579 predict a positive anomaly in the tropically averaged net cloud radiative effect in climate  
 1580 change (red; eight models) and models that predict a negative anomaly (blue; seven  
 1581 models) (fig. 9 in Bony et al. 2006, after Bony and Dufresne 2005). © American  
 1582 Geophysical Union.

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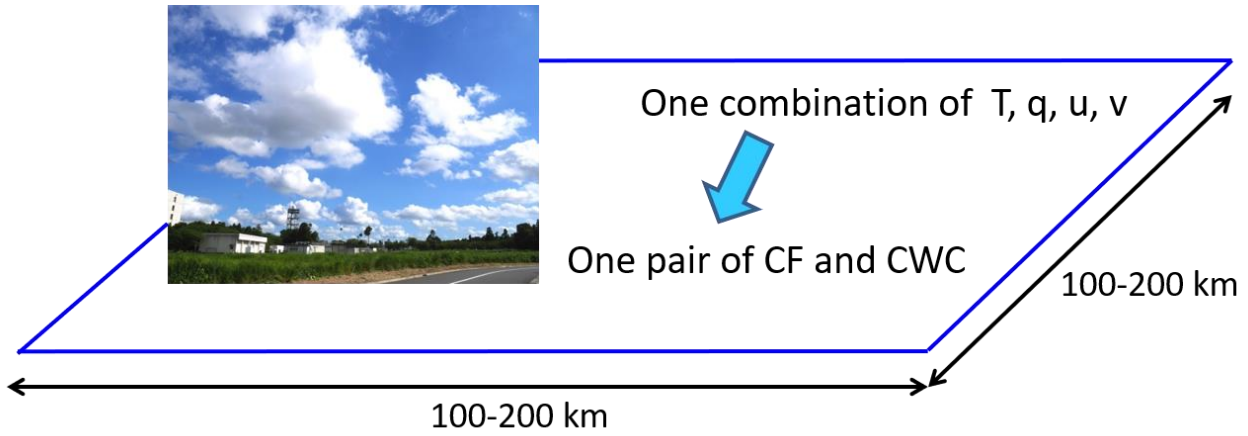
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1587 Fig. 12 Change in cloud radiative effect (CRE,  $W\ m^{-2}$ ) in SCMs for stratocumulus (at  
 1588 location S11 in CGILS:  $32^{\circ}N$ ,  $129^{\circ}W$ ) corresponding to a 2 K SST perturbation. The 'X'  
 1589 above a model name indicates that the shallow convection scheme is not active; 'O'  
 1590 indicates that the shallow convection scheme is active. Models without these characters  
 1591 either do not separately parameterize shallow convection and atmospheric boundary  
 1592 layer turbulence, or do not submit results with information on convection (fig. 7 in Zhang  
 1593 et al. 2013). © American Geophysical Union.

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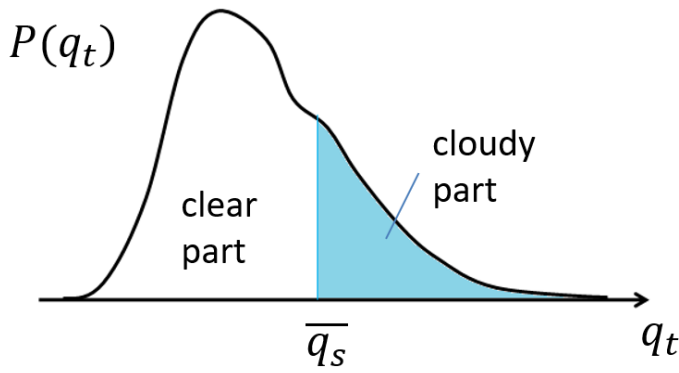
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1598 Fig. 13 Schematic of a GCM grid surrounding a photograph of real clouds. One pair of  
 1599 cloud fraction (CF) and cloud water content (CWC) values is determined from a  
 1600 combination of prognostic variables in the GCM; e.g., temperature ( $T$ ), humidity ( $q$ ), and  
 1601 wind ( $u, v$ ), which do not have subgrid fluctuation information. The photograph of the  
 1602 clouds was taken in Tsukuba on July 24, 2016 (courtesy of Osamu Arakawa).

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$$A = \int_{\bar{q}_s}^{\infty} P(q_t) dq_t$$

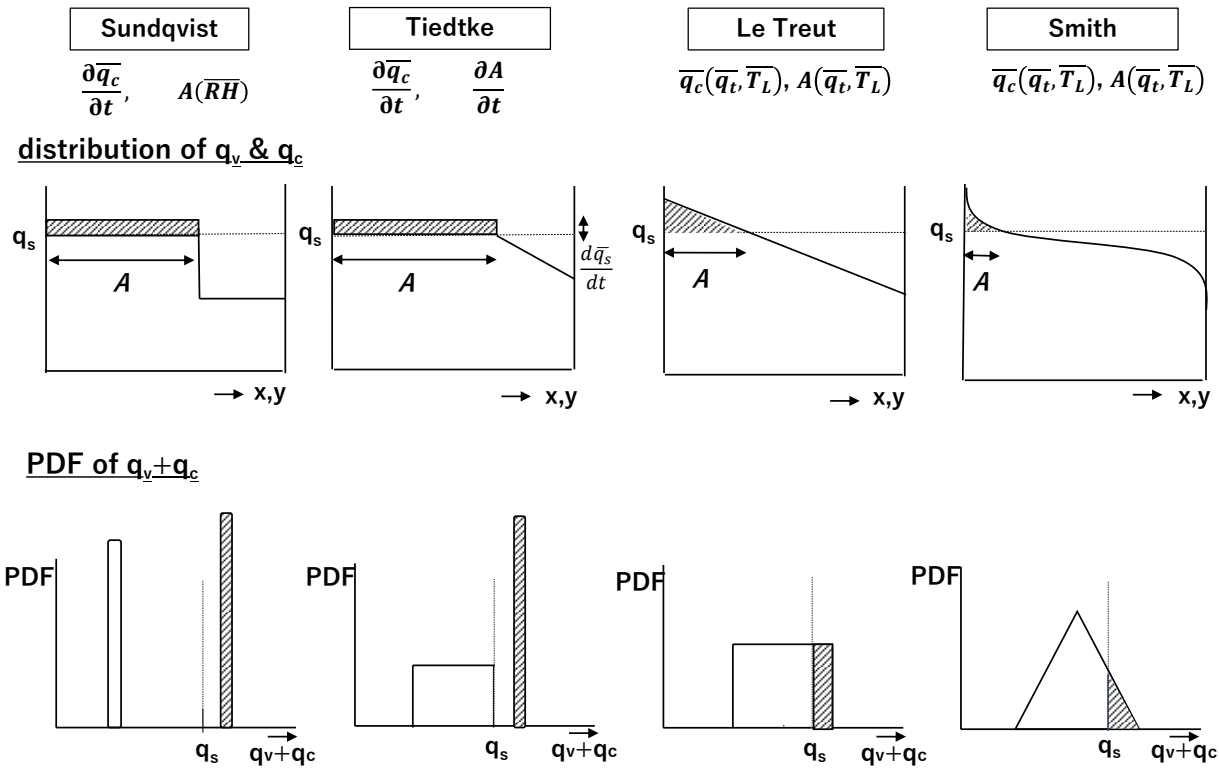
$$\bar{q}_c = \int_{\bar{q}_s}^{\infty} (q_t - \bar{q}_s) P(q_t) dq_t$$

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1606

1607 Fig. 14 Schematic of PDF-based cloud schemes.  $P$  is the probability density function of  
 1608 the total water content, normalized to 1. Cloud fraction and cloud water content are  
 1609 calculated using the equations to the right. Overbars denote the spatial average in each  
 1610 model grid box.

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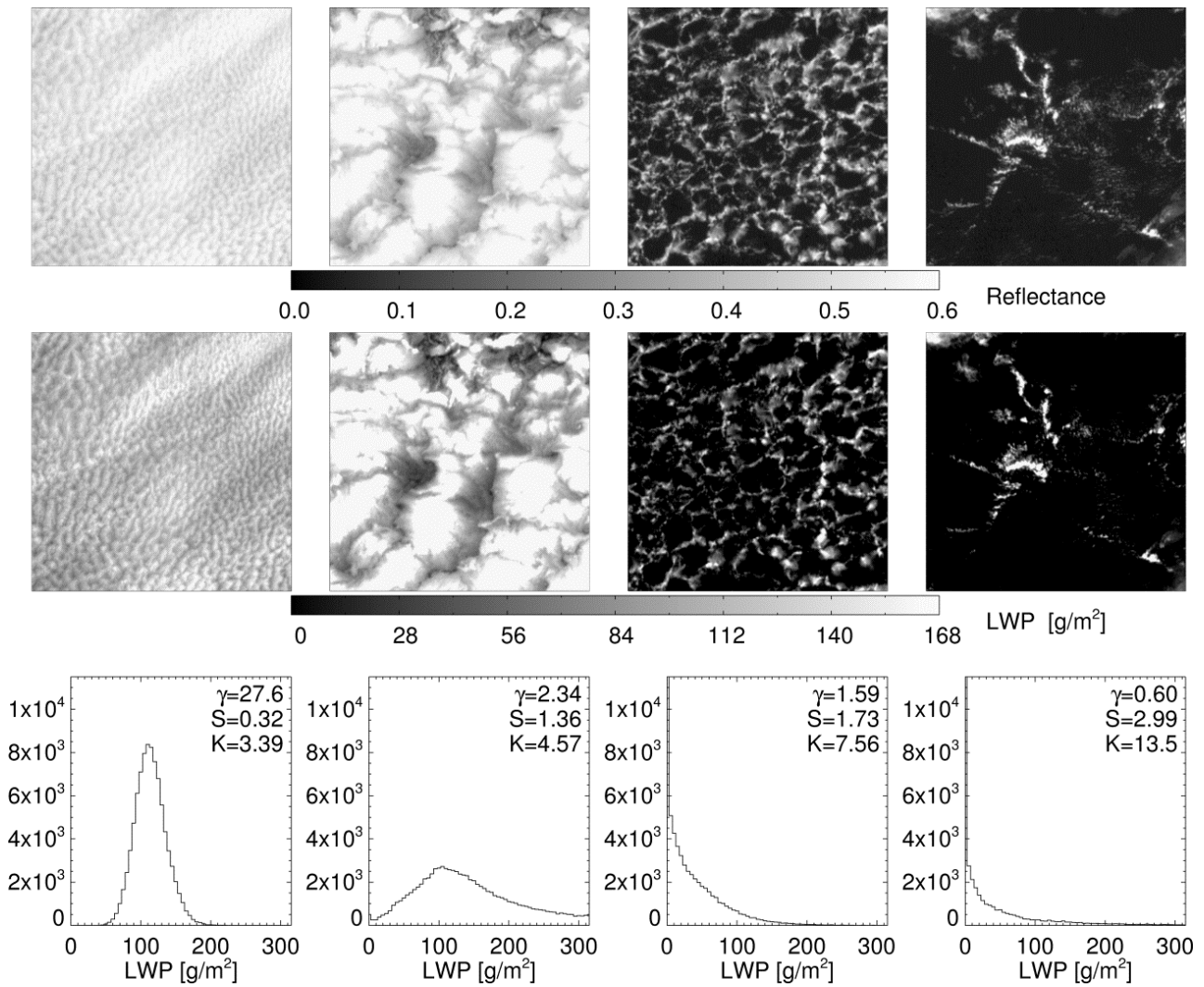
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1614 Fig. 15 (Top panels) Distributions of specific humidity and cloud water content in a grid  
 1615 box for various cloud schemes. Hatching corresponds to cloud water content. (Bottom  
 1616 panels) The corresponding probability density functions of the total water content  
 1617 (specific humidity + cloud water content). Hatching denotes cloudy parts and the area of  
 1618 hatching corresponds to cloud fraction.

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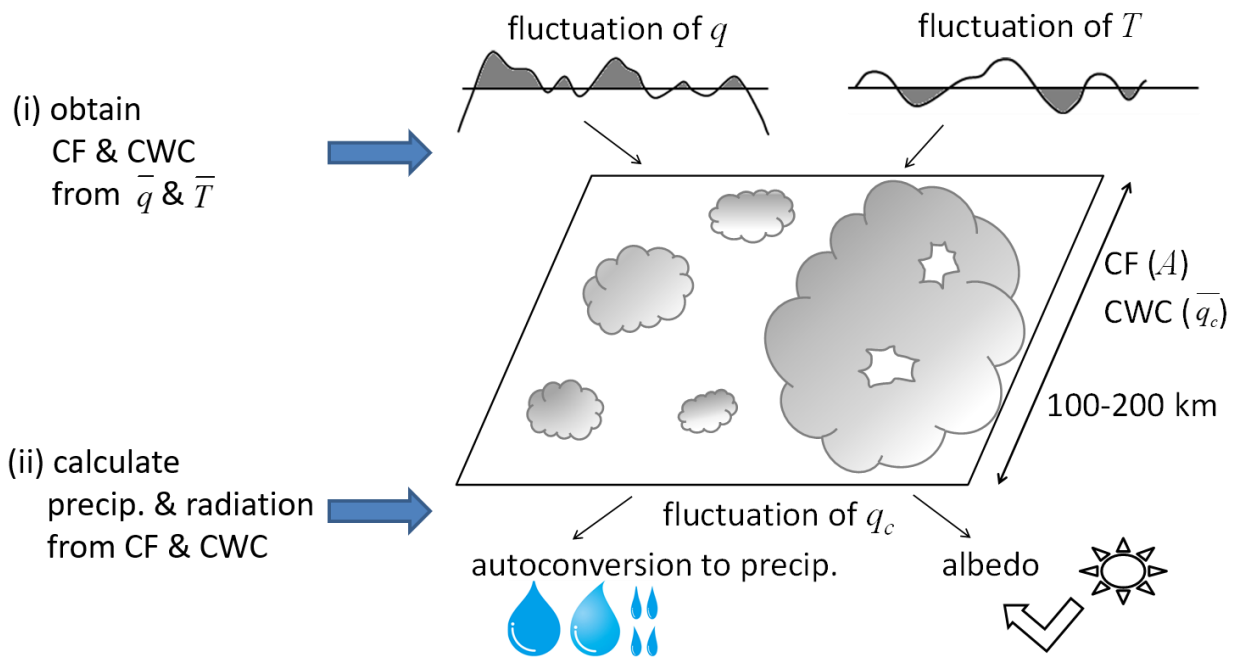
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Fig. 16 Examples of images, from distinct cloud regimes, of (top) reflectance, (middle) LWP ( $\text{g m}^{-2}$ ), and (bottom) PDFs of LWP. The areas correspond to  $200 \text{ km} \times 200 \text{ km}$  and the reflectance is calculated from Geostationary Operations Environmental Satellite (GOES) visible data. Values of homogeneity ( $\gamma$ ), skewness ( $S$ ), and kurtosis ( $K$ ) for each PDF are indicated in lower panels. Fig. 3 in Kawai and Teixeira 2010. © American Meteorological Society. Used with permission.

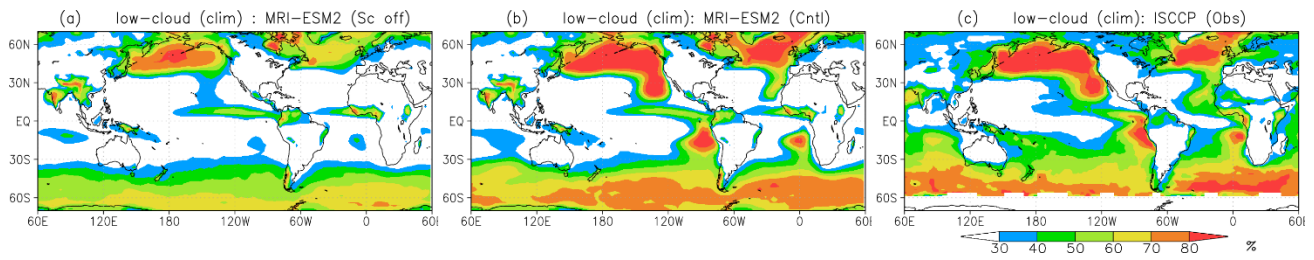


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1633 Fig. 17 Schematic of two steps that require subgrid PDF information related to cloud  
 1634 schemes for atmospheric model calculations. The first step is to determine a pair of cloud  
 1635 fraction and cloud water content values from humidity and temperature. The second step  
 1636 is to calculate the autoconversion rate of cloud water to precipitation in the moist  
 1637 processes and albedo in the radiation processes, from cloud fraction and cloud water  
 1638 content. These are affected by the inhomogeneity of cloud water content in the model  
 1639 grid box.

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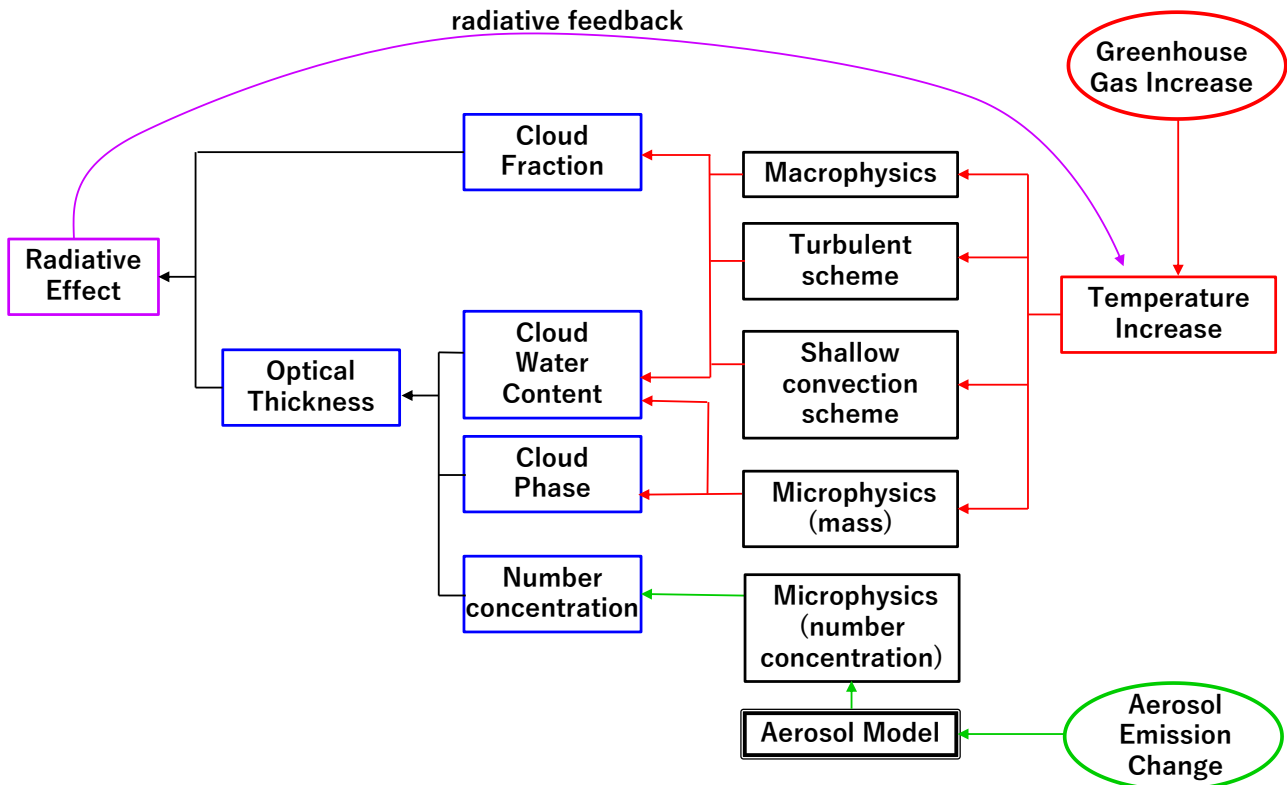
1642

1643 Fig. 18 Low cloud cover (below 680 hPa) in July in units of [%]. Output from the  
 1644 atmospheric model of MRI-ESM2 for 2000–2014 under given SST: (a) a version with the  
 1645 stratocumulus scheme off and (b) a control version. (c) ISCCP observational data for  
 1646 1986–2005 where the low cloud cover is corrected under an assumption of random cloud  
 1647 overlap.

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# Low Cloud Change and the Feedback in GCMs



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1652 Fig. 19 Schematic diagram of low cloud changes and related physical processes in GCMs

1653 in climate simulations. Ovals show forcing given in climate simulations. Cloud properties

1654 (blue boxes) that are affected by the forcing and physical processes (black boxes) that

1655 mainly affect the cloud properties are shown. The connections between boxes are major

1656 routes, although there are other minor relationships between them. Red lines show

1657 changes or effects related to greenhouse gas forcing and green lines to aerosol emission

1658 forcing.

1659

1660

1661 Table 1 List of major field campaigns associated with MLCs. Sc denotes stratocumulus  
 1662 and Cu denotes cumulus. Abbreviations are as follows: BOMEX (the Barbados  
 1663 Oceanographic and Meteorological Experiment), DYCOMS-II (the Second Dynamics and  
 1664 Chemistry of Marine Stratocumulus), and RICO (the Rain in Cumulus over the Ocean).  
 1665 See text for other abbreviations.

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<b>Field campaigns</b>	<b>Year</b>	<b>Area</b>	<b>Main target</b>	<b>Reference</b>
BOMEX	May-Jul 1969	Trop. Atlantic	Cu	Davidson (1968)
FIRE	Jun & Jul 1987	off California	Sc	Albrecht et al. (1988)
ASTEX	Jun 1992	NE Atlantic	Sc & Cu	Albrecht et al. (1995)
DYCOMS-II	Jul 2001	off California	Sc	Stevens et al. (2003)
EPIC	Sep & Oct 2001	off Peru	Sc	Bretherton et al. (2004b)
RICO	Nov 2004-Jan 2005	Trop. Atlantic	Cu	Rauber et al. (2007)
VOCALS-REx	Oct & Nov 2008	off Peru	Sc	Wood et al. (2011)
EUREC <sup>4</sup> A	Jan & Feb 2020	Trop. Atlantic	Cu	Bony et al. (2017)

1668 Table 2 List of experiments using atmospheric components of climate models in CMIP5.  
 1669 Strings of letters show the names of experiments commonly used in the project. The sign  
 1670 ‘-’ denotes experiments not proposed. The name ‘aqua’ denotes an aqua planet  
 1671 experiment, where zonally uniform SST is given for an ocean-covered earth. The name  
 1672 ‘sstClim’ denotes an experiment where SST climatology of pre-industrial control and  
 1673 preindustrial aerosols including sulfate are given. The CO<sub>2</sub> concentration is not changed  
 1674 for SST+4K experiments (both uniform and patterned SST perturbation), and SST is not  
 1675 changed for quadrupled CO<sub>2</sub> experiments.  
 1676

<b>Basic experim.</b>	<b>SST+4K uniform</b>	<b>SST+4K patterned</b>	<b>Quadrupled CO2</b>	<b>All aerosols of year 2000</b>	<b>Only sulfate of year 2000</b>
amip	amip4K	amipFuture	amip4xCO2	–	–
aqua	aqua4K	–	aqua4xCO2	–	–
sstClim	–	–	sstClim4xCO2	sstClimAerosol	sstClimSulfate