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1 **The influences of Monsoon Trough on the relative motion of**  
2 **binary tropical cyclones**

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26

27 **Abstract**

28 In this study, the effect of the zonally-elongating monsoon trough (MT) on the binary  
29 tropical-cyclones (TCs) interaction is investigated by using data analysis and idealized  
30 simulations. The binary-TCs interaction is found to be sensitive to the relative  
31 orientation of the two TCs embedded in the MT. When the two cyclones are lined up  
32 in a northeast-southwest (NE-SW) orientation, the MT steers the two cyclones to  
33 approach each other and promotes the Fujiwhara effect. In contrast, when the initial  
34 cyclones are orientated in the northwest-southeast (NW-SE) direction of the MT, they  
35 will move away from each other under the large-scale steering flows.

36 Idealized simulations are conducted to understand how the MT and the  $\beta$ -effect  
37 influence the binary TC interactions, focusing on NE-SW oriented pairs. The steering  
38 flows at different stages are examined by partitioning them into the one from the MT  
39 and the other cyclone in the pair. The analysis shows that the binary TCs' motions are  
40 mainly controlled by the large-scale steering flows in the initial stage. In the case of  
41 binary TCs with a NE-SW orientation, the MT can promote two TCs to approach each  
42 other, thus increasing the possibility of binary interactions.

43 The sensitivity of the binary TCs interaction to their intensities, the strength of the  
44 MT, and the  $\beta$ -effect are examined. The stronger the MT, the stronger its large-scale  
45 steering flows will be, thus making the two NE-SW oriented TCs merge faster.  
46 Furthermore, the binary interaction is stronger on the  $\beta$ -plane compared to  $f$ -plane. It  
47 is likely due to the  $\beta$ -induced Rossby wave energy dispersion. As the MT evolves into  
48 a monsoon gyre (MG) -like pattern, a pronounced southwesterly flow emanates in the  
49 southeast quadrant of MG. This southwesterly flow acts as a steering flow to help the  
50 western TC (TCW) move northeastward, by which accelerates to reach the critical  
51 distance.

52  
53 **Keywords:** Monsoon trough; Fujiwhara effect; Binary Tropical Cyclones

## 55 **1. Introduction**

56 The ‘Fujiwhara effect’ (also identified as the Fujiwhara interaction or a binary  
57 interaction) refers to the interaction of two or more cyclones, including mutual rotating,  
58 approaching, and merging (Fujiwhara 1921, 1923; Lander and Holland 1993). When  
59 two cyclonic vortices at a reasonably close distance experience a Fujiwhara interaction,  
60 they can be called the binary tropical cyclones (BTCs, Ren et al. 2020). Numerous  
61 modeling and observational studies have been conducted to investigate the interaction  
62 of BTCs. Dritschel and Waugh (1992) classified five most common Fujiwhara  
63 interactions using the idealized model: complete merger (CM), partial merger (PM),  
64 complete straining-out (CSO), partial straining-out (PSO), and elastic interaction (EI).  
65 Among them, the first two, CM and PM, are strong interactions. Based on the  
66 observations, Carr and Elsberry (1998) categorized the binary TCs interactions into  
67 direct TC interactions (DTIs), semidirect TC interactions (STIs), and indirect TC  
68 interactions (ITIs).

69 Some studies have focused on possible factors affecting the Fujiwhara interactions.  
70 Observational evidence by Brand (1970) suggested that two TCs interact when their  
71 initial separation distance is within 1400 km in the Western North Pacific (WNP). When  
72 the distance is less than 750 km, two TCs will attract to each other. Wang et al. (1989,  
73 1992a, 1992b) found that the relative motion of the binary vortices is sensitive to their  
74 initial spacing and relative intensity. They also confirmed the existence of the critical  
75 separation distance (CSD) for the Fujiwhara interaction. The CSD is used to determine  
76 the BTCs (DeMaria and Chan 1984; Ritchie and Holland 1993; Wang and Holland

77 1995). Ren et al. (2020) used the CSD to establish an objective definition of binary TCs,  
78 and explore typical BTCs interaction. Within the CSD, BTCs have multiple  
79 manifestations, including merging. However, different CSDs were obtained in different  
80 model frameworks. For example, Ritchie and Holland (1993) found that, in a barotropic  
81 model, the initial separation distance between two TCs must be less than 300 km in  
82 order for them to merge. Also using a baroclinic model, Wang and Holland (1995)  
83 showed that the two vortices separated by less than 450 km are likely to merge. These  
84 previous studies focused on the binary interaction in the absence of environmental  
85 flows. In a real world, the behavior of multiple tropical cyclones is more complicated  
86 due to the wide range of scales involved in the environmental flow. Dong (1980) found  
87 that the anticlockwise mutual rotation of two TCs in the cyclonic environmental fields  
88 is largely influenced by the environmental flow through analyzing real cases. Hart and  
89 Evans (1999) also found that the cyclonic mutual rotation of two TCs accelerates when  
90 they are embedded in an environment with large-scale cyclonic vorticity. Kuo et al.  
91 (2004) identified the role of vorticity strength ratio and vorticity radius ratios between  
92 two TCs on the merger and formation of concentric vorticity.

93 Globally, the WNP basin has the highest frequency of TC formations, and thus  
94 multiple TCs often co-exist therein. In the summertime, the monsoon trough (MT)  
95 serves as the most prominent large-scale system in the WNP. It manifests itself as the  
96 near-equatorial confluence or the shear zone between the lower-level westerly monsoon  
97 and easterly trade winds (Briegel and Frank 1997; Holland 1995; Lander 1996; Chan  
98 and Evans 2002). The observations indicate that typhoons Noru and Kulap in 2017,

99 which are oriented in NE-SW direction embedded in the MT, interacted and merged at  
100 the initial distance of 1800 km. However, two TCs Noul and Dolphin in 2015, which  
101 are located in the MT with a NW-SE orientation and distance of 1500 km, did not merge.  
102 The observational analysis presented in the next section will illustrate that there are  
103 distinct behaviors of two TCs within the MT. The two TCs in the MT can exhibit various  
104 types of Fujiwhara effects depending on the relative strength of two TCs, their  
105 characteristics in the MT, and the intensity of the MT. A better understanding of such  
106 occurrences could help to improve the perspective of TC track forecasts. This motivates  
107 us for this study. As our focus is to investigate strong Fujiwhara interactions, the CSD  
108 mentioned above refers to the threshold distance beyond which strong Fujiwhara  
109 interactions, such as PM and CM, occur.

110 This paper is organized as follows: Section 2 presents the characteristics of the two  
111 real cases in the observations, a pair of two typhoons Noru and Kulap in 2017 and Noul  
112 and Dolphin in 2015. Section 3 describes the model configuration of idealized  
113 simulations and experimental design. The simulated results for binary TCs in two  
114 different environmental characteristics and possible mechanisms involved are  
115 discussed in sections 4 and 5, respectively. A summary of the study is presented in  
116 section 6.

## 117 **2. Analysis of two cases with binary TCs**

118 Two distinctively different binary TCs behaviors within the MT region are presented.  
119 Scenarios of typhoons Noul and Dolphin in 2015, and Noru and Kulap in 2017 that are  
120 oriented in different directions embedded in the MT are selected to illustrate different

121 impacts of the MT on the interactions between the two cyclones. The TC data are  
122 obtained from the best track dataset at the Japan Meteorological Agency (JMA). The  
123 global reanalysis representing the environmental flows is from the National Centers for  
124 Environmental Prediction (NCEP) global final analyses (FNL) data (NCEP 2000). The  
125 horizontal resolution of the reanalysis data is  $1.0^{\circ} \times 1.0^{\circ}$  with a 6-hourly time interval.

126 Typhoon Noru and Kulap were embedded in the MG with a NE-SW orientation (Fig.  
127 1c). Figures 1a and 1b present the 12-hourly track positions of the two storms and their  
128 relative positions. At 00 UTC 23 July, the separation distance is about 1800 km. From  
129 this point, Kulap moved westward while Noru moved southeastward. As the two TCs  
130 approached each other, they started rotating anticlockwise around each other (Fig. 1a  
131 and 1b). Kulap weakened as it approached Noru, and their mutual rotation speed started  
132 slowing. The two vortices partially merged on 28 July (Fig. 1d).

133 In contrast, Noul and Dolphin were located in the MT with a NW-SE orientation on  
134 May 4, 2015 (Fig. 2c). Note that since the track record of Dolphin from JMA started on  
135 12 UTC 6 May, the track before that was based on the reanalysis data. The two typhoons'  
136 initial separation distance is about 1500 km (Fig. 2c). Dolphin moved southeastward  
137 under the westerly flows from the south side of the MT and then turned northward on  
138 8 May (Fig. 2a). Noul basically maintained its northwestward movement under the  
139 easterly flows from the northern flank of the MT. The distance between the two TCs  
140 keeps getting larger and there is no rotation between them (Fig. 2b, 2d).

141 It has been well realized that TC motion is influenced by large-scale environmental  
142 steering flows, the  $\beta$ -drift, and possibly the circulation of a neighboring TC. A Tukey

143 window spatial low-pass filtering will be used to separate the environmental flow from  
144 the TC-scale circulation (Hendricks et al. 2011; Ge et al. 2013, 2018; Xu et al. 2016;  
145 Dong and Neumann 1983). Systems with a wavelength greater than 1000 km are treated  
146 as the environmental fields, and those with a wavelength less than 1000 km are  
147 considered as the TC-scale system for the storm. It is worthwhile mentioning that  
148 different separating wavelengths have been tested, and the results are similar for the  
149 separation wavelength ranging from 500 to 1000 km.

150 After the separation of spatial scales, the steering flows from the MT and TCs are  
151 obtained by averaging the wind over an area within a radius of 400 km centered at the  
152 storm. For different intensities of TCs, different vertical layers have been used for a  
153 vertical average to better represent the steering flows instead of using a single-level  
154 field (Wu et al. 2011; Dong and Neumann 1983). Among the two selected real cases,  
155 Noul and Noru were the stronger ones within their own pairs. In the Noul-Dolphin pair,  
156 Noul's central minimum sea-level pressure (CMSLP) decreased from 1006 hPa to 935  
157 hPa during the period of interest, while Noru in the Noru-Kulap pair decreased from  
158 985 hPa to 970 hPa and then weakened to 975 hPa. Typhoon Dolphin and Kulap were  
159 weaker in their respective pairs, with Dolphin's intensity strengthening from 1007 hPa  
160 to 998 hPa during the period, while Kulap's intensity remained roughly unchanged at  
161 around 1002 hPa. Following Wu et al. (2011), the vertical averages between 925–250  
162 hPa are selected as the steering layer for Noul and Noru, and the averages between 850–  
163 500 hPa are used as the steering layer for Dolphin and Kulap.

164 With mainly westerly and easterly flows on the south and north side of the MT, Noru



165 and Kulap with a NE-SW orientation initially have their separation distance decreasing  
166 with time (Fig. 1b). After 00 UTC 23 July, the MT evolves into a MG. The time  
167 evolutions of the steering flows at different scales for Noru and Kulap are displayed in  
168 Figs. 3a and 3b, respectively. After 00 UTC 25 July, the dual-vortex interaction  
169 gradually strengthened (Fig. 1b). Specifically, the zonal component ( $C_x$ ) of Noru's  
170 movement conformed well with the large-scale steering flows before 18 UTC 25 July  
171 (Fig. 3a). Hereafter, Noru's  $C_x$  turned from positive to negative, and the deviation of  
172 it from  $C_{xL}$  increased. The difference between  $C_x$  and  $C_{xL}$  for Kulap, the weak  
173 cyclone of the pair, was large throughout. The meridional movement speed ( $C_y$ ) for  
174 both Noru and Kulap is different from the large-scale steering flow ( $C_{yL}$ ), especially  
175 after 12 UTC on 24 July, with Noru deviating to the north and Kulap to the south, and  
176 the difference reaches about 2–3  $\text{m s}^{-1}$ . The difference between  $C_x$  and  $C_{xL}$  of Kulap  
177 remains about 2  $\text{m s}^{-1}$  after 00 UTC 27 July, when Kulap moves westward and  
178 merges with the eastward-moving Noru. Overall, the MT steering cannot fully explain  
179 the storms' movement for this case. The underlying processes that account for the  
180 discrepancy of movement speed may come from the strong mutual interactions between  
181 the two TCs and the idealized simulations will investigate it.

182 For the case of Noul and Dolphin, which had a NW-SE orientation, the moving speed  
183 of the weaker Dolphin in general conformed with the environmental MT flow (Fig. 4).  
184 Noul maintained a westward movement, and Dolphin kept eastward under the mainly  
185 zonal large-scale steering flow. The  $C_{yL}$  of Noul and Dolphin remained nearly 0  
186  $\text{m s}^{-1}$  from 00 UTC 4 May to 18 UTC 7 May. The largest difference between the TC

187 movement and the environmental MT steering is with the zonal component of Noul for  
188 about 1–2 m s<sup>-1</sup>. The rather unique locations of the two storms allow the MT to push  
189 the two systems away from each other with no interactions between them.

190 The above results suggest that for a nearly east-west trough, when the two TCs are  
191 embedded in the MT at a certain orientation, their future motions can be very different  
192 as influenced by the MT steering forces. Ideal numerical experiments will be conducted  
193 to understand the influence of MT on the binary TCs interaction with different  
194 orientations.

### 195 **3. Model and experimental designs**

196 In this study, the Advanced Research version of the Weather Research and  
197 Forecasting model (WRF-ARW) is used for the idealized numerical experiments. The  
198 simulations use a single domain without nesting with a horizontal resolution of 18 km,  
199 and 55 levels in the vertical. The domain covers 6 °S – 33 °N, 118.5 °E – 179.5 °W.  
200 The periodic boundary conditions are applied in the east-west direction, and open  
201 boundary conditions are applied in the north-south boundary. The selected physics  
202 parameterizations are the WRF Single-Moment 6-class (WSM6; Hong et al. 2010)  
203 microphysics scheme, the Dudhia (1989) shortwave radiation scheme, the Rapid  
204 Radiative Transfer Model (RRTM; Mlawer et al. 1997) longwave radiation scheme, the  
205 Yonsei University planetary boundary layer (PBL) scheme (Hong et al. 2006) and the  
206 Kain-Fritsch cumulus parameterization scheme (Kain and Fritsch 1992). In this study,  
207 for those  $\beta$ -plane runs, the  $\beta$  value is set to  $2.21 \times 10^{-11} \text{ m}^{-1} \text{ s}^{-1}$ , which corresponds  
208 to the center latitude (i.e., 15°N).

209 Based on the analysis presented in Section 2, eleven sets of numerical experiments  
 210 are designed to reveal possible roles of the MT and the initial characteristics of the two  
 211 TCs on the TC interactions (Table 1). The MT over the WNP features low-latitude  
 212 cyclonic shear vorticity. In this study, the MT is defined as the shear zone between an  
 213 easterly and a westerly between 5°–25°N centered at around 15°N (Guinn and Schubert  
 214 1993; Ferreira and Schubert 1997). The MT has a baroclinic structure with a transition  
 215 at 400 hPa to an anticyclonic shear above. The horizontal distribution and vertical  
 216 structure of the idealized MT are given in Fig. 5. The zonal wind profile of the initial  
 217 MT is established as:

$$U(y) = -U_{m0} \cdot \left[ \frac{y - y_0}{y_m} \cdot e^{0.5 \left[ 1 - \left( \frac{y - y_0}{y_m} \right)^2 \right]} \cdot \sin \left( \frac{\pi}{2} \cdot \frac{\sigma - 0.4}{1 - 0.4} \right) \right] \quad (1)$$

218 where  $U(y)$  represents the zonal wind,  $U_{m0}$  is the maximum zonal wind,  $y$  is the  
 219 meridional distances,  $y_0$  represents the initial MT center,  $y_m$  indicates the half-width,  
 220 which is taken as 900 km;  $\sigma$  is the model sigma level.

221 The initial TC wind speed is maximum at low level, decreases gradually with height,  
 222 and vanishes at 100 hPa. That is, the tangential wind profile of initial TC is given by  
 223 Equation (2):

$$V_t = \begin{cases} V_{\max} \cdot \left[ \frac{r^2}{r_m^2} \cdot e^{\frac{1-r}{r_m}} \cdot \sin \left( \frac{\pi}{2} \cdot \frac{\sigma - 0.1}{1 - 0.1} \right) \right] & , r \leq r_m \\ V_{\max} \cdot \left[ \frac{r}{r_m} \cdot e^{\frac{1-r}{r_m}} - \frac{|r - r_m|}{r_0 - r_m} \cdot e^{\frac{1-r_0}{r_m}} \right] \cdot \sin \left( \frac{\pi}{2} \cdot \frac{\sigma - 0.1}{1 - 0.1} \right) & , r > r_m \end{cases} \quad (2)$$

224 where  $V_t$  is tangential wind,  $r$  is the radius,  $V_{\max}$  is maximum tangential wind,  $r_m$   
 225 is the radius of  $V_{\max}$ , and  $r_0$  represents the radius of tangential wind vanished. For  
 226 TC,  $r_m$  and  $r_0$  are 100 km, 1500 km respectively in idealized experiments.

227 Since the interaction between the two NE-SW oriented TCs in the MT presents a  
228 more interesting scenario, as shown by the example in Fig. 1, it is this study's main  
229 focus. In the control experiment “NE-CTL”, two idealized TC-like vortices are  
230 embedded in the zonally oriented MT with a NE-SW orientation at the initial time. The  
231 two vortices are specified with different initial intensities. The strong one has a  
232 maximum wind speed ( $V_{max}$ ) of  $30 \text{ m s}^{-1}$  and the weak storm of  $10 \text{ m s}^{-1}$ , both at a  
233 radius of 100 km. Given the specified two vortices, the CSD is 1111.3 km according to  
234 the Liou-Liu empirical formula (Liou et al. 2016). The initial distance between the two  
235 vortices is therefore set to 1200 km, which is unfavorable to their interactions. To  
236 investigate the role of the MT on Fujiwhara interaction, the monsoon trough is excluded  
237 in the experiment “NE-NMT”. In the third experiment “NE-WMT”, the strength of the  
238 MT is reduced by 20%. To further explore the effect of the relative strength of the initial  
239 vortices on the BTCs interaction, experiments “NE-SVI” and “NE-LVI” are set up with  
240 the same separation distance of the two TCs as in the NE-CTL but with different relative  
241 intensities (Table 1). Here “SVI” (LVI) is the abbreviation for the same (low) vortex  
242 intensity ratio. It should be noted that the relative intensity is defined as the ratio of the  
243 initial maximum wind speed of the western vortex to the eastern one.

244 In experiments “NW-CTL”, “NW-SVI”, and “NW-LVI”, the two TC vortices are  
245 initially positioned in a NW-SE orientation embedded in the MT, representing the  
246 characteristics of the Noul-Dolphin couplets (Fig. 2). The three experiments carry the  
247 same intensities for the two TCs as in NE-CTL, NE-SVI, and NE-LVI. For brevity, the  
248 vortex initially located on the west side is identified as TCW, and the one on the east

249 side is TCE in this study. In addition, a set of  $f$ -plane experiments are conducted for  
250 different relative intensities and relative positions of two TCs to investigate the  $\beta$ -  
251 effect on binary interactions. Three additional sets of NW-SE experiments are  
252 conducted, in which the idealized MT is centered around  $7^\circ\text{N}$  that is closer to the Noul-  
253 Dolphin case (Fig. 2). These experiments have similar results to those in which the  
254 MT's center is placed at  $15^\circ\text{N}$  (Figure not shown).

## 255 **4 Binary TCs with northeast-southwest orientation**

### 256 *4.1 The role of the monsoon trough*

#### 257 *a). Simulated Results*

258 Figures 6–7 display the tracks, relative positions, and the evolution characteristics of  
259 the two TCs in NE-CTL, NE-NMT, and NE-WMT. In NE-CTL, the two vortices are  
260 initially located on either side of the MT within a NE-SW orientation. Due to the  
261 steering of the MT circulation, TCW in the NE-CTL moves northeastward and TCE  
262 moves northwestward so that the two TCs slowly approach each other and the cyclone-  
263 cyclone interaction strengthens. Subsequently, the two vortices rotate anticlockwise  
264 around each other (Fig. 6d). It is worth mentioning that after  $t = 48$  h, the idealized  
265 zonal MT flow gradually evolves into a large cyclonic flow (Fig. 7d). By  $t = 72$  h, TCE  
266 has moved to north of TCW. Meanwhile, the distance between TCW and TCE gradually  
267 decreases, and the distortion of the vortices increases (Fig. 7g). These two storms begin  
268 to merge at around  $t = 120$  h (Fig. 7j). The MT is now a large MG, very similar to the  
269 MG in the Noru-Kulap case (Fig. 1c). In this study, when the large-scale environmental  
270 flow evolves into a sub-circular cyclonic vortex with a radius above 800 km, the MT is

271 considered to evolve into an MG (Lander 1994; Wu et al. 2013; Molinari and Vollaro  
272 2017). It should be noted that, under the idealized framework, the structure of the  
273 idealized MT is difficult to maintain in the absence of environmental weather systems  
274 (e.g., subtropical high). Dynamically, the MT region satisfies the necessary condition  
275 of barotropic instability, which leads to wave breakdown and evolves into several  
276 vortices (Guinn and Schubert 1993).

277 In contrast, the behaviors of TCW and TCE show marked differences in NE-NMT.  
278 Since there is no large-scale steering flow, the vortex pair only exhibit their individual  
279 northwestward movement under the  $\beta$ -drift effect (Fig. 6b). There is little change of  
280 the distance between TCW and TCE. Meanwhile, by testing the binary interaction in  
281 absence of MT with different initial spacings from 400–800 km, it is found that TCW  
282 and TCE will merge when they are separated by approximately less than 500 km  
283 initially. The weaker TCE deforms and merges into the spiral rainband of stronger TCW  
284 under the strong Fujiwhara effect (Figure not shown). The above results show that MT  
285 can advect the two TCs and make them close enough to occur the Fujiwhara interactions.

286 In NE-WMT with reduced MT intensity, the evolution characteristics of TCW and  
287 TCE are similar to those of NE-CTL. However, there remains a significant distance  
288 between the two vortices at the end of the integration  $t = 120$  h, as the approaching  
289 speed of the two cyclones is slower with weaker steering by the MT and the two entities  
290 miss the window of opportunity to merge together (Fig. 6f). As mentioned above, the  
291 circulation of MT is likely to facilitate the two TCs' merging, as well as the merging  
292 rate, which is sensitive to the MT strength. The merging rate is represented by the

293 relative distance between two TCs during the integration period of 120 h. The results  
294 suggest that the MT can significantly affect the Fujiwhara effect of two TCs, in  
295 agreement with previous studies (Brand 1970; Wang and Holland 1995; Wang et al.  
296 1989).

297 *b). Decomposition of steering flows at different scales*

298 As with the real cases discussed in Section 2, the MT and typhoon-scale flows can  
299 be separated using the spatial filtering method (Ge et al. 2013; Xu et al. 2016). Since  
300 the TC-scale circulation contains both TCW and TCE, we also separate out the  
301 circulation associated with each individual TC. We attempt to obtain the system-scale  
302 circulation by partitioning and reconstructing the wind field in a limited vortex core  
303 area (Zhou and Cao 2010; Cao et al. 2019). Specifically, we first extract one TC from  
304 the total fields (i.e., the TCE) with its circulation confined within a region with “0”  
305 contour in the relative vorticity. The stream function and velocity potential are then  
306 calculated based on the finite region’s vorticity and divergence. Then the associated  
307 rotational and divergent winds are obtained. Finally, the storm-scale circulation is  
308 obtained by adding the rotational and divergent flows together. By subtracting the  
309 circulation of TCE from the filtered system-scale circulation, the remaining total TC  
310 circulation is taken as the circulation of TCW. The same method can be applied to  
311 extract the TCW.

312 Separating the large-scale monsoonal flow from the storm-scale circulation of each  
313 TC can better reflect the relative significance of the BTCs interaction and the large-  
314 scale steering flow on the TC’s movement. In our idealized numerical experiments, the

315 averaged value of different steering flows from different vertical layers is selected  
316 depending on the strength of the vortex (Wu et al. 2011; Dong and Neumann 1983).  
317 The vertical average between 1–10 km is selected as the steering layer for the stronger  
318 TC, and the average of 1–6 km is obtained as the steering layer for the weaker one,  
319 respectively. At each level, the steering flows from the different scales are obtained by  
320 averaging the wind fields within a radius of 500 km centered at the storm.

321 Figure 8 presents the time series of different components of the steering flows in NE-  
322 CTL associated with MT, TCW, and TCE separately. In the early stage (i.e.,  $t = 0$ –48  
323 h), for both TCW and TCE, their movements are primarily controlled by the MT  
324 steering, since the movement speeds closely match with the components derived from  
325 the MT flow. During the next 24 hours ( $t = 48$ –72 h), the TCW is still steered by the  
326 monsoonal flow, but TCE exhibits different evolution features. For instance, the  
327 contribution from TCW for TCE starts to become significant shortly after 48 h.  
328 However, the impact of TCE on TCW is not evident until  $t = 72$  h, while the distance  
329 between TCE and TCW consistently decreases since the start (Fig. 6a, d).

330 To summarize, TCW first moves northeastward under the large-scale steering flow  
331 and then experiences a re-curvature to be northwestward around  $t = 108$  h under the  
332 combined effect of the TCE and the MT. For TCE, it is affected by the MT before 48 h,  
333 and then experiences an anticlockwise movement with combined effects from the MT  
334 and TCW. The reason that the TCE is affected by TCW earlier is due to the size  
335 differences between them so that the weaker cyclone is attracted by the stronger one  
336 quicker. The steering flows in the meridional and zonal directions display similar



337 characteristics, except that the meridional component of TCE is completely controlled  
338 by the TCW beyond 72 h (Fig. 8d) during the looping of TCE by the TCW (Fig. 6a).  
339 The overall process is similar to the merging of Noru and Kulap (Fig. 1).

340 In NE-NMT, TCW and TCE do not approach each other, and both two entities show  
341 steadily northwestward movements due to the  $\beta$ -effect (Fig. 6b, e). The study of Chan  
342 and Williams (1987) suggests that the  $\beta$ -drift is largely proportional to the TC size. As  
343 a stronger TC tends to have a larger outer size, it has a larger northwestward propagation  
344 speed than TCE. Therefore, the  $\beta$ -effect can drive clockwise rotation of two TCs  
345 relative to their midpoint. In NE-WMT (Fig. 9), the weakening of MT inevitably leads  
346 to a correspondingly smaller large-scale steering flow, slowing down the TCW and  
347 TCE's approach to each other. As a result, the time when TCW and TCE starts  
348 interacting lags behind that in NE-CTL but the overall patterns are similar between NE-  
349 CTL and NE-WMT. In NE-WMT, the contribution from TCW to TCE beyond 72h (Fig.  
350 9d) is much less than its counterpart in NE-CTL (Fig. 8d), indicating a later merger  
351 between the two cyclones.

#### 352 ***4.2 Sensitivity of relative intensity and the $\beta$ -effect***

353 The binary vortices in the first three experiments all have a NE-SW orientation and  
354 the same relative intensities of the binary TCs. Because the relative intensity of the two  
355 TCs can have a wide range in real cases, two more experiments are conducted to  
356 investigate the sensitivity of TC interactions to their relative strength. In NE-SVI, the  
357 intensities for the two TCs are the same of  $30 \text{ m s}^{-1}$  maximum wind, while in NE-LVI,  
358 the TCW and TCE have  $10 \text{ m s}^{-1}$  and  $30 \text{ m s}^{-1}$ , respectively. In both experiments, the

359 initial positions of the two TCs are the same as in NE-CTL.

360 Figure 10 presents the tracks and the relative positions of the binary TCs' center in  
361 NE-SVI and NE-LVI experiments. For better comparison, Fig. 6a and 6d for NE-CTL  
362 are also included in Fig. 10. In general, regardless of their relative intensities, the binary  
363 TCs rotate anticlockwise and approach each other under the large-scale steering flows  
364 and experience the Fujiwhara effect, and all eventually merge. In NE-SVI, the two  
365 equally strong TCs approach to each other faster than in NE-CTL and experience two  
366 looping motions (Fig. 10b, e). Meanwhile, the TCW's intensity weakens gradually, thus  
367 favoring their faster merge than in NE-CTL (Figure not shown). In NE-LVI, the  
368 stronger TCE moves northwestward during  $t = 0-24$  h. Then, after a short southward  
369 motion during  $t = 24-42$  h, it moves northwestward steadily under the MG circulation  
370 and a strong  $\beta$ -effect, while the weaker TCW moves mostly eastward in the early stage  
371 under the influence of the MG with a weaker  $\beta$ -effect and then it moves northward  
372 under the influence of TCE. The two cyclones loop around each other in the early stage  
373 and merge after 87h (Fig. 10f). Although the  $\beta$ -drift of TCE favors it to move  
374 northwestward, the weaker TCW's intensity weakens quickly, which is conducive to  
375 the stronger TCE to approach to TCW.

376 The evolution of different components of the steering flows at different scales for  
377 NE-SVI and NE-LVI are given in Fig. 11. As the two cyclones get closer, it is difficult  
378 to separate the steering components from one another, only the periods before the two  
379 vortices got closer than 370 km are shown for NE-SVI and NE-LVI. In NE-SVI, the  
380 Fujiwhara interaction starts to appear after 39 h. Because both TCW and TCE are strong

381 typhoons in this case, both of them undergo multiple turns before eventually merging.  
382 Beyond 60h, the binary TCs interaction is significant, as shown by the large  
383 contribution of the steering of one TC to the other, reflecting the interactions of the two  
384 vortices. In NE-LVI, the weaker typhoon TCW approaches TCE rapidly after 24 h as a  
385 result of the combined effect of the large-scale steering flows and different intensities  
386 of the two cyclones. Meanwhile, the stronger TCE is basically controlled by the large-  
387 scale steering flows, and the influence of TCW on it is small (Fig. 11d, h). These  
388 idealized simulations reflect many characteristics of the evolution of the Noru and  
389 Kulap, indicating that when the binary TCs are initially oriented NE-SW in the MT, the  
390 large-scale steering flows are conducive to the merger of two TCs.

391 In comparison with the evolutions of the binary vortices in NE-CTL, NE-SVI, and  
392 NE-LVI, the dual storms only partially merge in the NE-CTL, while a complete merging  
393 has occurred in NE-SVI and NE-LVI. According to the NE-NMT experiment, a  
394 clockwise (anticlockwise) mutual rotation of the two TCs occurs in NE-CTL (NE-LVI),  
395 relative to the midpoint of the two TCs. It is speculated that this clockwise rotation is  
396 ascribed to the different  $\beta$ -drift associated with the storm size. In NE-NMT, TCW has  
397 a larger outer size and thus has a larger  $\beta$ -drift. As such, it has a larger northwestward  
398 propagation speed compared to its counterpart (TCE), which likely induces the  
399 clockwise mutual rotation. Likewise, the difference in  $\beta$ -drift can account for a  
400 clockwise (anticlockwise) mutual rotation in NE-CTL (NE-LVI), relative to the  
401 midpoint of the two TCs.

402 To explore more specifically the role of the  $\beta$ -effect, the three NE-SW oriented

403 experiments with the same relative intensities as in NE-CTL, NE-SVI, and NE-LVI are  
404 conducted on the  $f$ -plane, identified with “F” in front of the experiment names (Table  
405 1), and their tracks and relative positions are given in Fig. 12. In FNE-CTL and FNE-  
406 LVI, the relative distances between two TCs are both approximately 300 km around  $t$   
407 = 120 h. Of particular interest is that the weaker TC approaches and rotates around the  
408 strong one. Thereafter, the weak TC becomes the outer spiral rain band of the strong  
409 TC (Figure not shown). In the absence of the  $\beta$ -effect, the two vortices in FNE-CTL  
410 and FNE-LVI have nearly mirroring trajectories, and their approaching speed is similar.  
411 In FNE-SVI, the lack of  $\beta$ -effect makes the TCs rotate with each other in a symmetric  
412 way with their equal intensities under the influence of MT. In summary, two TCs with  
413 large size differences are more likely to interact than those with identical sizes.

414 Furthermore, the results above indicate that the binary interaction is faster on the  $\beta$ -  
415 plane compared to  $f$ -plane. As the  $\beta$ -effect likely affects large-scale environmental  
416 flow, the evolutions of the large-scale circulation in NE-LVI and FNE-LVI are shown  
417 in Fig. 13. Previous studies (Carr and Elsberry 1995; Bi et al. 2015) have pointed out  
418 that Rossby wave energy dispersion contributes to a sudden northward track change of  
419 TC. As MT evolves into MG, a pronounced southwesterly flow emanates due to the  $\beta$ -  
420 induced energy dispersion (Ge et al. 2008). An anticyclone, therefore, develops in the  
421 southeastern flank of MG. This pattern enhances the pressure gradient and thus the  
422 southwesterly flow therein. This flow acts as a steering flow to help TCW move  
423 northeastward, which accelerates to reach the CSD (top panels in Fig. 13). With this  
424 regard, the  $\beta$ -effect can impact the approaching speed of two TCs and thus Fujiwhara

425 effect, which is in agreement with Chan and Law (1995).

## 426 **5 Binary TCs with northwest-southeast orientation**

427 In the two observational cases, both the tropical cyclone couplets Noru-Kulap and  
428 Noul-Dolphin, are located in the MT, but showed completely different tracks. This  
429 indicates that the relative position of the two storms embedded in the MT may affect  
430 their interactions (Fig.1-2).

431 Figure 14 displays the tracks, and relative positions of the two TCs in NW-CTL, NW-  
432 SVI, and NW-LVI. All the systems are embedded in the NW-SE direction in the MG,  
433 and have the same storm intensities as their counterparts in NE-CTL, NE-SVI and NE-  
434 LVI, respectively. In NW-CTL, the two TCs initially drift away from each other without  
435 a mutual rotation. Their initial relative motions are similar to the movements of Noul-  
436 Dolphin. Nevertheless, after  $t = 60$  h, the two vortices have some rotation around each  
437 other. In NW-SVI, the two TCs exhibit a more distinct mutual rotation during  $t = 0$ -  
438 69 h (Fig. 14e). Furthermore, the two vortices in NW-LVI rotate with each other during  
439 the integration period (Fig. 14f).

440 To further demonstrate these discrepancies, the evolutions characteristics of the two  
441 TCs in NW-CTL, NW-SVI, and NW-LVI are given in Fig. 15. In NW-CTL, as the TCW  
442 is stronger, a cyclonic vortex with a radius over 800 km forms near the strong TC. MT  
443 still evolves into MG through the interaction with the TCs. The southwesterly winds  
444 are strengthened on its southeast side due to the energy dispersion. This contributes to  
445 the separation of TCW and TCE (left panels in Fig. 15). In NW-SVI, since both TCW  
446 and TCE are intense TCs, the southwesterly winds on the southeast side of TCE are

447 enhanced more significantly. The enhanced southwesterly flow likely helps TCW move  
448 faster to turn northeastward, thus making the TCW and TCE exhibit mutual rotation  
449 (middle panels in Fig. 15). Similarly, as the MT evolves into MG through the interaction  
450 with the TCs, the TCW moves to the southwest after several track swings under the  
451 effect of MG in NW-LVI (right panels in Fig. 15). Once again, due to the lack of the  
452 constrain of larger circulation (e.g., subtropical high), the structure of MT cannot be  
453 maintained.

454 The evolution of each steering flow component from different scales for NW-CTL,  
455 NW-SVI, and NW-LVI are given in Figures 16-17. In these experiments, the initial two  
456 TCs depart from each other under the influence of easterly and westerly flows on either  
457 side of the MT. During the 120 h of integration, the actual speeds of TCW and TCE are  
458 in good agreement with the large-scale steering flows regardless of their relative  
459 intensities. Meanwhile, the impact of adjacent TC fluctuates around zero during the  
460 integration time in these NW-SE experiments. This indicates that the large-scale  
461 steering flows dominate the movements of TCW and TCE.

462 Overall, when the two vortices are located with a NW-SE orientation in the zonal  
463 MT, the easterly and westerly large-scale steering flows keep them away from each  
464 other, unfavorable for their merging. These findings are consistent with the similar  
465 theoretical model of Dong and Neumann (1983). Meanwhile, when the eastern TC is  
466 stronger, the  $\beta$ -effect favors more north and northwestward motion and pushes it away  
467 from the MT's westerly flow. As MT still evolves into MG through the interaction with  
468 the TCs, the southwesterly winds are strengthened on its southeast side due to the

469 energy dispersion, thus making the TCW and TCE exhibit mutual rotation.

## 470 **6 Discussion and summary**

471 The observational analysis shows that a Fujiwhara effect occurs between two  
472 typhoons Noru and Kulap (2015), which are originally located on the two sides of the  
473 MT with a NE-SW orientation, and eventually merge. Conversely, Noul and Dolphin  
474 (2017) located in the MT with a NW-SE orientation move away from each other. It is  
475 worth noting that Noru-Kulap merges eventually with an initial distance of 1800 km  
476 apart. In contrast, Noul-Dolphin, separated initially by 1500 km, did not merge. The  
477 goal of this study is to examine the influence of MT on the interactions of two TCs by  
478 utilizing ideal numerical simulations.

479 The steering from the MT and from the other co-existing cyclone are separated out  
480 and analyzed. A conceptual model of how MT affects the BTCs interactions in different  
481 configurations is given in Fig. 18. When the two vortices are distributed in a NE-SW  
482 direction in the beginning, the MT flow plays an essential role for both cyclones at the  
483 early stage. The MT's circulation pushes the two cyclones closer and promotes the  
484 cyclone-cyclone interaction. Once two vortices approach within a short distance, the  
485 impact from the nearby TC becomes more evident, and the two TCs exhibit Fujiwhara  
486 interaction (Fig. 18a). In this set up, even if the two vortices are initially far apart, they  
487 can still interact with the help of the steering from the MT. Therefore, MT can accelerate  
488 the two TCs to move closer, thus the Fujiwhara interaction.

489 In addition, the dual-vortex interaction is sensitive to the MT's strength, the relative  
490 intensity of the two TCs, and the  $\beta$ -effect. The stronger the MT, the faster the two

491 vortices approach each other and merge. Moreover, the binary interaction on the  $\beta$ -  
492 plane series is stronger than those on the  $f$ -plane. Once the MT evolves into an MG-  
493 like pattern, a pronounced southwesterly flow emanates due to the energy dispersion.  
494 This southwesterly flow acts as a steering flow to help TCW move northeastward,  
495 which accelerates to reach the CSD.

496 When the two TCs are located with a NW-SE orientation in the MT, the MT  
497 circulation pushes the two cyclones away from each other and further prevents the  
498 interactions between them (Fig. 18b). Therefore, the motion of two vortices will be  
499 controlled by the large-scale steering flows throughout. In such a configuration, the  
500 greater the relative intensity of the two storms, the faster they separate from each other.

501 In this study, the simulations are idealized. In reality, the MT structure is more  
502 complicated also. This implies that the binary TCs' development may highly depend on  
503 the morphology of the MT and TC structure. These issues need to be further addressed  
504 in future studies.

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509 ***Data availability statement.*** The datasets generated and/or analyzed in this study are  
510 available from the corresponding author on reasonable request.

511



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## List of Tables

667 **Table 1.** Summary of the idealized experiments.

668

**Table 1.** Summary of the idealized experiments.

Experiment	Monsoon trough	The $V_{max}$ of western vortex (m/s)	The $V_{max}$ of eastern vortex (m/s)	Initial orientation of two TCs	$\beta/ f$ - plane
NE-CTL	Existence	30	10	NE-SW	$\beta$
NE-WMT	Existence (reduced 20%)	30	10	NE-SW	$\beta$
NE-NMT	Not existence	30	10	NE-SW	$\beta$
NE-SVI	Existence	30	30	NE-SW	$\beta$
NE-LVI	Existence	10	30	NE-SW	$\beta$
FNE-CTL	Existence	30	10	NE-SW	$f$
FNE-SVI	Existence	30	30	NE-SW	$f$
FNE-LVI	Existence	10	30	NE-SW	$f$
NW-CTL	Existence	30	10	NW-SE	$\beta$
NW-SVI	Existence	30	30	NW-SE	$\beta$
NW-LVI	Existence	10	30	NW-SE	$\beta$

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673 **Fig. 1.** (a) The JMA 12-hourly best tracks of Noru (blue) and Kulap (red) from 00  
674 UTC 23 July to 00 UTC 28 July 2017. The typhoon symbols denote the beginning  
675 and ending or the typhoon positions from the JMA best track data. The dashed line  
676 represents the TC's best tracks before it transitions to an extratropical cyclone. The  
677 solid line represents the time period of interest in this study; (b) The evolution of  
678 relative positions of two TCs. The origin (0, 0) is the middle point between two  
679 vortices at each time; (c)-(d) The 850 hPa wind (vector; unit:  $\text{m s}^{-1}$ ) and vorticity  
680 (shading, unit:  $1 \times 10^{-5} \text{ s}^{-1}$ ) on 00 UTC 23 July and 00 UTC 28 July 2017.

681 **Fig. 2.** (a) The 12-hourly track positions of Noul (blue line) and Dolphin (red line)  
682 from 00 UTC 4 May to 00 UTC 9 May 2015. The typhoon symbols denote the  
683 beginning and ending or the typhoon positions from the JMA best track data. The  
684 dashed line represents the TC's best tracks before it transitions to an extratropical  
685 cyclone. The solid line represents the time period of interest in this study; (b) The  
686 evolution of relative positions of two TCs in which the origin (0, 0) is the middle  
687 point between two vortices at each time; (c)-(d) The 850 hPa wind (vector; unit:  
688  $\text{m s}^{-1}$ ) and vorticity (shading, unit:  $1 \times 10^{-5} \text{ s}^{-1}$ ) on 00 UTC 4 May and 00 UTC 9  
689 May 2015, respectively.

690 **Fig. 3.** Evolutions of the steering flows at different scales of the Noru (left panels) and  
691 Kulap (right panels).  $C_X$  and  $C_Y$  (black lines) represent the TC's actual movement  
692 speed.  $C_{XL}$  and  $C_{YL}$  (blue lines) show the large-scale steering flow. X and Y denote the  
693 zonal and meridional components, respectively.

694 **Fig. 4.** As in Fig.3, but for Typhoon Noul (left panels) and Dolphin (right panels).

695 **Fig. 5.** Initial configurations of (a) 850 hPa wind fields of ideal MT and (b) vertical  
696 structure of zonal winds.

697 **Fig. 6.** The tracks (top) and relative positions (bottom) of TCW (black lines) and TCE  
698 (red lines) in NE-CTL (left panels), NE-NMT (middle panels), and NE-WMT (right  
699 panels) from  $t = 0$  h to 120 h.

700 **Fig. 7.** Time evolutions of 850 hPa wind (vector; unit:  $\text{m s}^{-1}$ ) and vorticity (shading;  
701 unit:  $1 \times 10^{-5} \text{ s}^{-1}$ ) in NE-CTL (left panels), NE-NMT (middle panels), and NE-WMT  
702 (right panels), respectively.

703 **Fig. 8.** Evolutions of the steering flows at different scales of the TCW (left panels) and  
704 TCE (right panels) in NE-CTL.  $C_X$  and  $C_Y$  (black lines) represent the actual moving  
705 speed of TC.  $C_{XL}$  and  $C_{YL}$  (blue lines) show the large-scale steering flow.  $C_{XW}$ ,  $C_{YW}$ ,  
706  $C_{XE}$  and  $C_{YE}$  (red lines) present the impact of TCW and TCE on the other storm. X  
707 and Y denote the zonal and meridional components, respectively.

708 **Fig. 9.** As in Fig.8, but for NE-WMT.

709 **Fig. 10.** The tracks (top) and relative positions (bottom) of TCW (black lines) and TCE  
710 (red lines) in NE-CTL (left), NE-SVI (middle) and NE-LVI (right) from  $t = 0$  h to 120  
711 h.

712 **Fig. 11.** As in Fig.8, but for NE-SVI (left two panels), and NE-LVI (right two panels).

713 **Fig. 12.** The tracks (top) and relative positions (bottom) of TCW (black lines) and  
714 TCE (red lines) in FNE-CTL (left panels), FNE-SVI (middle panels), and FNE-LVI  
715 (right panels) from  $t = 0$  h to 120 h.

716 **Fig. 13.** The tracks (top) and relative positions (bottom) of TCW (black lines) and  
717 TCE (red lines) in NW-CTL (left panels), NW-SVI (middle panels), and NW-LVI  
718 (right panels) from  $t = 0$  h to 120 h.

719 **Fig. 14.** Evolutions of 850 hPa monsoonal wind (vector; unit:  $\text{m s}^{-1}$ ) and vorticity  
720 (shading; unit:  $1 \times 10^{-6} \text{ s}^{-1}$ ) in NE-LVI (top panels) and FNE-LVI (bottom panels).  
721 The white “W” and “E” indicate the positions of TCW and TCE correspondingly at  
722 that moment. Vectors in red represent wind speeds greater than  $10 \text{ m s}^{-1}$ .

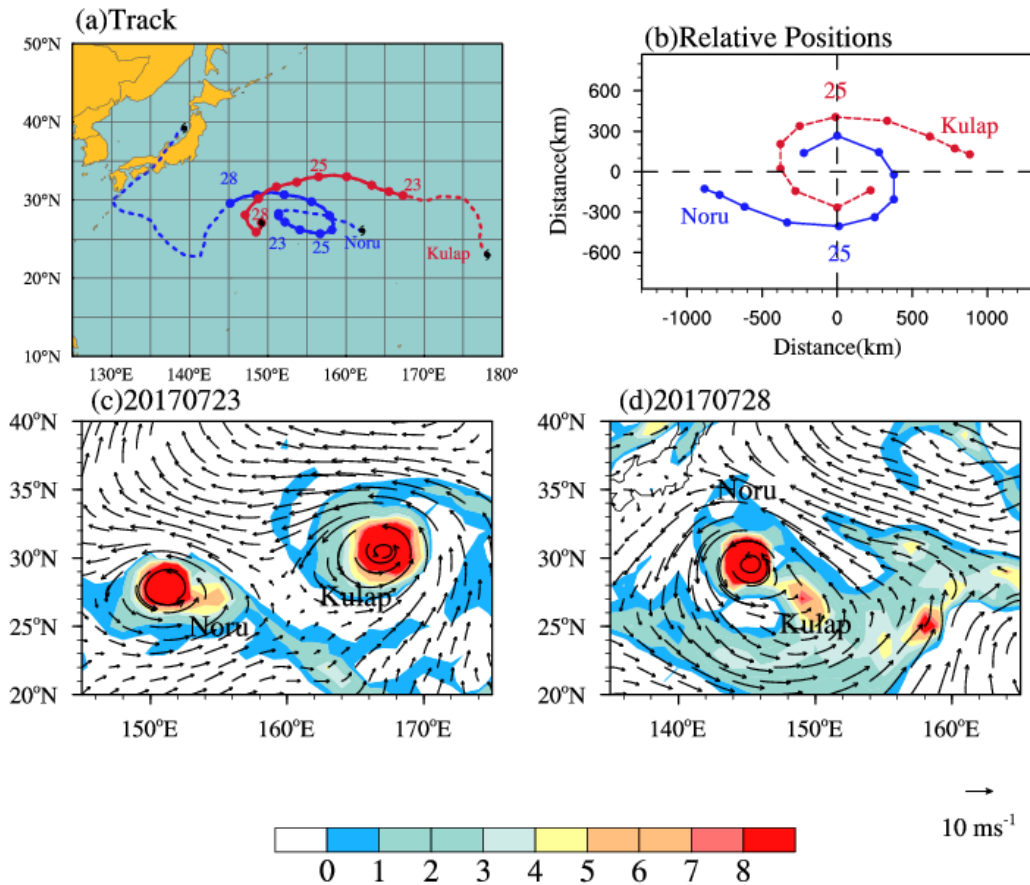
723 **Fig. 15.** Time evolutions of 850 hPa wind (vector; unit:  $\text{m s}^{-1}$ ) and vorticity  
724 (shading; unit:  $1 \times 10^{-5} \text{ s}^{-1}$ ) in NW-CTL (left panels), NW-SVI (middle panels), and  
725 NW-LVI (right panels), respectively.

726 **Fig. 16.** As in Fig.8, but for NW-CTL.

727 **Fig. 17.** As in Fig.8, but for NW-SVI (left two panels) and NW-LVI (right two  
728 panels).

729 **Fig. 18.** Conceptual model of the influences of monsoon trough on the BTCs  
730 interactions in the (a) NE-SW and (b) NW-SE configuration.

731



732

733 **Fig. 1.** (a) The JMA 12-hourly best tracks of Noru (blue) and Kulap (red) from 00 UTC

734 23 July to 00 UTC 28 July 2017. The typhoon symbols denote the beginning and ending

735 of the typhoon positions from the JMA best track data. The dashed line represents the

736 TC's best tracks before it transitions to an extratropical cyclone. The solid line

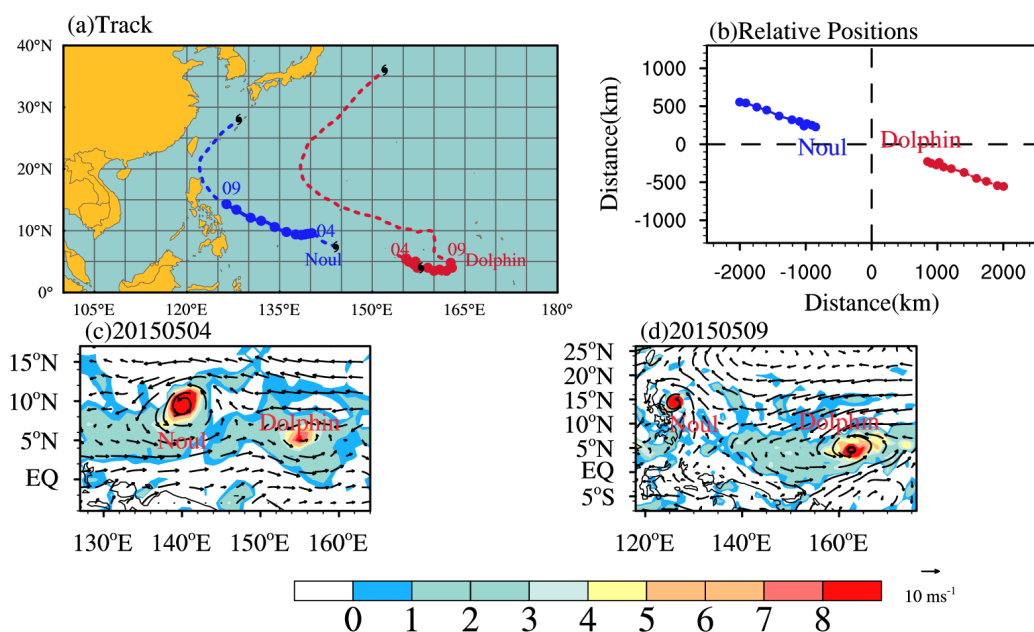
737 represents the time period of interest in this study; (b) The evolution of relative positions

738 of two TCs. The origin (0, 0) is the middle point between two vortices at each time; (c)-

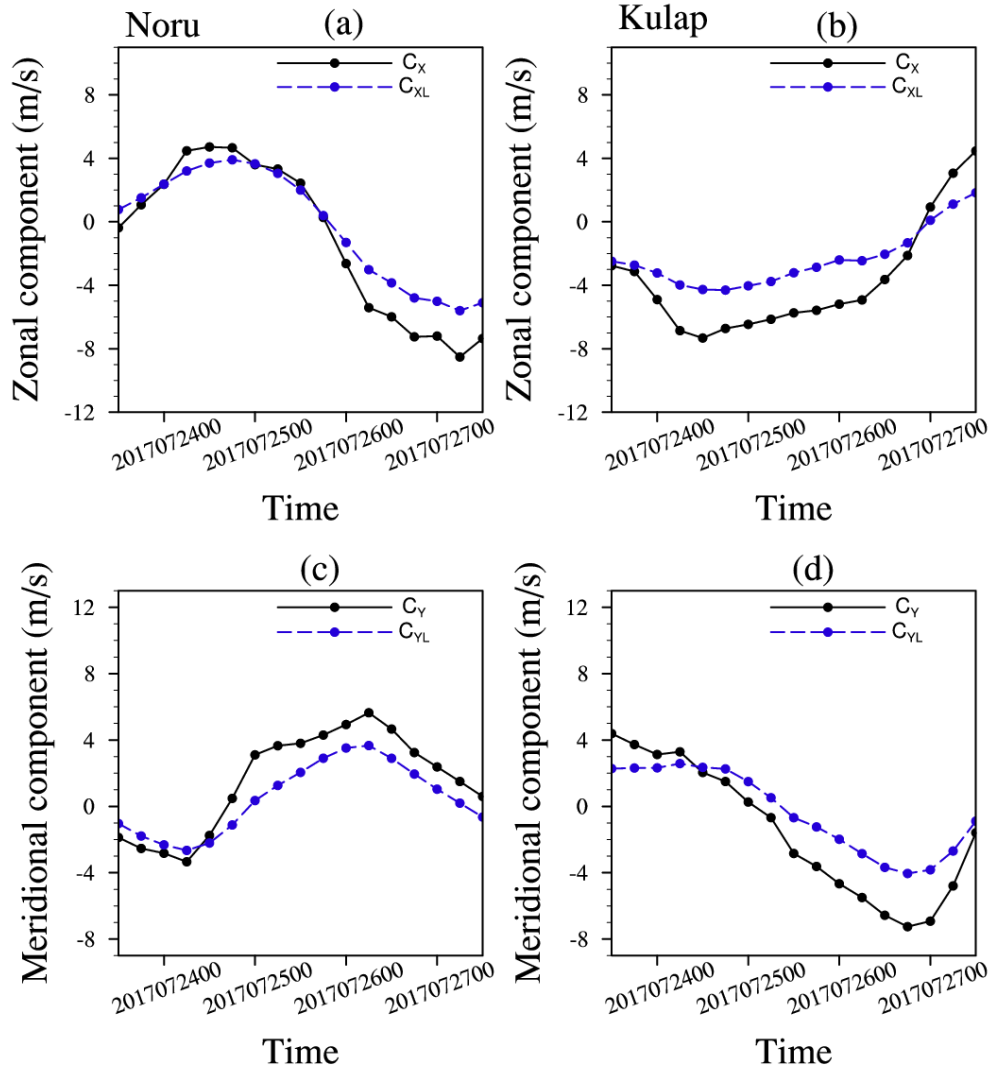
739 (d) The 850 hPa wind (vector; unit:  $\text{m s}^{-1}$ ) and vorticity (shading, unit:  $1 \times 10^{-5} \text{ s}^{-1}$ )

740 on 00 UTC 23 July and 00 UTC 28 July 2017.

741



742  
 743 **Fig. 2.** (a) The 12-hourly track positions of Noul (blue line) and Dolphin (red line)  
 744 from 00 UTC 4 May to 00 UTC 9 May 2015. The typhoon symbols denote the  
 745 beginning and ending or the typhoon positions from the JMA best track data. The  
 746 dashed line represents the TC's best tracks before it transitions to an extratropical  
 747 cyclone. The solid line represents the time period of interest in this study; (b) The  
 748 evolution of relative positions of two TCs in which the origin (0,0) is the middle point  
 749 between two vortices at each time; (c)-(d) The 850 hPa wind (vector; unit:  $\text{m s}^{-1}$ )  
 750 and vorticity (shading, unit:  $1 \times 10^{-5} \text{ s}^{-1}$ ) on 00 UTC 4 May and 00 UTC 9 May  
 751 2015, respectively.  
 752



753

754 **Fig. 3.** Evolutions of the steering flows at different scales of the Noru (left panels) and

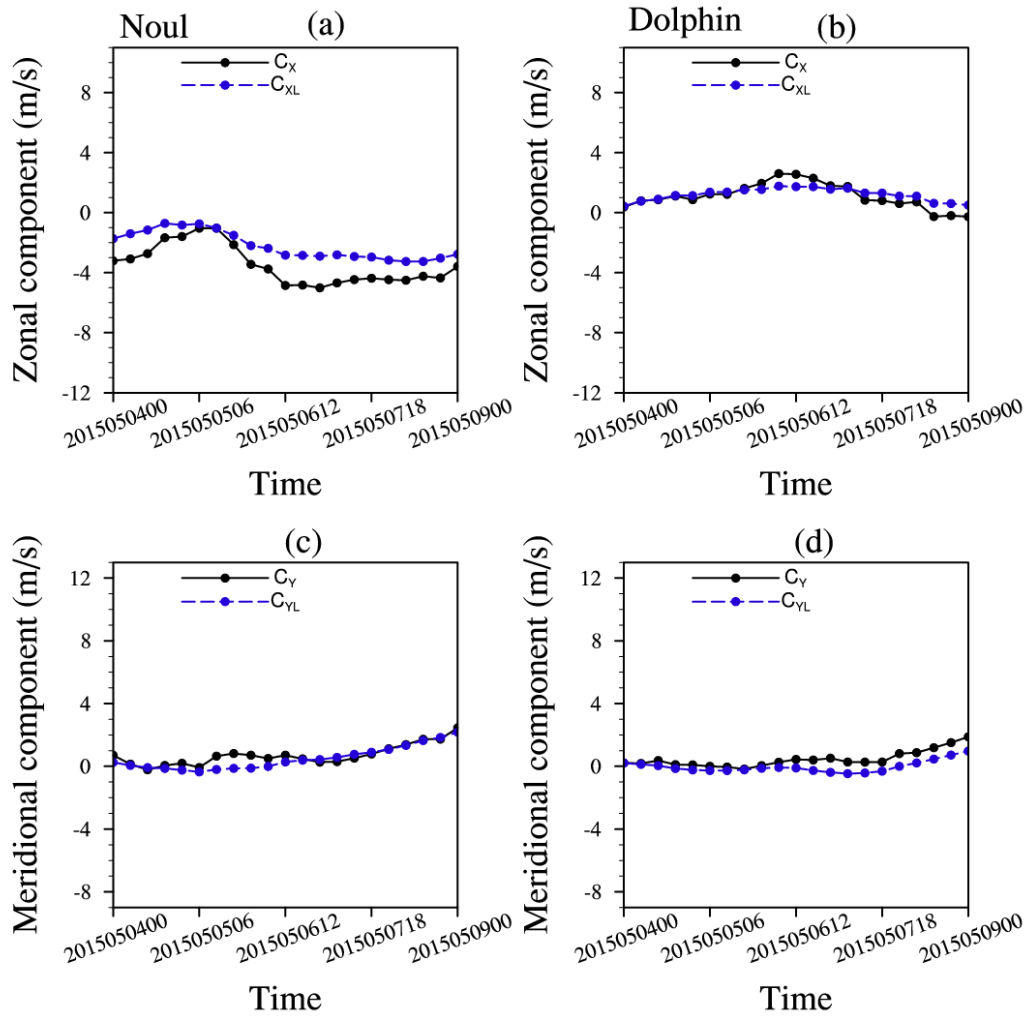
755 Kulap (right panels).  $C_x$  and  $C_y$  (black lines) represent the TC's actual movement

756 speed.  $C_{xL}$  and  $C_{yL}$  (blue lines) show the large-scale steering flow. X and Y denote the

757 zonal and meridional components, respectively.

758

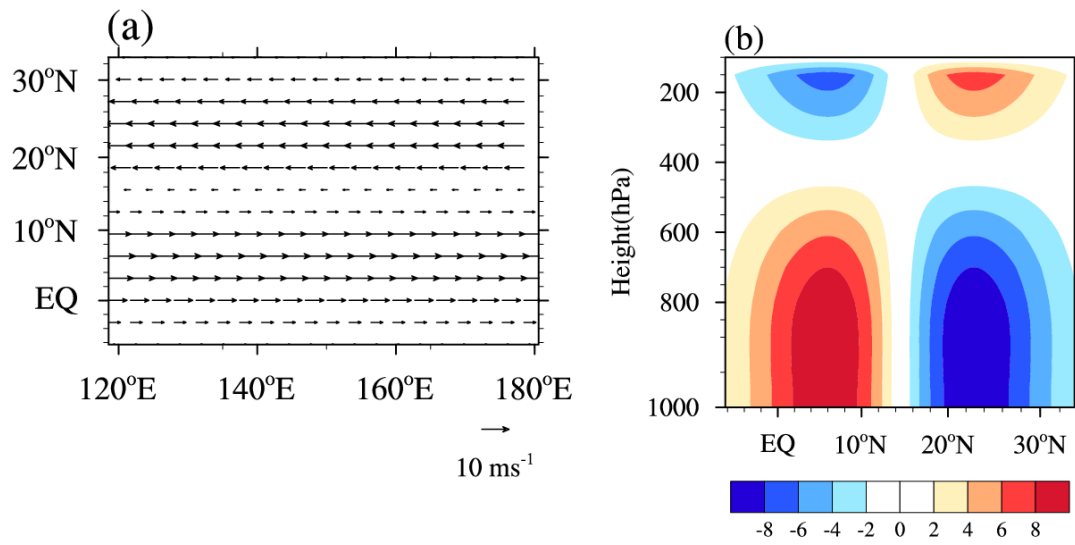




759

760 **Fig. 4.** As in Fig.3, but for Typhoon Noul (left panels) and Dolphin (right panels).

761

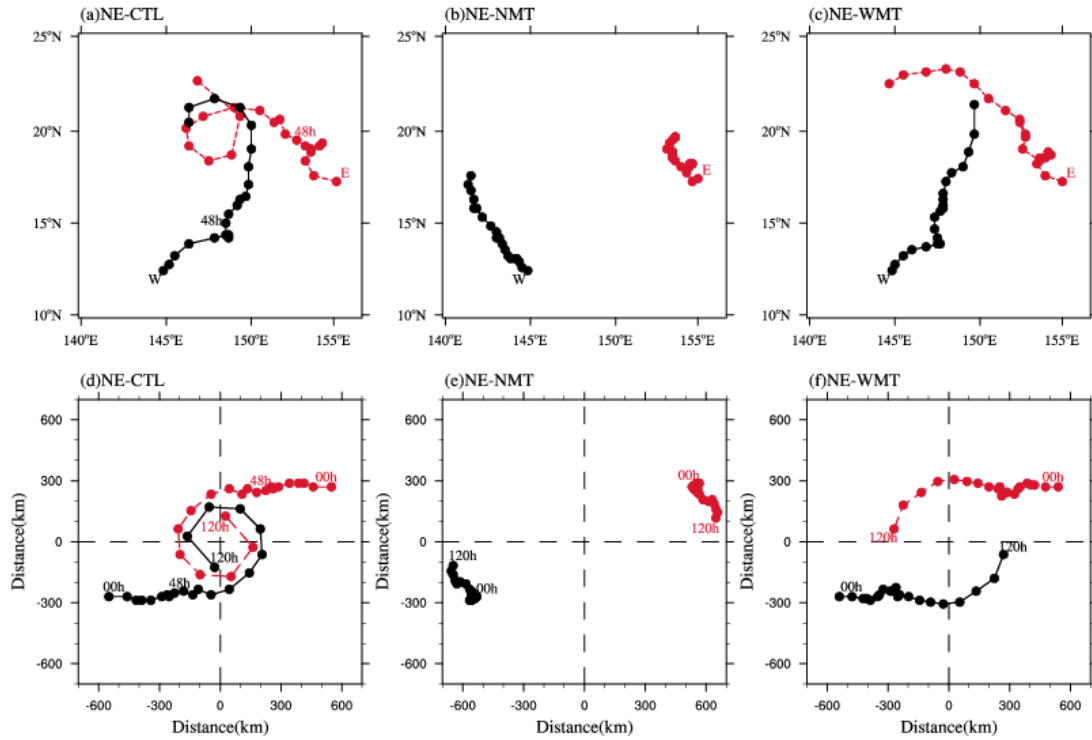


762

763 **Fig. 5.** Initial configurations of (a) 850 hPa wind fields of ideal MT and (b) vertical

764 structure of zonal winds.

765



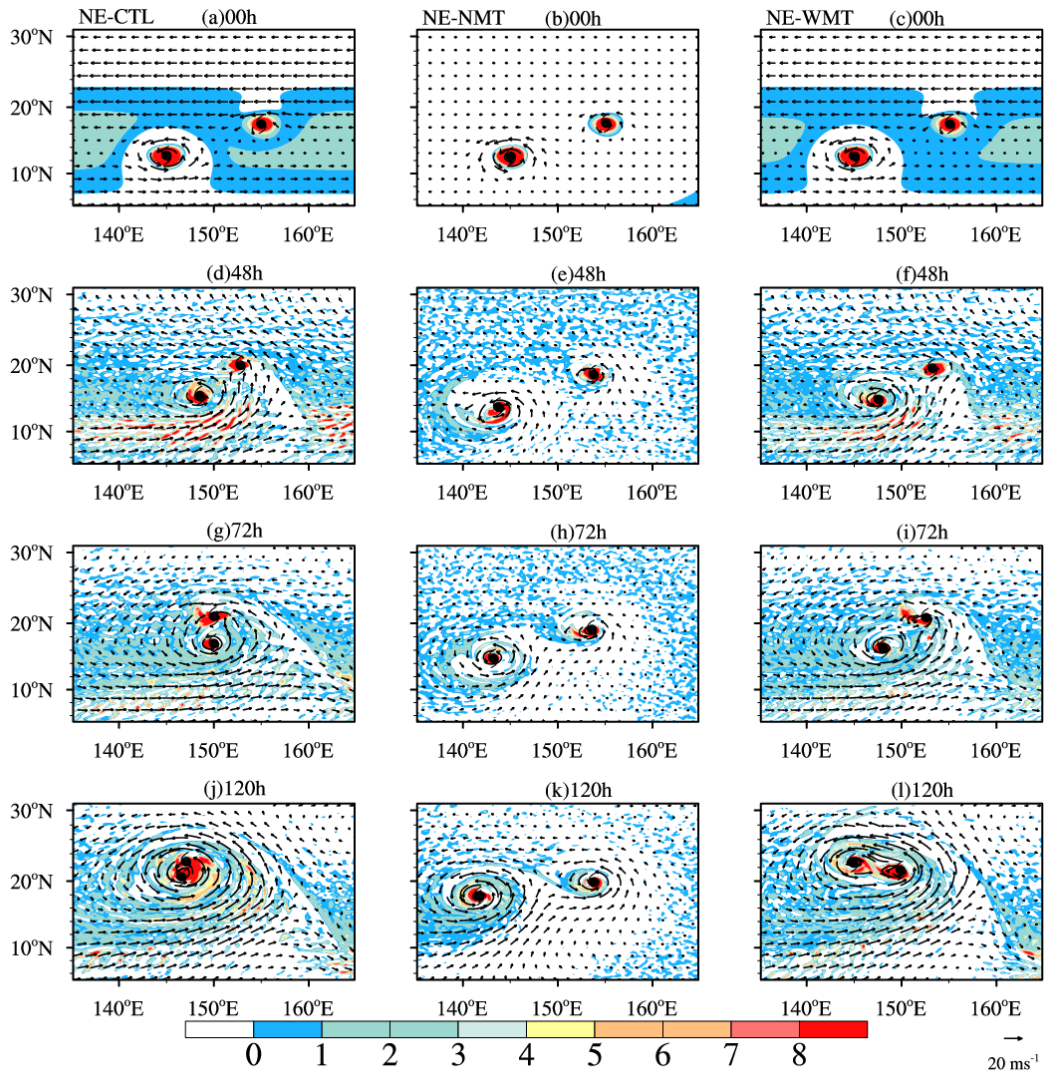
766

767 **Fig. 6.** The tracks (top) and relative positions (bottom) of TCW (black lines) and TCE

768 (red lines) in NE-CTL (left panels), NE-NMT (middle panels), and NE-WMT (right

769 panels) from  $t = 0$  h to 120 h.

770



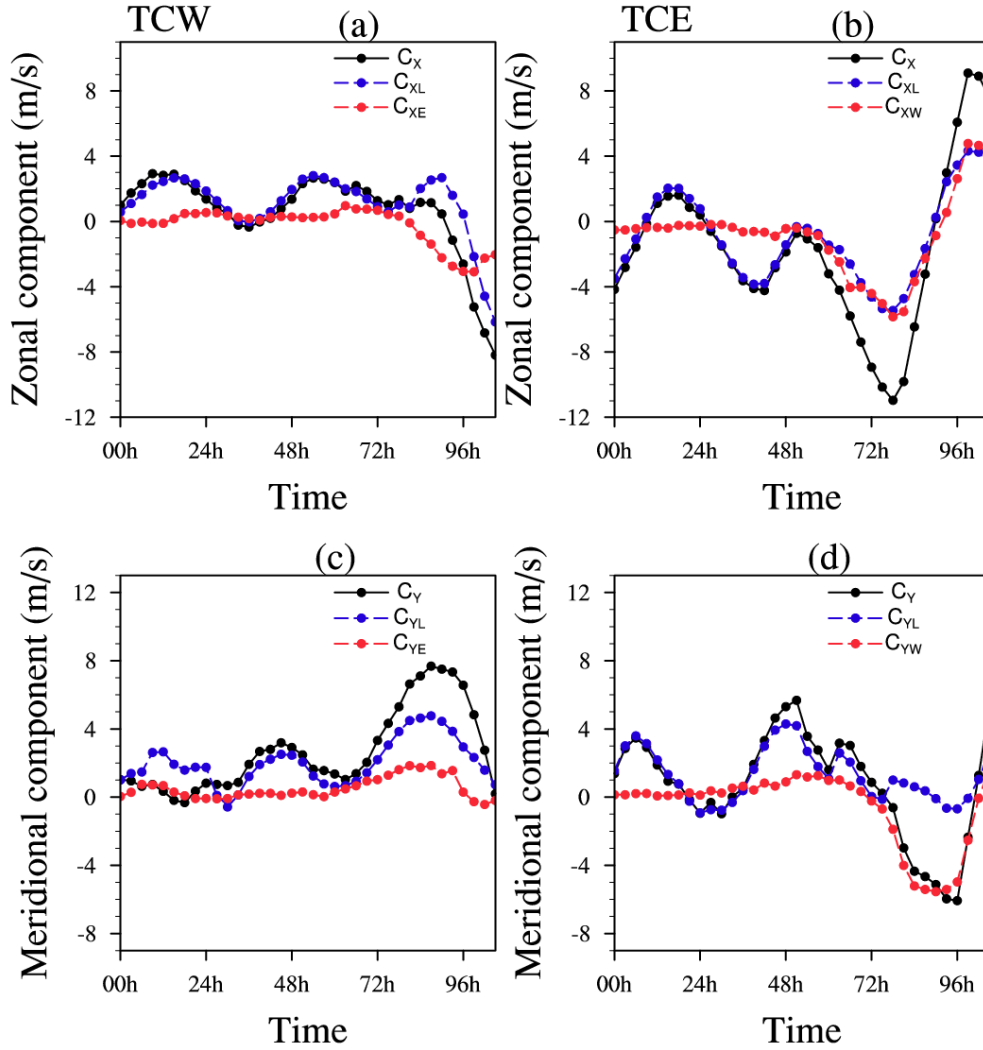
771

772 **Fig. 7.** Time evolutions of 850 hPa wind (vector; unit:  $\text{m s}^{-1}$ ) and vorticity (shading;

773 unit:  $1 \times 10^{-5} \text{ s}^{-1}$ ) in NE-CTL (left panels), NE-NMT (middle panels), and NE-WMT

774 (right panels), respectively.

775



776

777 **Fig. 8.** Evolutions of the steering flows at different scales of the TCW (left panels) and

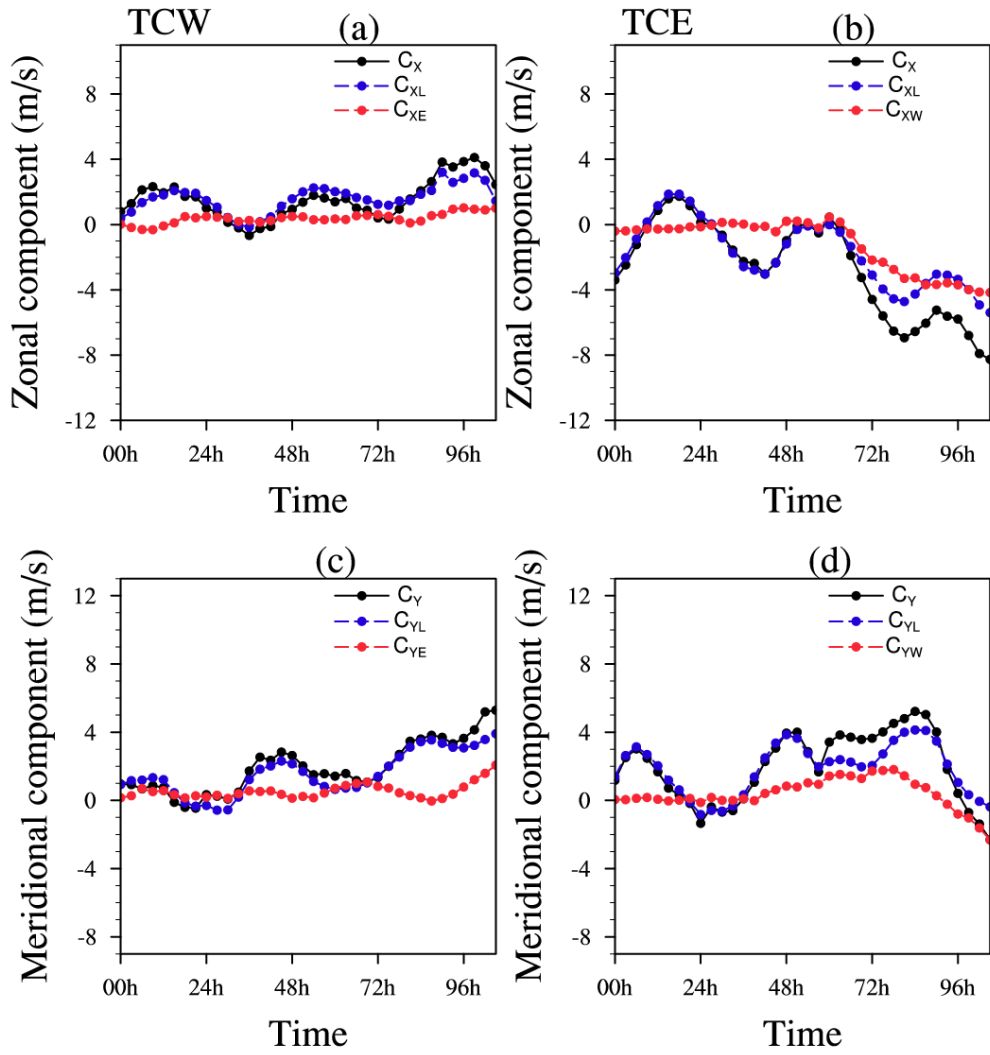
778 TCE (right panels) in NE-CTL.  $C_X$  and  $C_Y$  (black lines) represent the actual moving

779 speed of TC.  $C_{XL}$  and  $C_{YL}$  (blue lines) show the large-scale steering flow.  $C_{XW}$ ,  $C_{YW}$ ,

780  $C_{XE}$  and  $C_{YE}$  (red lines) present the impact of TCW and TCE on the other storm. X

781 and Y denote the zonal and meridional components, respectively.

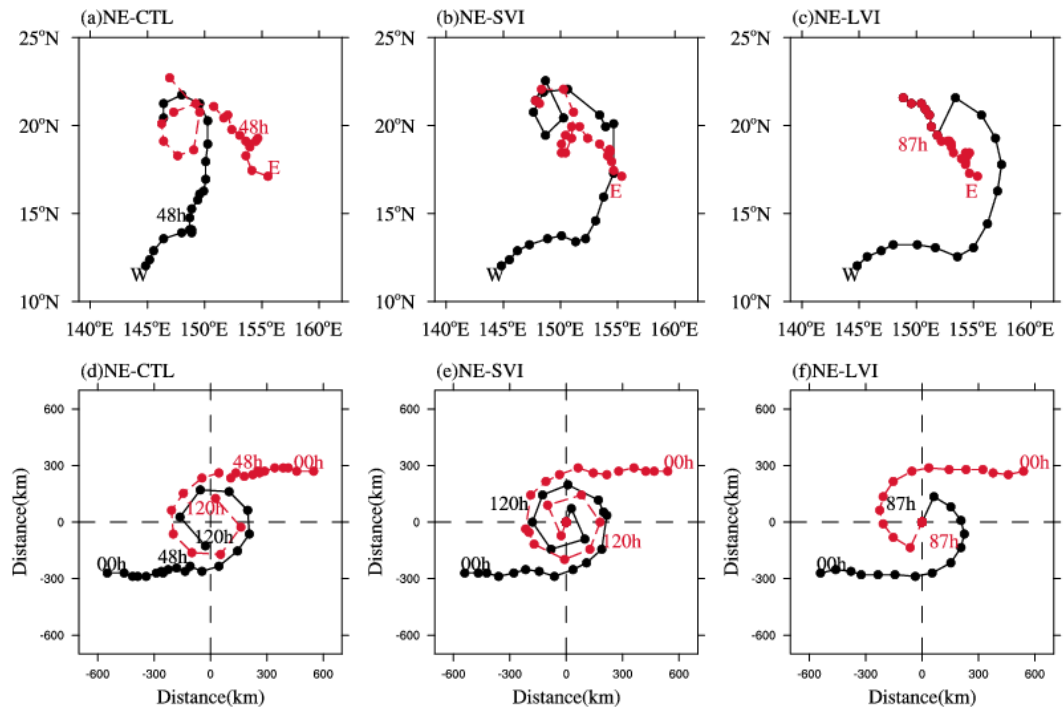
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783

784 **Fig. 9.** As in Fig.8, but for NE-WMT.

785



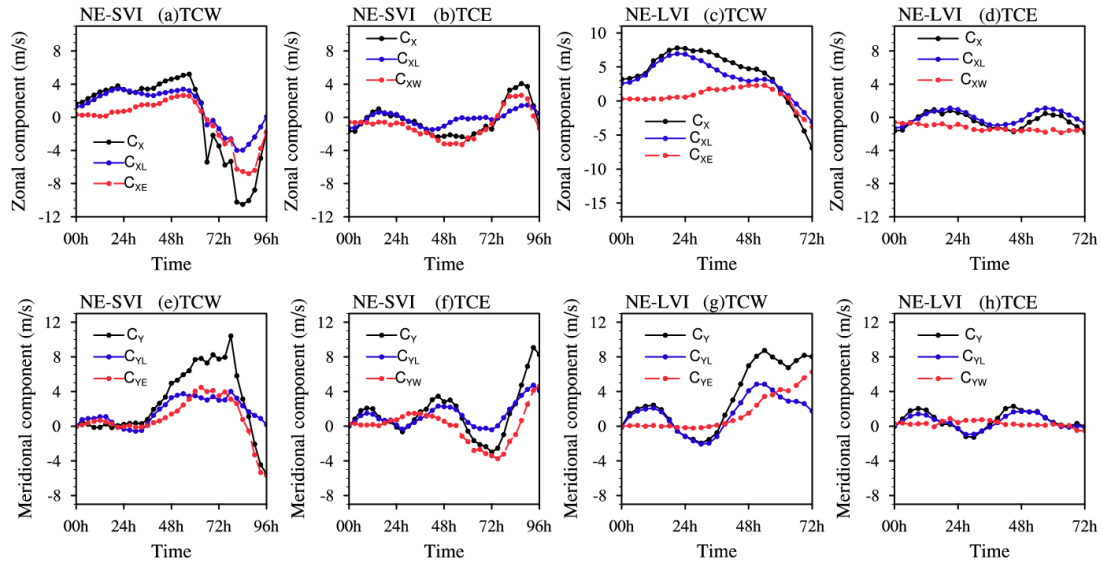
786

787 **Fig. 10.** The tracks (top) and relative positions (bottom) of TCW (black lines) and TCE

788 (red lines) in NE-CTL (left), NE-SVI (middle) and NE-LVI (right) from  $t = 0$  h to 120

789 h.

790

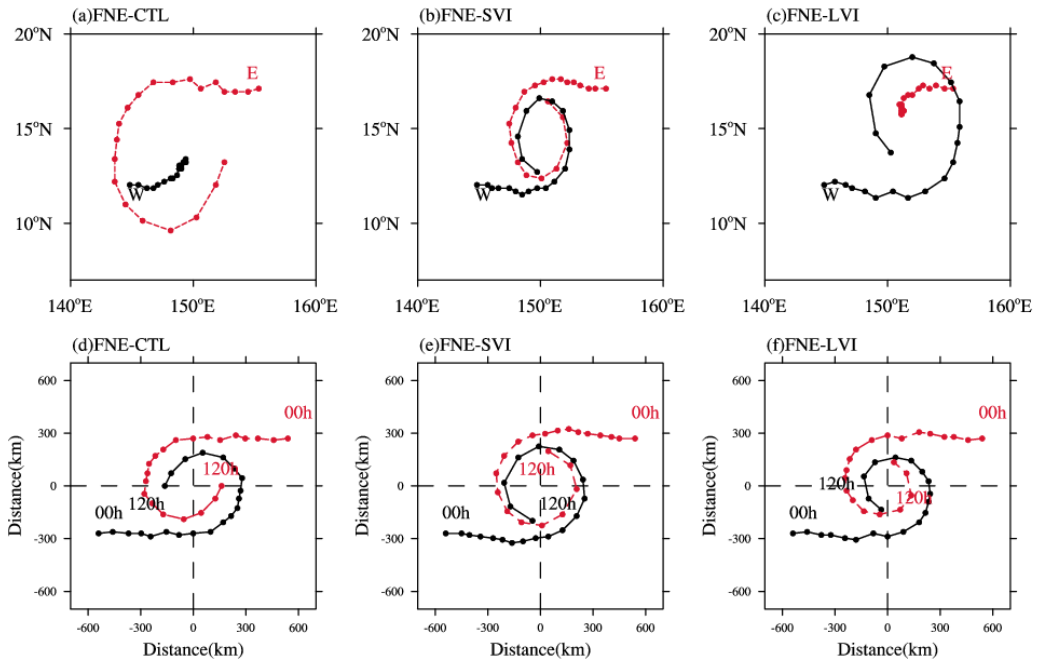


791

792 **Fig. 11.** As in Fig.8, but for NE-SVI (left two panels), and NE-LVI (right two panels).

793





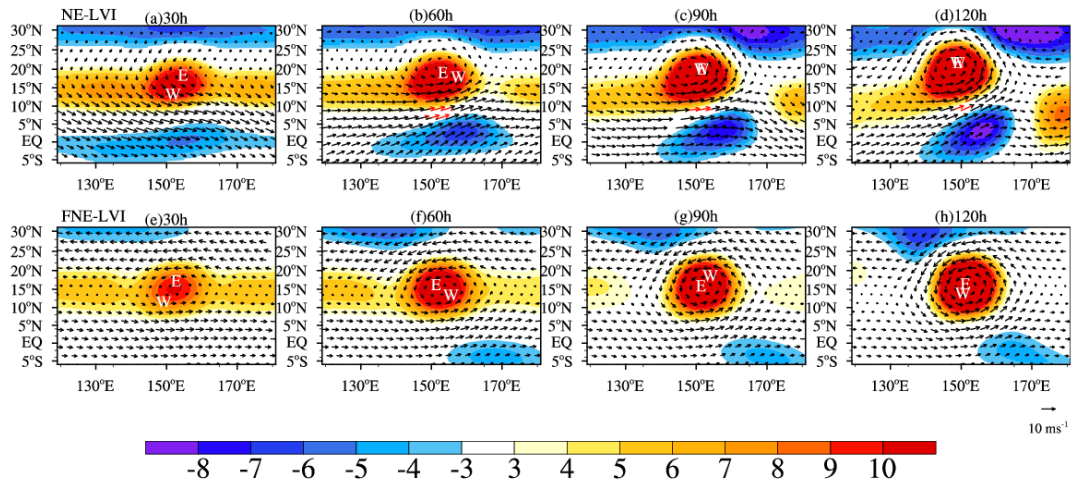
794

795 **Fig. 12.** The tracks (top) and relative positions (bottom) of TCW (black lines) and TCE

796 (red lines) in FNE-CTL (left panels), FNE-SVI (middle panels), and FNE-LVI (right

797 panels) from  $t = 0$  h to 120 h.

798



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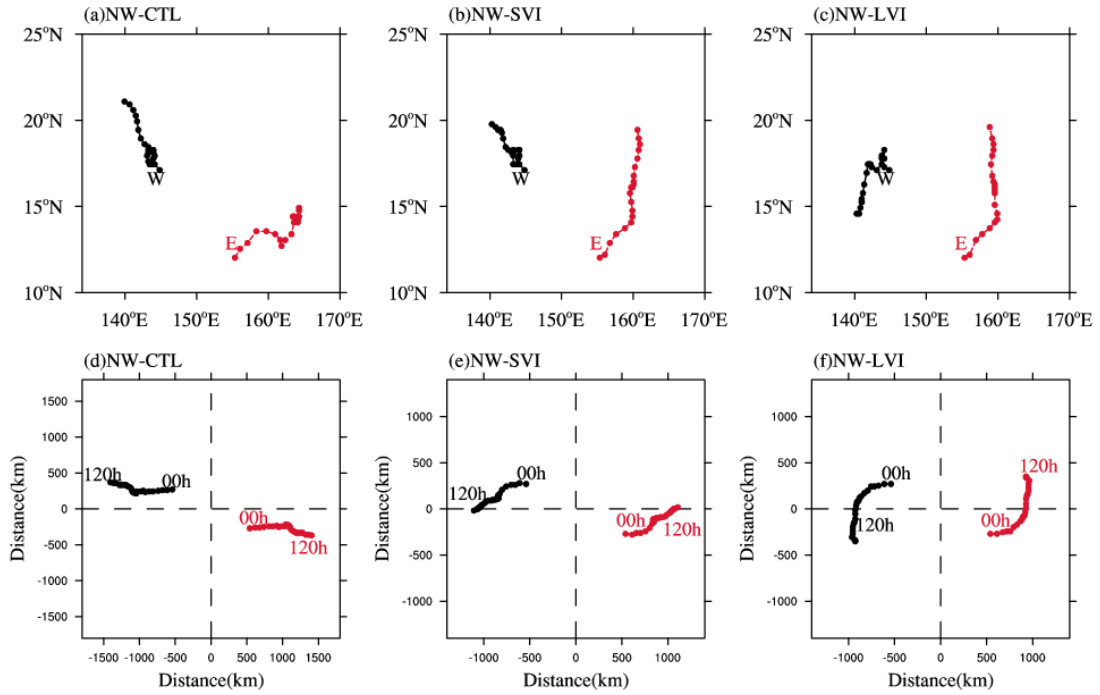
800 **Fig. 13.** Evolutions of 850 hPa monsoonal wind (vector; unit:  $\text{m s}^{-1}$ ) and vorticity

801 (shading; unit:  $1 \times 10^{-6} \text{ s}^{-1}$ ) in NE-LVI (top panels) and FNE-LVI (bottom panels).

802 The white “W” and “E” indicate the positions of TCW and TCE correspondingly at that

803 moment. Vectors in red represent wind speeds greater than  $10 \text{ m s}^{-1}$ .

804



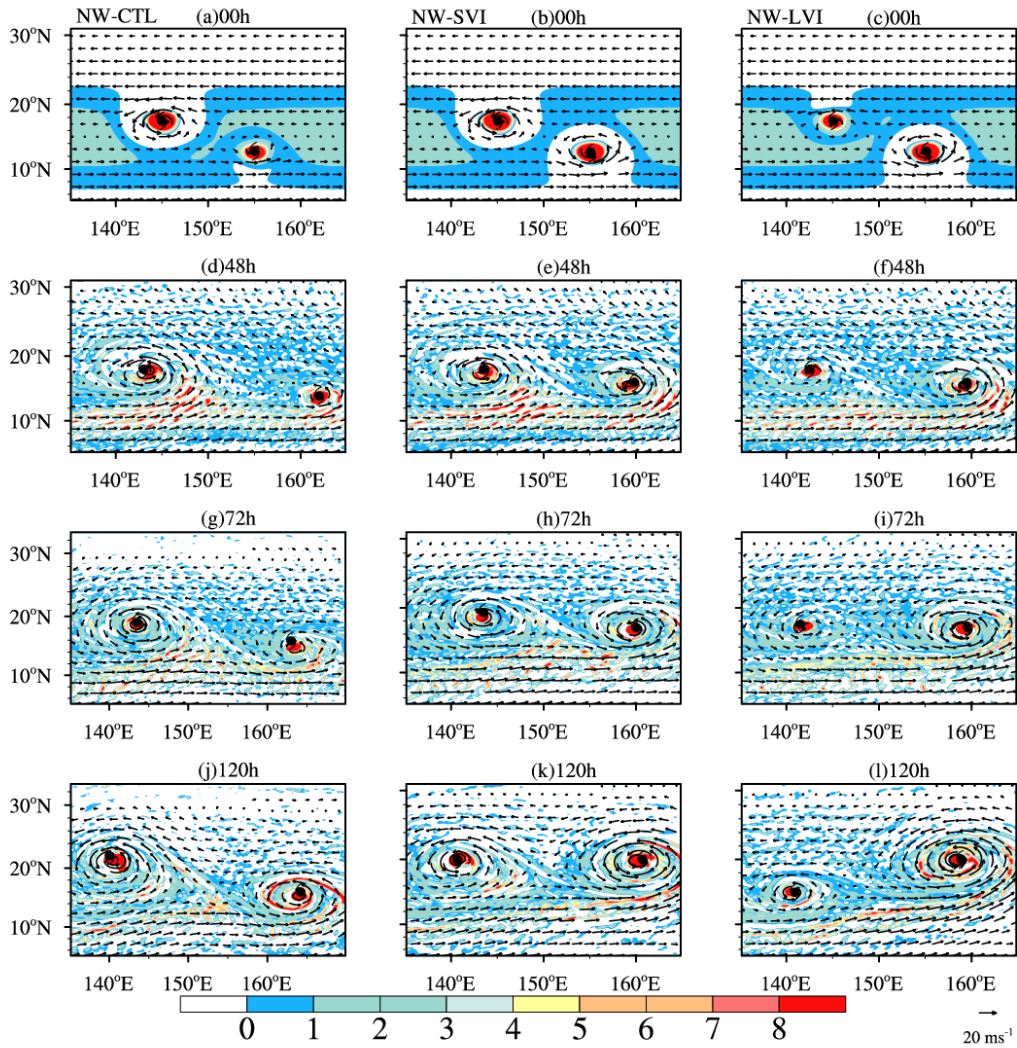
805

806 **Fig. 14.** The tracks (top) and relative positions (bottom) of TCW (black lines) and TCE

807 (red lines) in NW-CTL (left panels), NW-SVI (middle panels), and NW-LVI (right

808 panels) from  $t = 0$  h to 120 h.

809



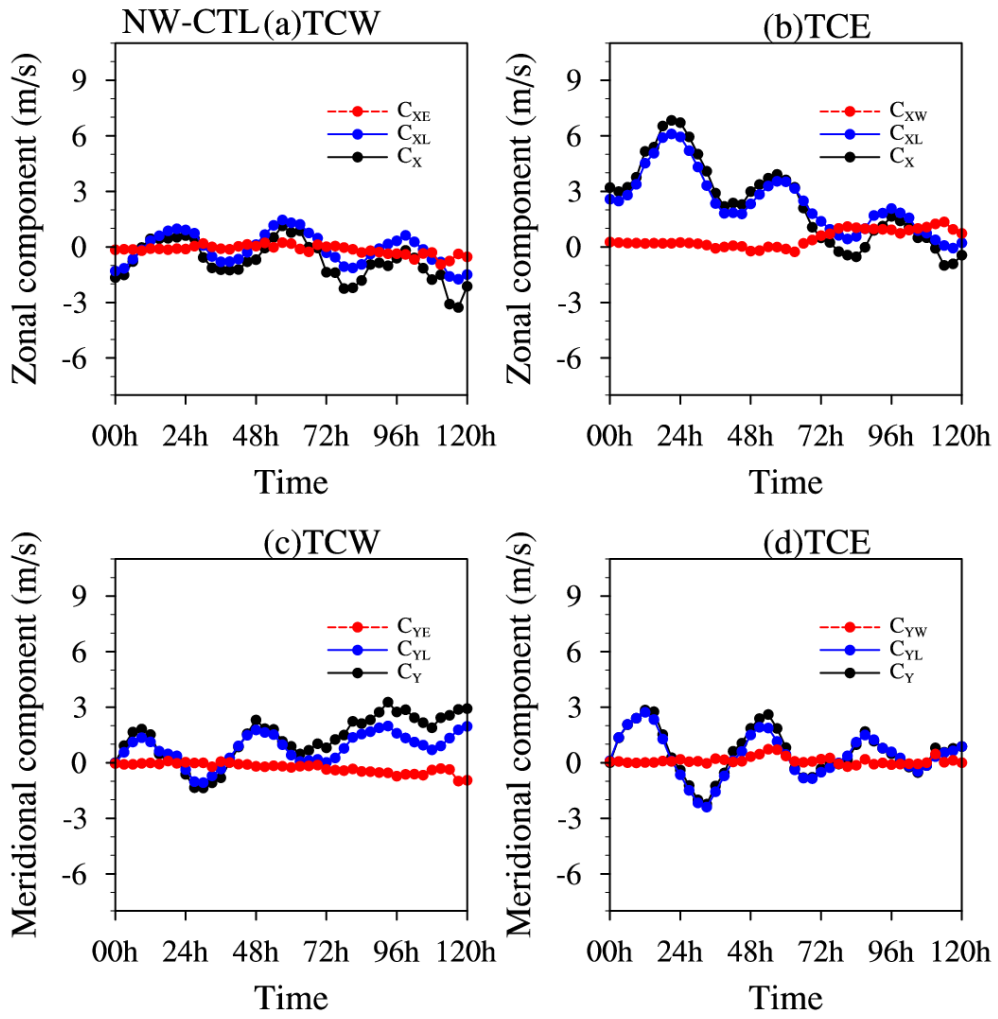
810

811 **Fig. 15.** Time evolutions of 850 hPa wind (vector; unit:  $\text{m s}^{-1}$ ) and vorticity

812 (shading; unit:  $1 \times 10^{-5} \text{ s}^{-1}$ ) in NW-CTL (left panels), NW-SVI (middle panels), and

813 NW-LVI (right panels), respectively.

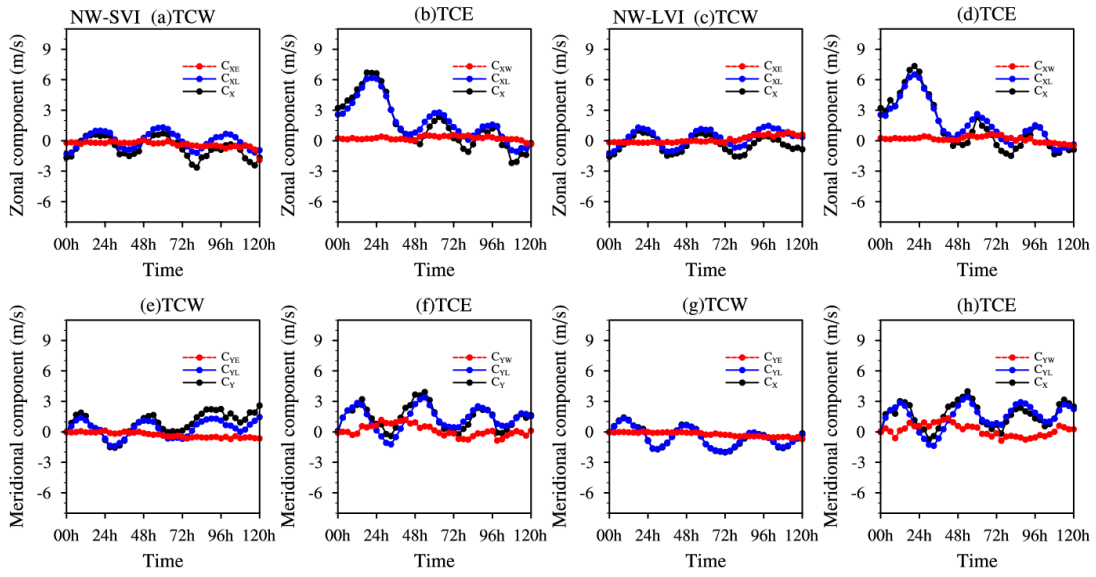
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816 **Fig. 16.** As in Fig.8, but for NW-CTL.

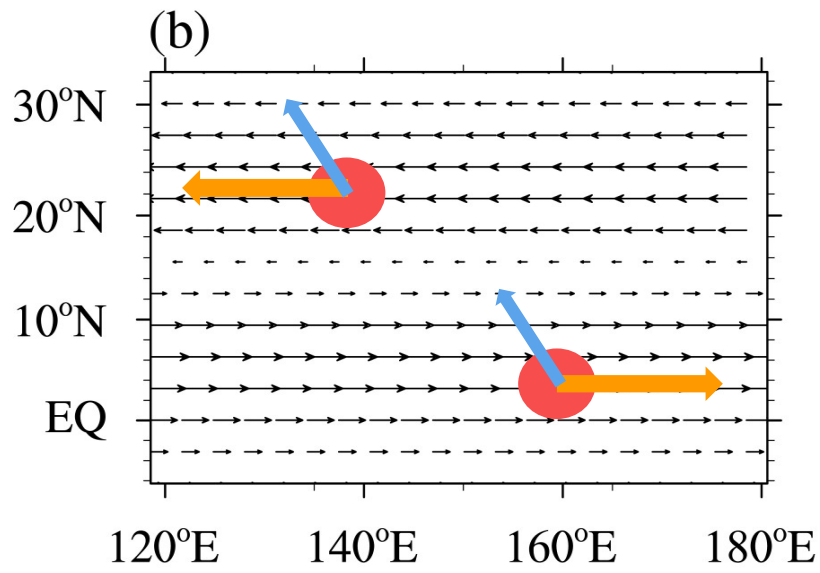
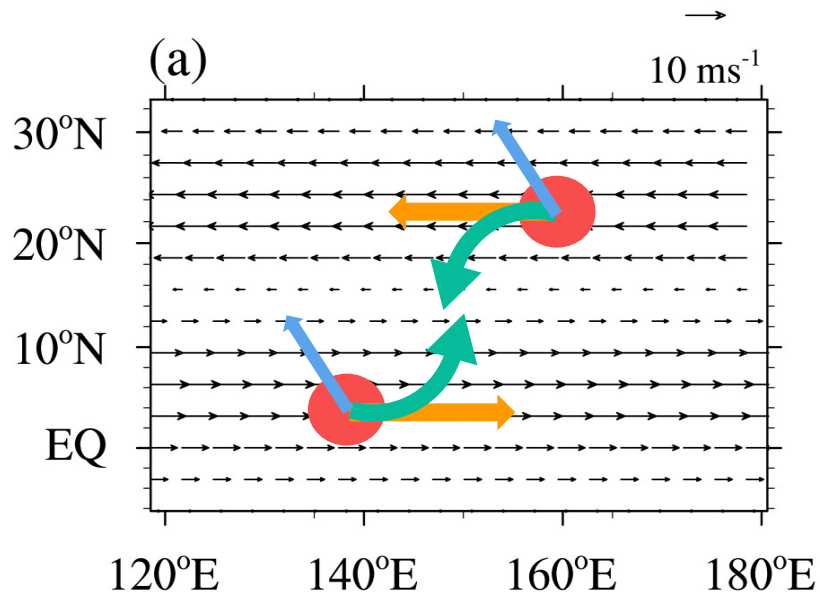
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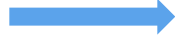




818

819 **Fig. 17.** As in Fig.8, but for NW-SVI (left two panels) and NW-LVI (right two panels).

820



MT steering flow   $\beta$  effect   
 BTCs interaction  TC 

821

822 **Fig. 18.** Conceptual model of the influences of monsoon trough on the BTCs

823 interactions in the (a) NE-SW and (b) NW-SE configuration.